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THESIS

MODELING AIRCRAFT ATTRITION
IN THE AIR DEFENSE ENVIRONMENT

by

George D. Panagakos

March 1986

Thesis Advisor:

Jack B. Gafford

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Modeling Aircraft Attrition in the Air Defense Environment

by

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Submitted in partial fulfillment of the
requirements for the degree of

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from the

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March 1986

ABSTRACT

This thesis presents a high resolution, computer simulation model of aircraft attrition in the air defense environment. The model employs extensive pre-processing submodels and programs in order to efficiently examine tactical scenarios and reduce program execution time. The pre-processing outputs are loaded into a dynamic simulation submodel to analyze the aircraft/air defense engagement sequence. The overall simulation model is modular and can be easily modified to satisfy the user's particular analysis objectives.

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I. INTRODUCTION

A. BACKGROUND

In modern warfare, predicting the attrition of high performance aircraft as they penetrate the hostile area is very important. In general, this prediction depends on many variables. Factors such as weather, terrain, aircraft performance and weapons capabilities affect the air battle greatly. Calculation of aircraft attrition, in large-scale combat models, is difficult because the process is highly stochastic. Current modeling has analyzed aircraft attrition and air defense effectiveness by aggregating many factors.

Two large high resolution combat models, CORDIVEM and VECTOR-2, have used aggregate air models in an attempt to evaluate the effect of air defense against overflight aircraft. The model designers have tried to represent warfare in a realistic and accurate way. However they have ignored or oversimplified factors such as command and control, terrain masking, weather, and enemy electronic countermeasures(ECM). The command and control issues have been oversimplified by assuming that radar sites and firing units act autonomously. Terrain masking, which is extremely important for aircraft survivability, has been totally ignored. Most terrain models require many computations, large data bases, and are cumbersome. ECM capabilities have

been disregarded because they also require extremely high resolution modeling to yield reliable results. High resolution models can be used to combine these factors and add realism to the air battle.

Due to the aggregation methods, sensitivity analysis is much more difficult. The model builder can not easily estimate the change in attrition rate when critical parameters such as aircraft flight level, type of aircraft formation, aircraft speed and ECM capabilities are varied. In general, the current air models have sacrificed detail for computational simplicity.

B. THE PROBLEM

A high resolution (HIRES) model which permits realistic analysis of aircraft attrition must be very complex and contain many submodels and subprograms. Furthermore, the computer time required to execute a HIRES model, as part of a high resolution wargame, is significant. The task facing the model builder is to design a HIRES air model that is efficient and produces acceptable results in a timely manner.

Lee and Cho introduced a framework for designing attrition models in their Naval Postgraduate thesis entitled, A Generalized Approach to Air Defense Combat Modeling, September 1985. This author has implemented their concepts by designing and programming a high resolution aircraft attrition model which improves the analyst's capability to account for the uncertainties in the air attack/defense problem.

C. THESIS OBJECTIVES

The objectives of this thesis are:

1. To create a model which realistically estimates the attrition of an aircraft formation during its route across the hostile area.
2. To program the model so that most calculations are performed in an off-line, pre-processing mode.
3. To design the dynamic simulation segment of the model to take advantage of the pre-processing output and efficiently simulate the stochastic elements of the air battle.
4. To perform sensitivity analyses of the critical variables in the air attack/defense problem.

D. APPROACH

The air model will be developed in the following sequence.

1. Pre-Processing Sub-Models

The deterministic elements of the air battle will be accounted for in this phase.

a. Terrain

The terrain module will be developed and used to calculate a minimum altitude of detection matrix for all radar sites contained in the simulation (Chapters II and III).

b. Detection Geometry

The detection module will be developed and used to determine the possibility of detection based on line-of-sight and acquisition radar range considerations (Chapter IV)

c. Aircraft Movement

The aircraft movement module will be developed to simulate the flight paths of all the aircraft in the scenario (Chapter V).

d. Engagement

The detection, acquisition, interception, and prioritization modules will be developed to determine the feasibility of the engagement sequence (Chapter VI)

2. Dynamic Sub-Models

The stochastic elements of the air battle will be simulated in this phase. These sub-models will allow for the replication of scenarios and the summarization of probabilistic events. The dynamic portion of the model will use the outputs of the pre-processing submodels for each replication (Chapter VII and VIII).

3. Scenario Demonstration and Model Execution

In Chapter IX, a specific scenario will be described and loaded into the air model. This scenario will be used to demonstrate the execution of the computer simulation and generate sample outputs of a typical air battle. The outputs will be statistically summarized and analyzed. Sensitivity analysis will be performed to demonstrate the relationship between aircraft altitude and expected attrition rate.

E. SUMMARY

The thesis will demonstrate that aircraft attrition in an air defense environment can be efficiently and accurately modeled using high resolution techniques and efficient use of off-line, pre-processing programs and routines.

II. TERRAIN SIMULATION

Terrain simulation must be developed to represent the terrain over which the attacking formation flies.

The attacking aircraft a/c uses terrain masking in order to avoid enemy radar detection. Since radars require line-of-sight, earth detection can be restricted by the interfering terrain form. In order to determine if a radar has line-of-sight (LOS) to the a/c in the air defense simulation, it is necessary to analyze the terrain which lies between the radar and the a/c formation.

This terrain simulation developed in this thesis is based on a grid square method. The area to be analyzed is divided into uniform squares. Other shape such as hexagon could also be used. The length of the side of each square depends on the accuracy of the terrain representation required. The smaller the length, the greater the accuracy of the terrain model. If great accuracy is desired, extensive calculations must be anticipated. This chapter will describe the terrain model and the factors which affect the terrain simulation accuracy.

A. ACCURACY

The most important question concerning terrain modeling is determining the appropriate degree of accuracy. A high resolution terrain representation will require extensive computer processing. Furthermore the formation of the

attacking a/c, the number of a/c, and the flight altitude are also factors which affect the accuracy question and must be considered.

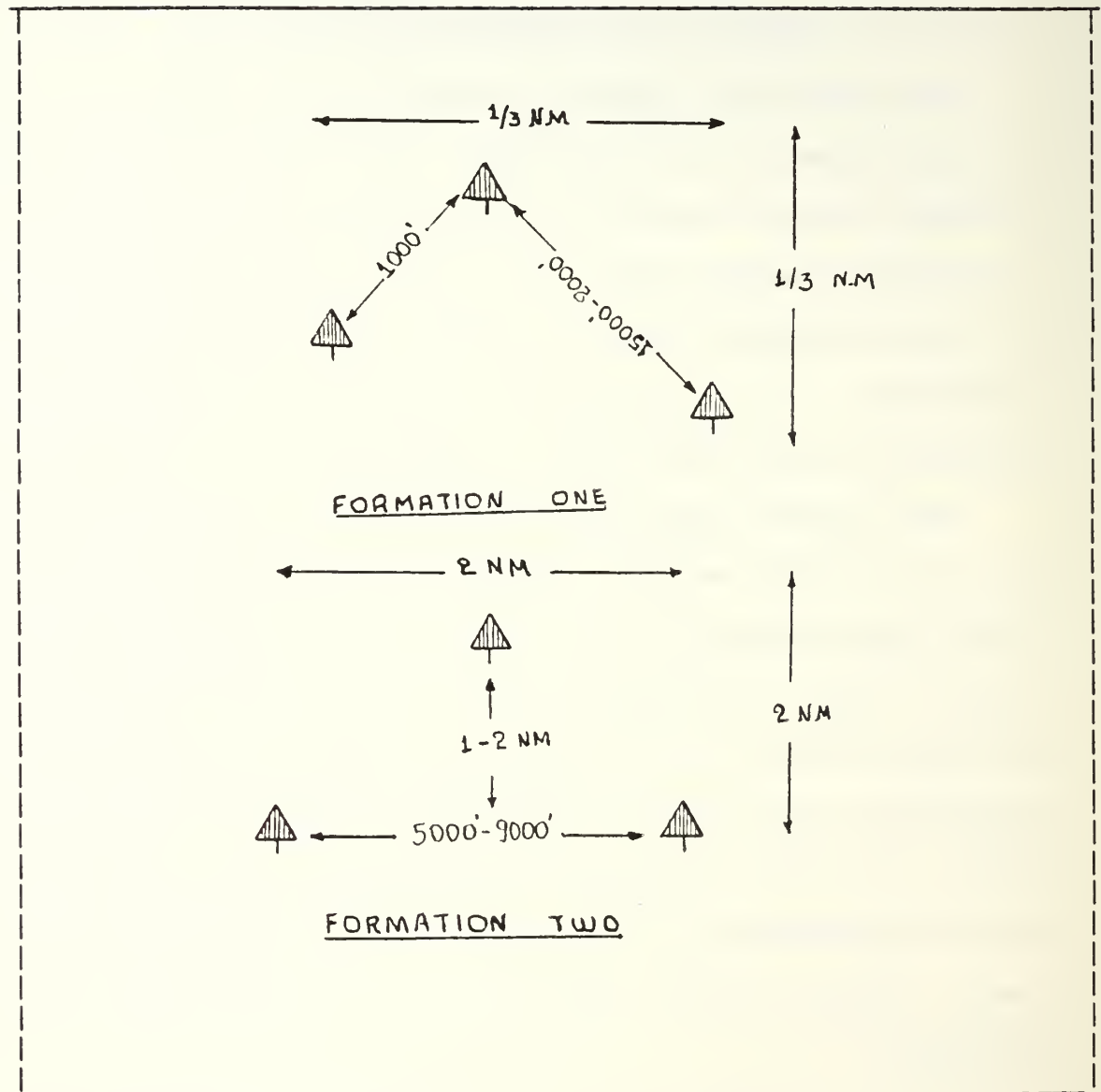


Figure 2.1 Formation of Three A/C

1. Formation

Attack formations vary greatly and depend on the tactics and the mission. For example, consider the two kinds of formation shown in Figure 2.1.

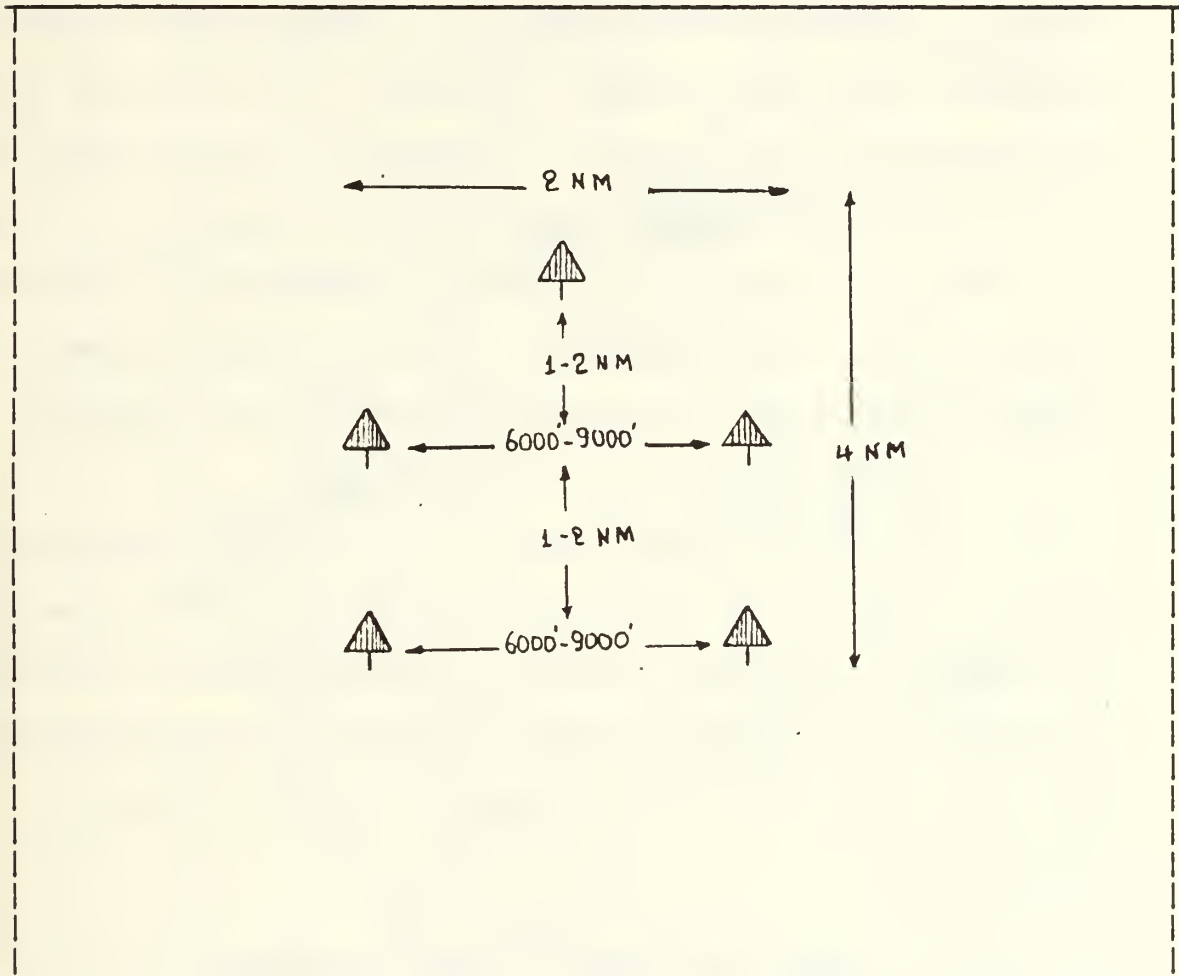


Figure 2.2 Formation of Five A/C

Both formations have three a/c, but formation one has dimensions approximately 1/3 by 1/3 NM while formation two is 2 NM by 2 NM. Because formation one is smaller, it is more flexible and it can use terrain masking better than formation

two. Thus, if the attack formations are of the first type, greater terrain modeling accuracy will be required.

2. Number of A/C

The number of a/c in a given formation also influences the terrain accuracy. The formation in Figure 2.2 above is similar to formation two in Figure 2.1; however, the number of aircraft has been increased. In this case, the five aircraft are flying in a formation which is 4 by 2 NM. This type of formation is less flexible and must fly higher. As a result, less terrain simulation accuracy is required. In particular, the dimensions of the grid square have to be approximately equal to the dimensions of the formation.

3. Flight Level

The flight level used by the attacking formation is also critical to the determination of the terrain simulation accuracy. If the user wants to analyze attrition against extremely low flying aircraft, the terrain simulation must be of very high resolution in order to generate accurate predictions.

B. CALCULATION OF THE GRID SQUARE ALTITUDES

The first step in the procedure used here is to calculate a representation altitude for each grid square. To find the altitude of each grid square corner a map is needed. The desired accuracy of the terrain simulation determines the scale of this map. In general, any military map with scale 1:50,000, 1:250,000 or 1:500,000 is appropriate.

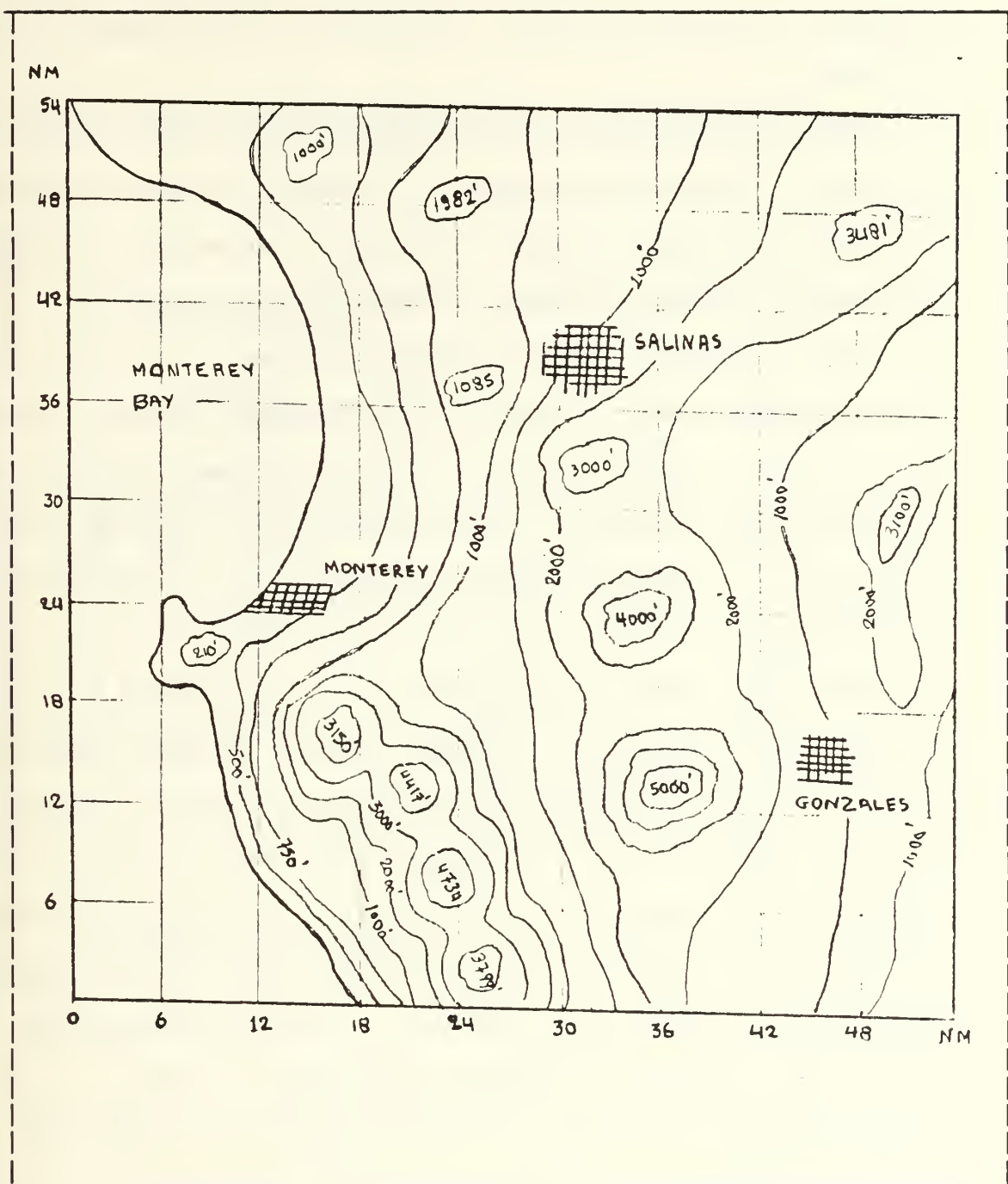


Figure 2.3 Terrain Divided into Square Grids

In Figure 2.3 a military map with a 1:500,000 scale is shown. Consider the map as an example of a defended area divided into grid squares. The size of each square is equal to 6 NM.

This map contains all the information needed for the average altitude calculation. It contains the scale of the ranges and enough contours to extract the heights of the four corners of each grid square in the following manner.

If one contour passes through a corner of the grid square assign the altitude of this contour to this corner. If no contour passes exactly through a corner, we interpolate the altitude between the two contours which contain the particular corner and assign that value to the corner in question.

Figure 2.4 shows an example. The grid square A B C D is used to calculate the average heights in this particular area. Contours pass through the corners A and D so the altitude 2,000 can be assigned to these two corners. For the corners B and C we have to interpolate the heights by using the contours 2,500 and 3,000 feet for point B and contours 3,000 and 3,500 feet for point C. A good approximation height is 2,700 and 3,250 feet for points B and C respectively.

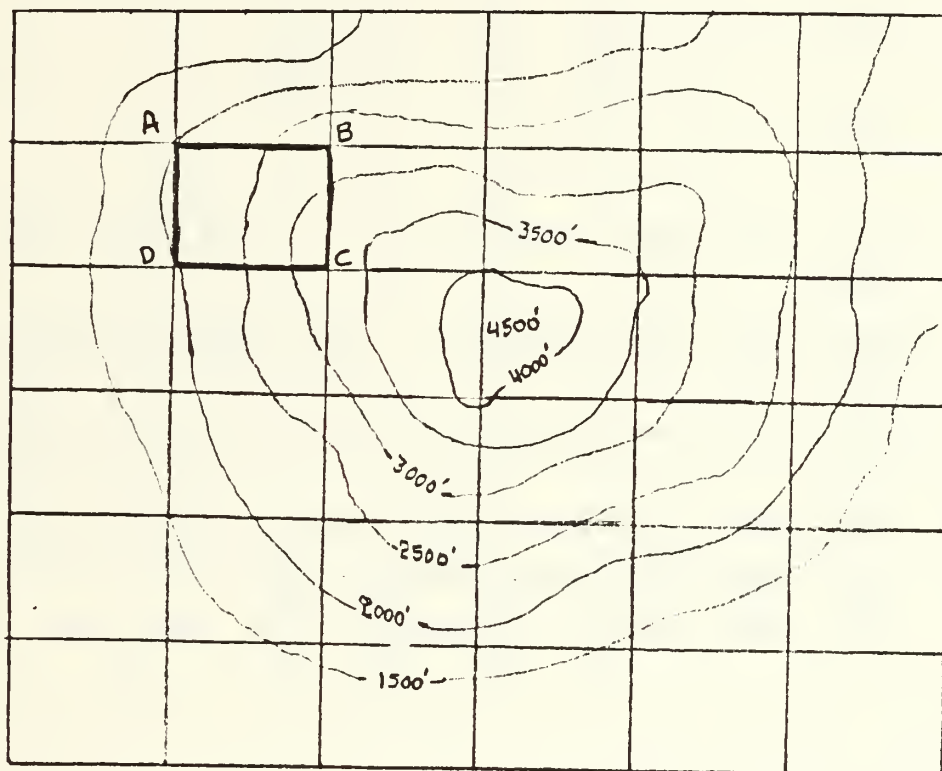


Figure 2.4 Grid Squares and Contours Curves

TABLE 1

ALTITUDES OF THE GRID SQUARE CORNERS

A hand-drawn graph on a grid showing the relationship between wavelength (nm) and intensity. The x-axis is labeled 'nm' and ranges from 0 to 54. The y-axis is labeled 'nm' and ranges from 6 to 42. Data points are plotted at various wavelengths and intensities, with some points labeled with values like 420, 480, 450, 420, 510, 1500, 2000, 500, 512.5, 400, 720, 2800, 3900, 800, 540, 530, 510, 2000, 2050, 1500, 540, 540, 580, 320, 530, 490, 435, 457.5, 440, 372.5, 312.5, 500, 280, 250, 260, 250, 150, 180, 200, 210, 240.

Table 1 shows the altitudes of the grid square corners of the terrain shown in Figure 2.3.

To find these altitudes is cubersome work but it must only be done once. Later average altitudes can be calculated for each grid and a data matrix can be stored to be used for many simulation purposes. Table 2 shows the average altitude of each grid square. After the calculations have been made

in this particular model, each average altitude represents the altitude of a 6 by 6 NM area.

TABLE 2
AVERAGE ALTITUDES OF GRID SQUARES

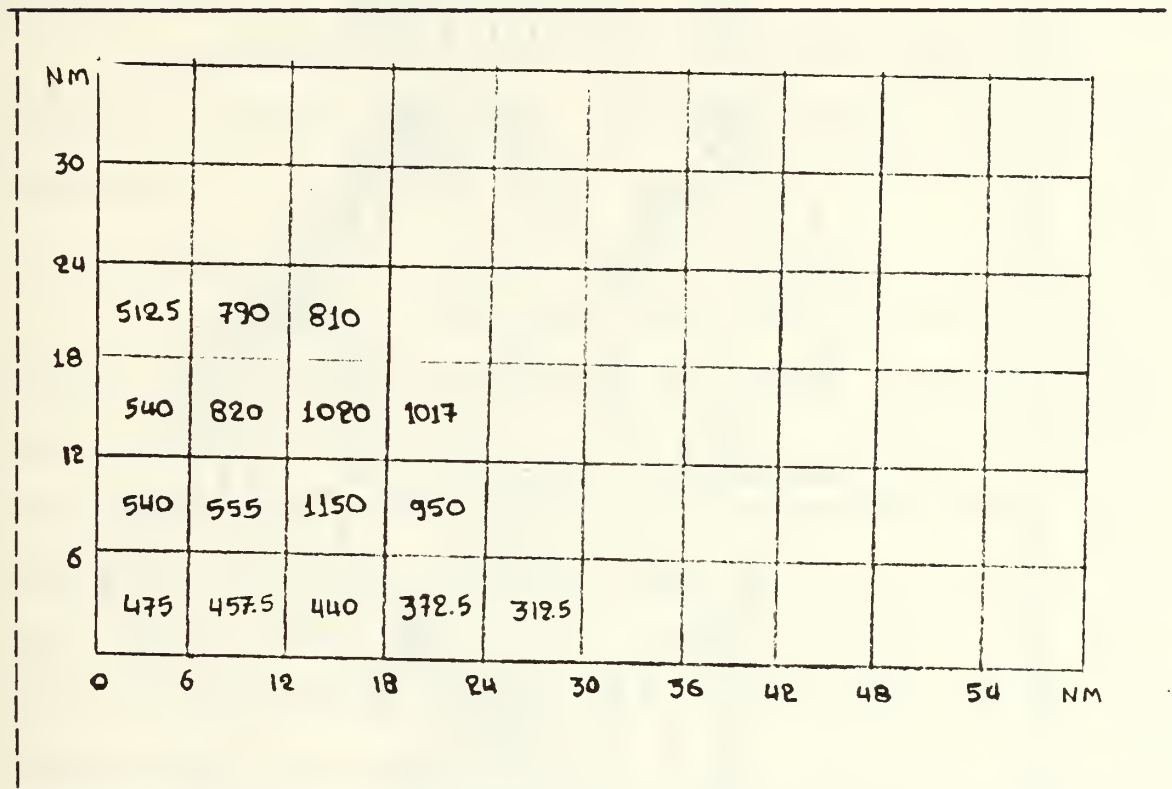


Figure 2.5, shows the plot of terrain made by a computer by using the data in Table 2 and the program in Appendix A. In this figure we can see Monterey Bay and most of the contours which are shown in Figure 2.3 above.

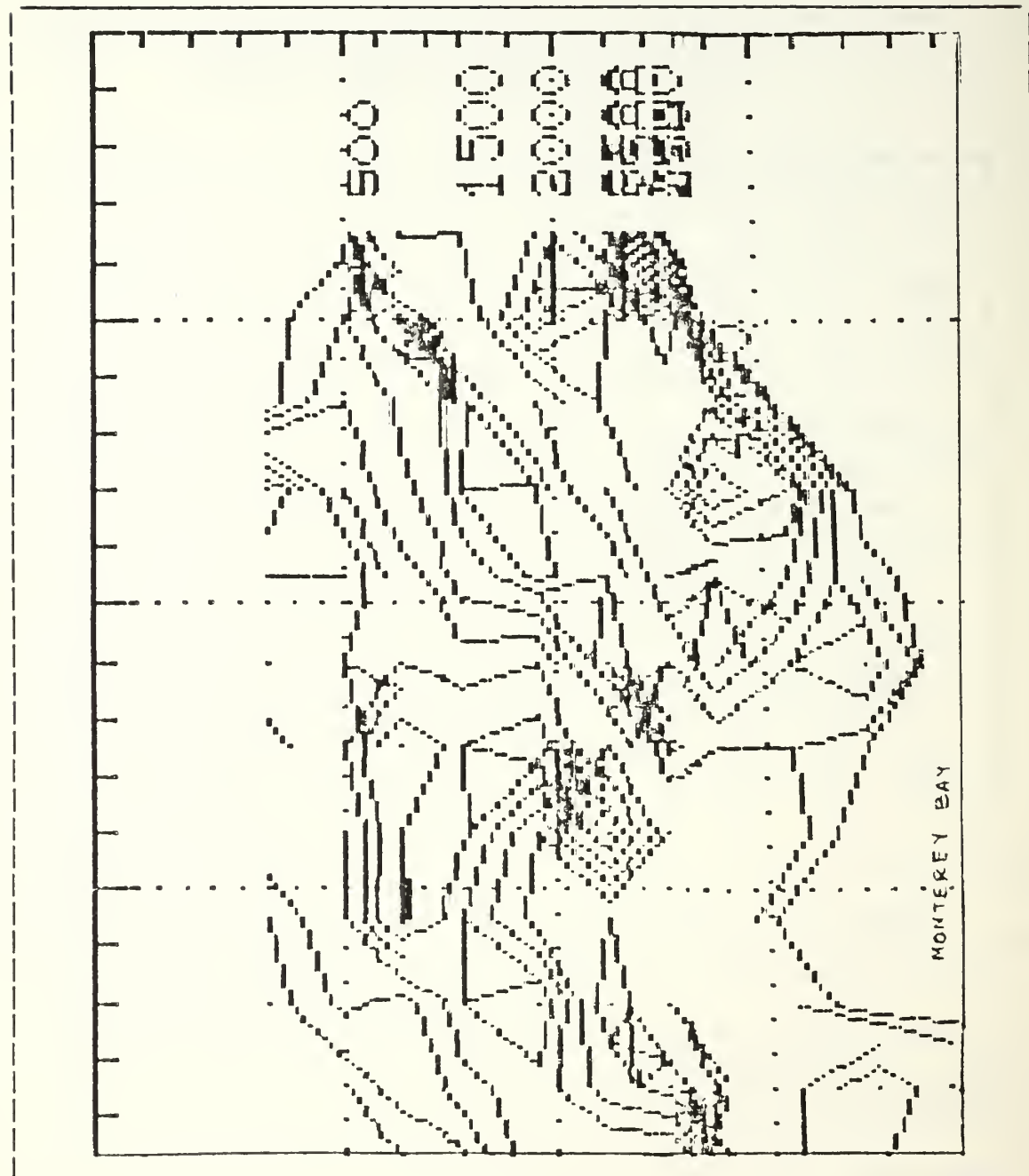


Figure 2.5 Plot of Terrain

C. ADVANTAGES AND DISADVANTAGES OF GRID SQUARE METHOD

1. Advantages

This method is very simple. It does not require difficult mathematical formulas or extensive calculations.

All computations can be done off-line and can be used in many different types of simulations.

The computer program which calculates the average altitudes - shown in Appendix A - can be used in any terrain situation.

2. Disadvantages

The method is discrete. When the average altitude of the grid square is calculated, it is used to represent the altitude for any point inside this area. Figure 2.6 compares the actual terrain with the grid square approximation. The terrain is divided into columns whose bases are squares 6 by 6 NM. By examining the points a and b in column 4, we can see that this method may sometimes overestimates (point b) or underestimates the actual terrain height (point a). This disadvantage can be eliminated by decreasing the length at the side of the square grid, but with the resulting increase in computation.

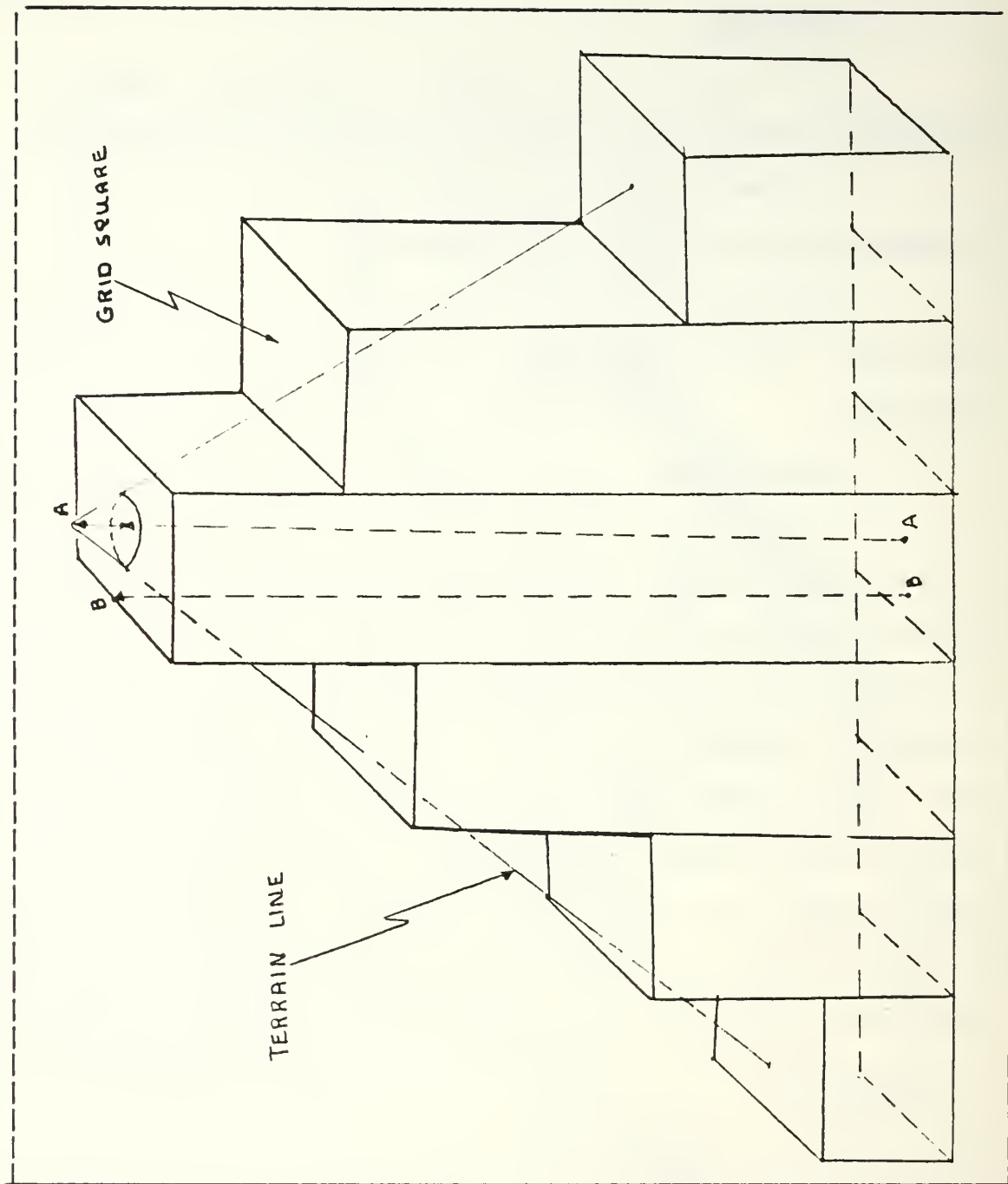


Figure 2.6 Terrain Represented by a Grid Square

III. CONSTRUCTION OF A MINIMUM ALTITUDE GRID

A. INTRODUCTION

The possibility that a radar site will detect a target which penetrates its area depends critically on its ability to "see" in the space where the target flies. Usually, especially in high threat areas, the attacking aircraft use terrain masking to avoid radar detection. On the other hand, radar sites try to improve the ability to "see" as low as possible by using more sophisticated equipment. Both radar sites and aircraft are concerned about the minimum altitudes that a particular radar can detect a target. Radar sites can use this information to find out their limitations and to design the area defense in better way. The attacking a/c can use the minimum altitude grid to plan their penetration route through the enemy area and take advantage of terrain masking. These routes must be planned to avoid radar detection, to save fuel, and to decrease the possibility of navigational errors.

This chapter will develop a model for calculation the minimum altitude grid. This minimum altitude grid will be used in the next chapter to determine radar line-of-sight and the possibility of detection.

B. DESCRIPTION OF THE MODEL

Consider the average altitude grid shown in Figure 3.1.

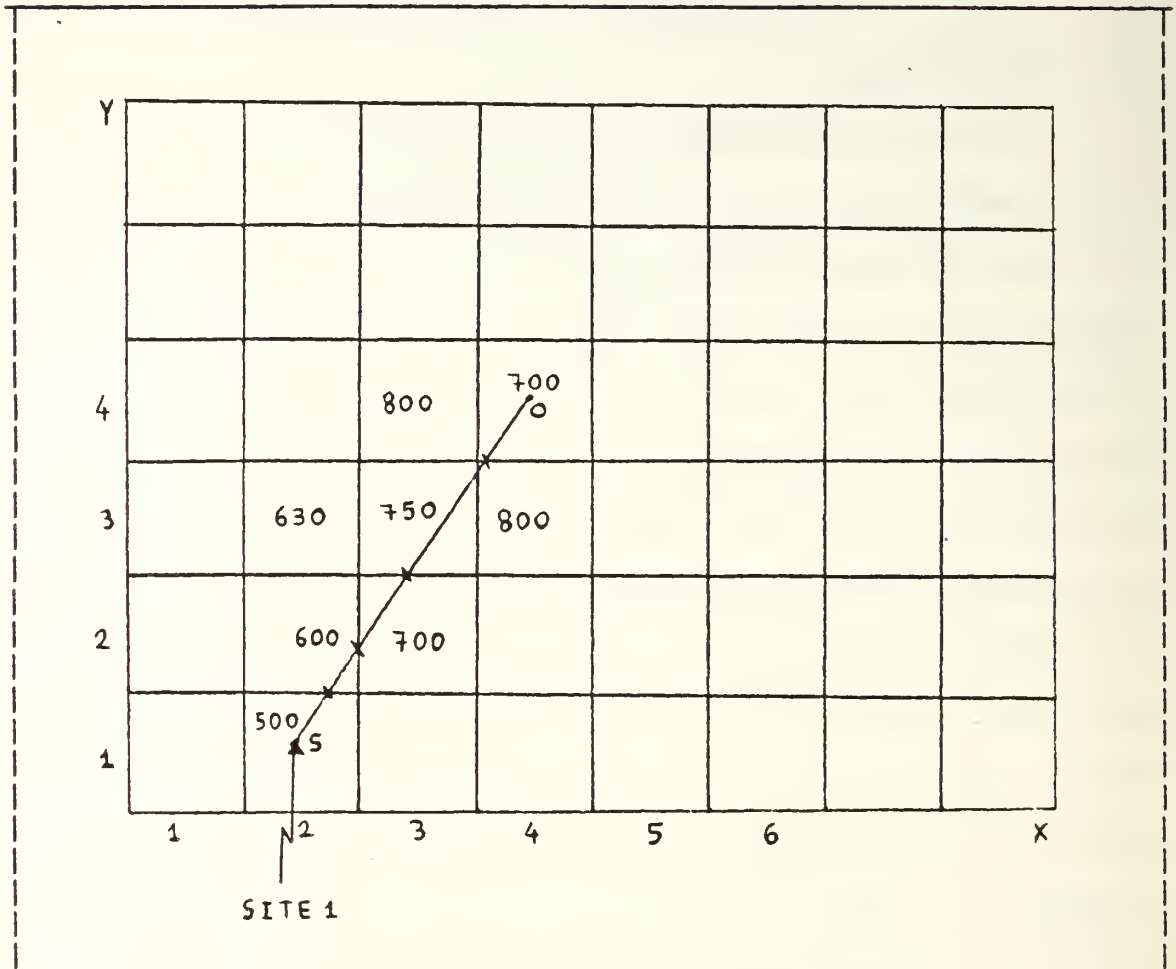


Figure 3.1 Average Altitude Grid

The line-of-sight from site 1 (S) to the center of grid (O) square (4,4) will be analysed.

This line starts from the position of site 1, passes through the grid (2,2), (3,2), (3,3) and ends at point (4,4). A profile of this line-of-sight is shown in Figure 3.2.

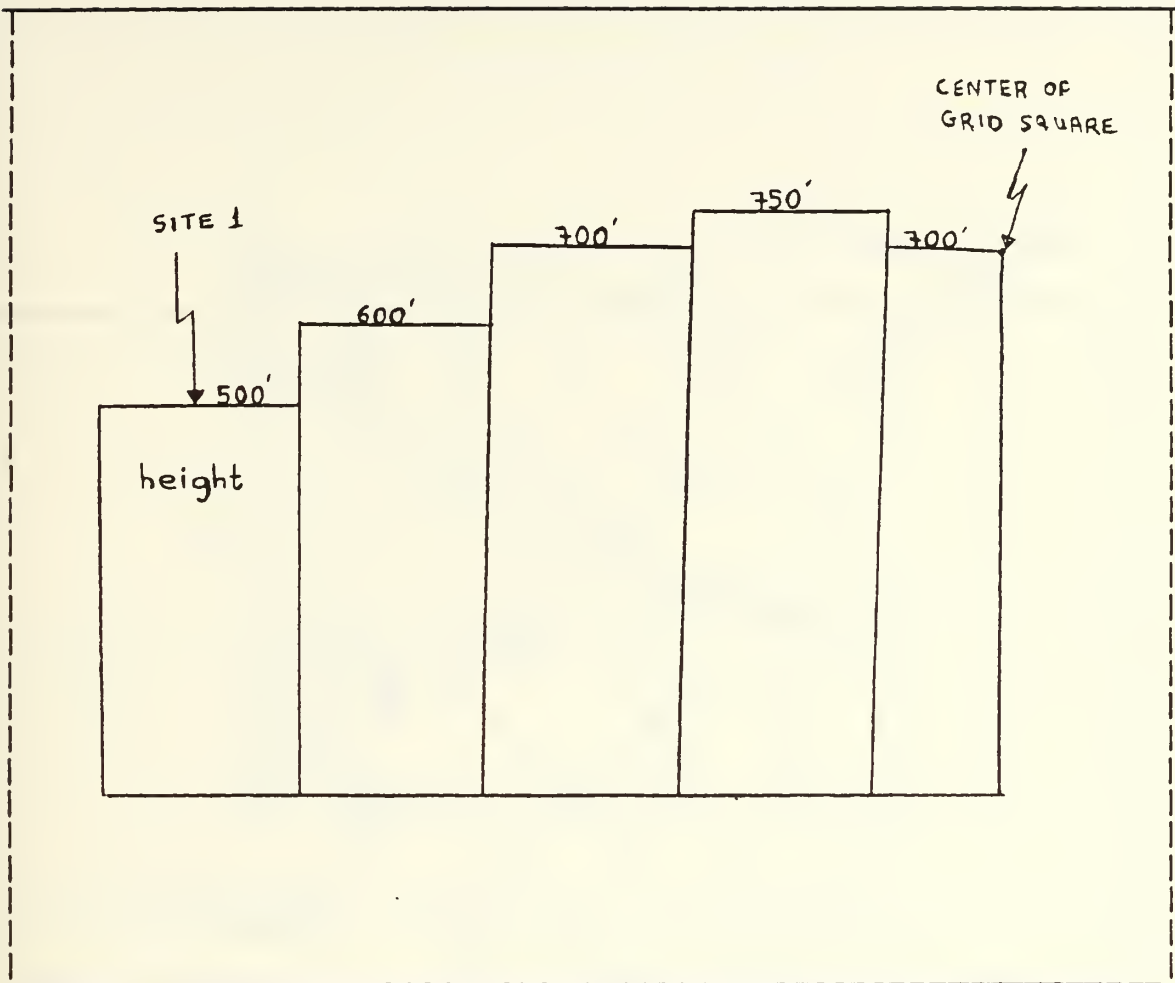


Figure 3.2 Profile of Average Altitude

The profile can be adjusted for earth curvature, as shown in Figure 3.3. Drawing a ray, AB, from site 1 through the edge of the first block illustrates the terrain masking that the first terrain block creates. Based on the first grid square masking, the minimum altitude required for radar line-of-sight to a target flying over grid square (4,4) will be calculated. The geometry of this situation, considering the grid (2,1) position and the grid (4,4) position, is shown in Figure 3.4.

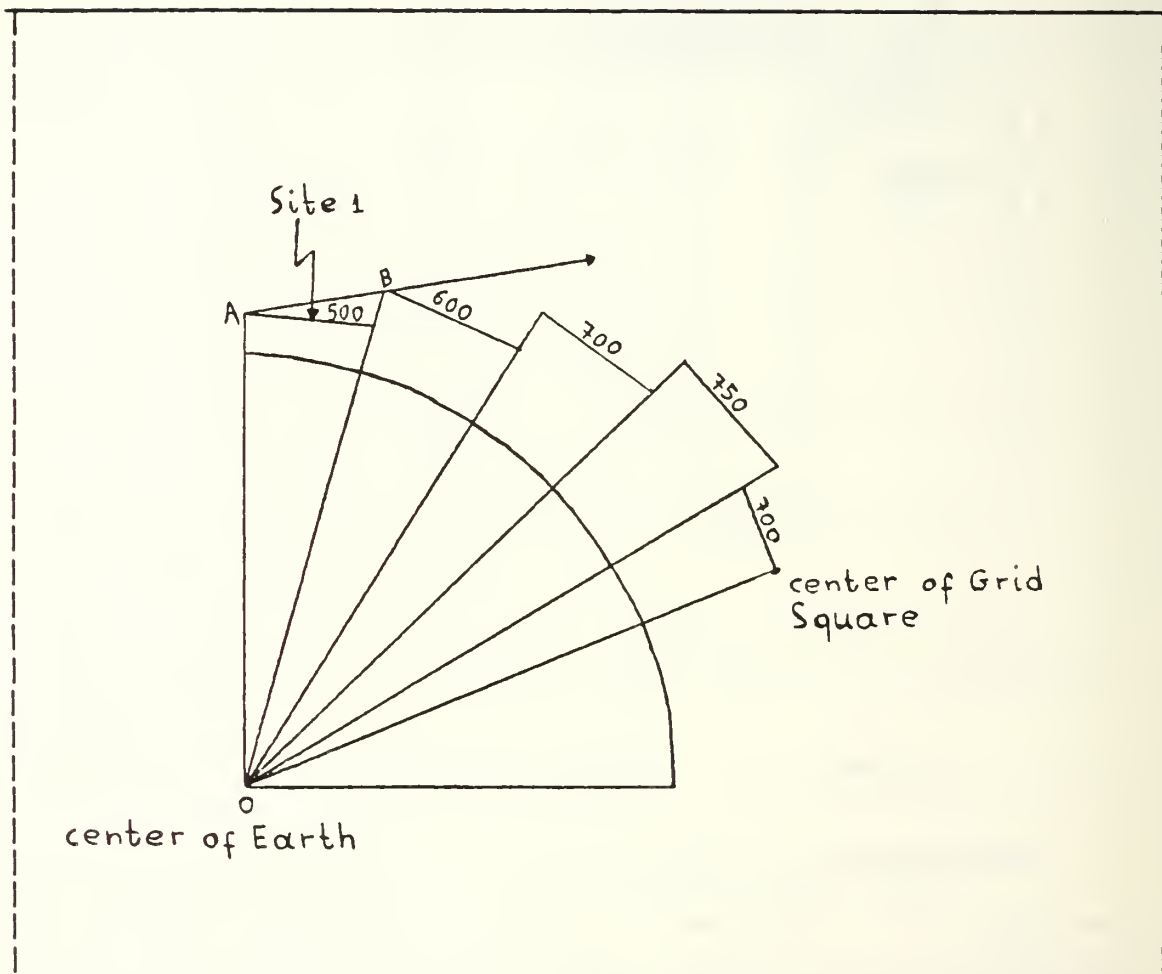


Figure 3.3 Profile of Average Altitude Adjusted
For Earth Curvature

al = Minimum altitude that the radar site 1 can
 "see" due to the grid (2,1)

The length of the arcs AG and AE can be calculated by
 using the formula:

$$\text{ARC(AG)} = ((X2-X1)^2 + (Y2-Y1)^2)^{1/2} \quad (1)$$

$$\text{ARC(AE)} = ((X3-X1)^2 + (Y3-Y1)^2)^{1/2}$$

Where:

X1, X2 = the cartesian coordinates of radar
 site 1.

X1, Y2 = the cartesian coordinates of grid
 (2,1)

X3, Y3 = The cartesian coordinates of grid
 (4,4)

The angles W1 and W2 can be found by using the
 formula:

$$W1 = \frac{\text{ARC(AG)}}{\text{Re}} \quad (\text{in rands}) \quad , \quad W2 = \frac{\text{ARC(AE)}}{\text{Re}} \quad (2)$$

The distances D1 and D2 can be now calculated by
 using the law of cosines:

$$(D1)^2 = (OA)^2 + (OG)^2 - 2(OA)(OG)\cos(W1) \quad (3)$$

Substitution of $OA=OF=R$, $ARC(AG)$, $ARC(AE)$ and $W1$ from formulae (1) and (2) into formula (3) yields:

$$D1 = Re[2 - \cos(\frac{((X2 - X1)^2 + (Y2 - Y1)^2)^{1/2}}{Re})]^{1/2} \quad (4)$$

In the same way the distance $D2$ can be found.

2. Calculation of the altitude $a1$

In order to calculate the altitude $a1$, we also need the distance BC and the angle $W3$. These two can be found as follows:

$$(BC)^2 = (OB)^2 + (OC)^2 - 2(OB)(OC)\cos(W1) \quad (5)$$

From Figure 3.4 we can see that $OB = R+S$ and $OC = R+h$. By using this result and the formula (2) we can rewrite formula (5) as:

$$(BC)^2 = (R+S)^2 + (R+h)^2 - 2(R+S)(R+h)\cos(\frac{ARC(AG)}{Re}) \quad (6)$$

Now, we know the sides OB and BC of the triangle OBC , so we are able to find the angle $W3$ by using the law of cosines and formulae (5) and (6) :

$$W3 = \text{ARC} \left[\frac{(OB)^2 + (BC)^2 - (OC)^2}{2(OB)(BC)} \right] =$$

$$\text{ARC} \left[\frac{(R+S)^2 [1 - (R+H)\cos(W_1)]}{(R+S)^2 + (R+h)^2 - 2[R+S][R+h]\cos(W_1)} \right] \quad (7)$$

We also have:

$$W_4 = - (W_1 + W_2 + W_3) \quad (8)$$

Finally, by using the law of sines we can find the altitude a_1 as follows:

$$\frac{\sin(W_3)}{OD} = \frac{\sin(W_4)}{OB} \implies OD = \frac{\sin(W_3)(OB)}{\sin(W_4)} \implies$$

$$Re + a_1 = \frac{\sin(W_3)(R+S)}{\sin(W_4)} \implies$$

$$a_1 = \frac{\sin(W_3)[R+S]}{\sin(W_4)} - Re \quad (9)$$

Thus, given R , S , h , D_1 and D_2 , the minimum altitude required because of terrain masking by the first block can be calculated.

Formula (9) may give us negative altitudes. This can happen in the case, when the height of the radar site is much higher than the height of the first block.

Negative minimum altitudes mean that the radar site can "see" even below the surface of the earth. It is obvious

that in this case, we have to assign the average height of the target grid (4,4), namely 700 feet (see Figure 3.1).

To summarize, the complete algorithm for calculating the minimum altitude a_1 is:

If a_1 is greater or equal to zero, then store the result.

Otherwise store zero and continue to calculate a new a_1 because of the second block

3. Calculation of the maximum altitude a_1

As one proceeds across grid squares along the line-of-sight path in Figure 3.1, four grid blocks are encountered. Therefore, minimum altitude calculations would be performed four times. These four altitudes, a_1 through a_4 , are shown in Figure 3.5.

The minimum altitude entry, a_{44} for grid square (4,4) in relation to site 1, is:

$a_{44} = \text{maximum}(a_1, a_2, a_3, a_4)$. This procedure must be repeated for every grid square located within the max radar range of site 1. Then, the site 1 minimum altitude grid would be completed.

The program "MINALT" (MINimum ALTitude), described in Appendix B, calculates the minimum altitudes for a given radar site. A small output of this program is shown in Figure 3.6. The upper number of each square represents the average terrain altitude for this grid and the lower number represents the minimum altitude that the radar at site 1, located in grid (3,3), can "see". For example, the minimum

altitude for grid (5,5) is 876 feet instead of 562 feet because of the terrain masking that the grid (4,4) creates.

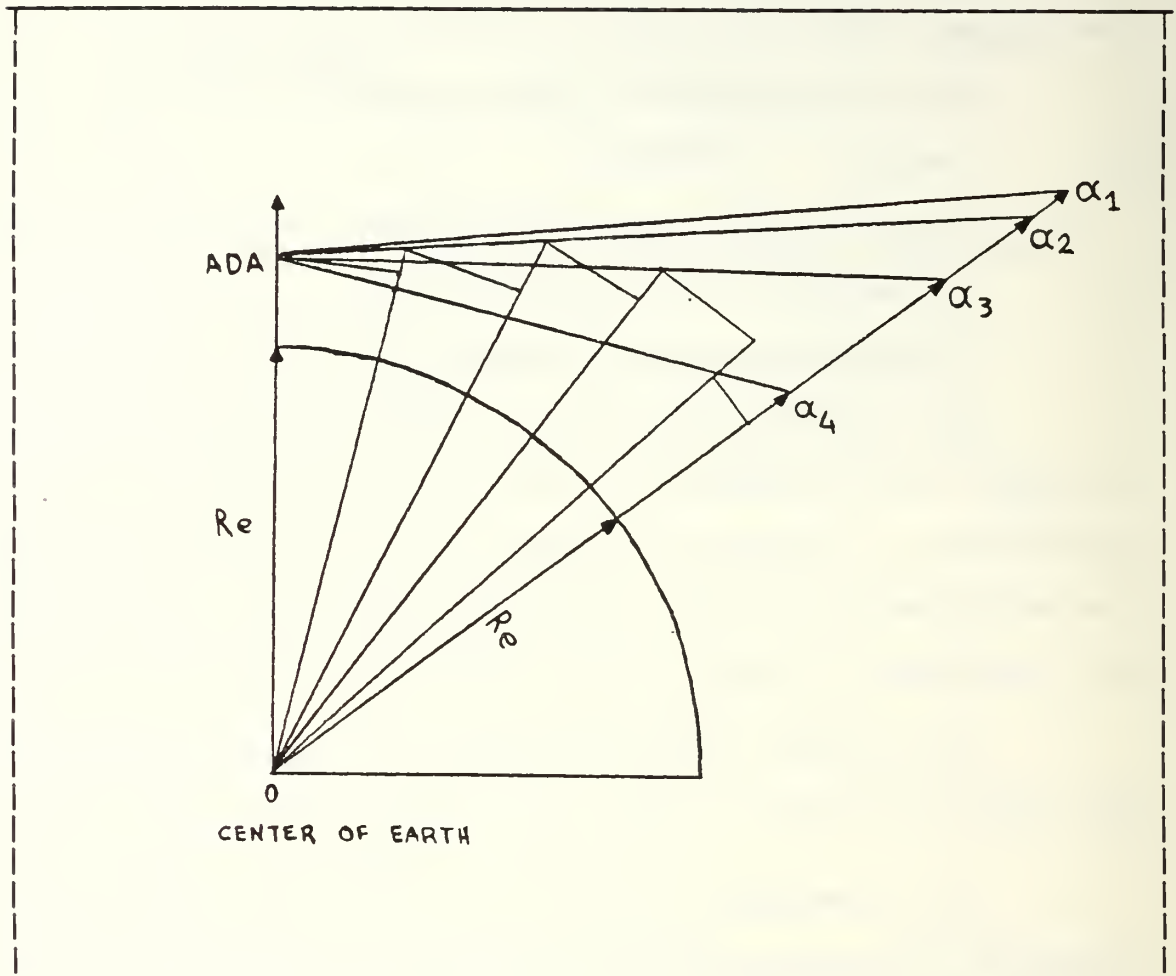


Figure 3.5 Minimum Altitudes along the Line-of-Sight

C. ADVANTAGES AND DISADVANTAGES OF THIS METHOD

1. Advantages

a. The calculation of the minimum altitudes a_i is performed by using precise computations. It is not an approximation.

b. The minimum altitudes have to be calculated once for each radar site. After that, these altitudes can be used for finding the line-of-sight. They also can be used as inputs to other models in a more complex simulation.

7	0 0	0 0	140 140	490 490	787 892	625 1443	1000 1586	1812 4745
6	0 0	0 83	177 177	527 527	787 862	1312 1312	1312 3757	1587 4327
5	0 0	62 359	350 438	550 913	562 876	1425 2899	2075 3418	2275 4016
4	0 23	438 438	821 913	1000 1000	925 2176	737 2652	1637 3203	2262 3823
3	0 0	500 500	RADAR SITE	1625 1625	1620 2063	937 2565	725 3129	1162 3757
2	0 0	125 125	1375 1375	1625 2625	2500 3482	1625 3110	587 3801	337 3823
1	0 0	0 1617	750 1563	2375 3482	2875 4127	2150 5006	1200 6031	412 7163
	1	2	3	4	5	6	7	8

Figure 3.6 Minimum Altitudes for Site 1 (3,3) - Elevation -

2. Disadvantages

In accurate line-of-sight determination, many calculations are necessary. However, if we consider that

these calculations will be done once and can be performed in a pre-processing stage, this algorithm poses no major problems.

IV. LINE-OF-SIGHT AND POSSIBILITY OF DETECTION

A. INTRODUCTION

All radars which operate in high frequencies have some restrictions which must be satisfied so that they will be able to detect a target flying across their area. The two most important restrictions are the existence of line-of-sight and the requirement that the target flies inside the maximum range of radar site.

This chapter will develop a method to find out if there is a line-of-sight for a particular radar site. It will also develop a model to determinate the possibility of detection of the target given that it flies inside the maximum range of the radar site.

B. LINE-OF-SIGHT DETERMINATION

Line-of-sight means that there is nothing between the radar site and target. Line-of-sight may be prohibited for two reasons.

First, terrain, such as hills and mountains, prohibit line of sight. Figure 4.1 below shows this case.

The second reason is the curvature of the earth. If the distance between radar site and target is lengthy then line-of-sight may be restricted due to earth curvature.

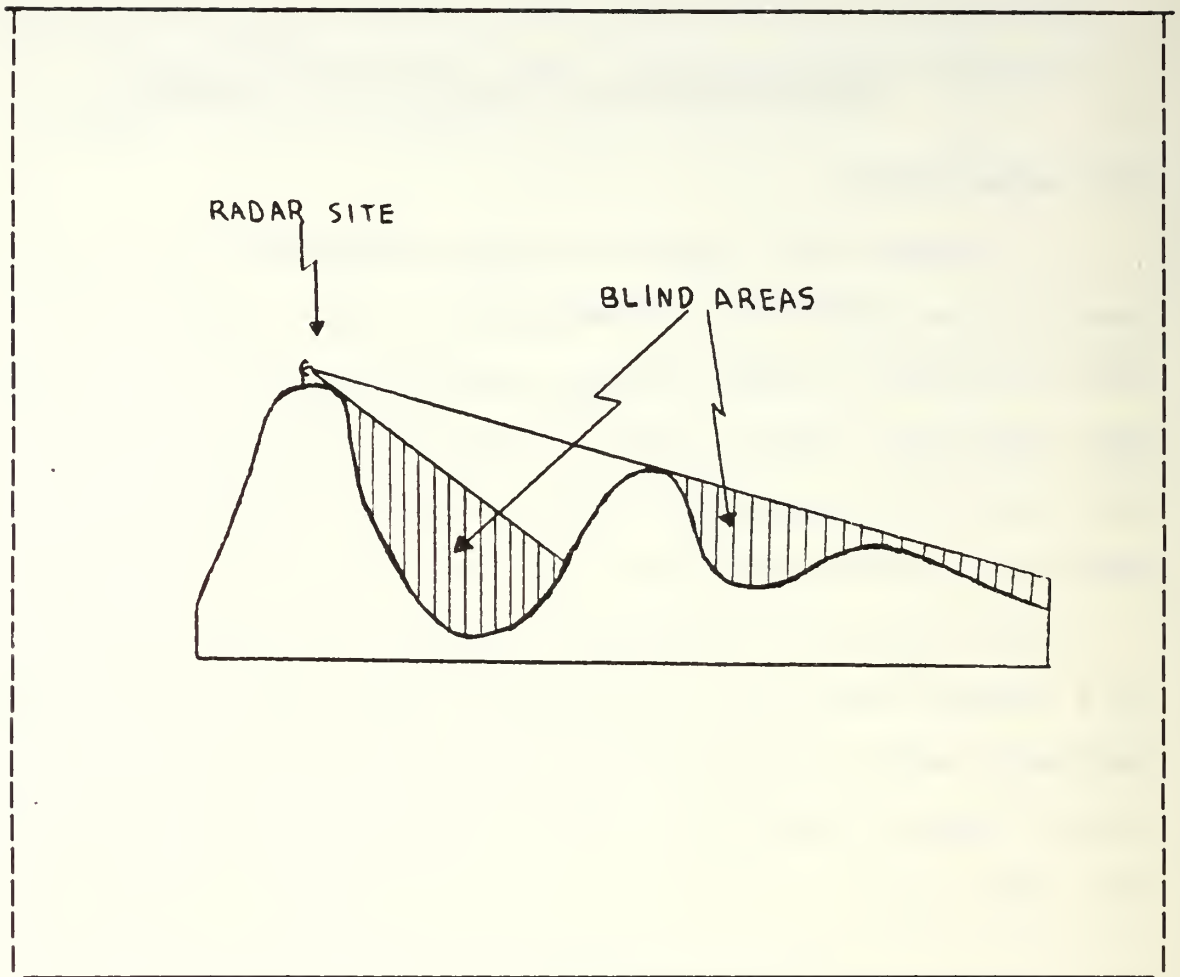


Figure 4.1 Line-of-Sight Restricted by Hill

This case is shown in Figure 4.2. As an example, when the altitude of the radar site is zero and the distance between radar site and target is 50 NM the target must fly approximately 2200 feet above ground in order to be seen by the radar site.

On the other hand, if the altitude of radar site is 1000 feet and the target's altitude is 2000 feet, the distance that the radar site will be able to detect the target is 87 NM.

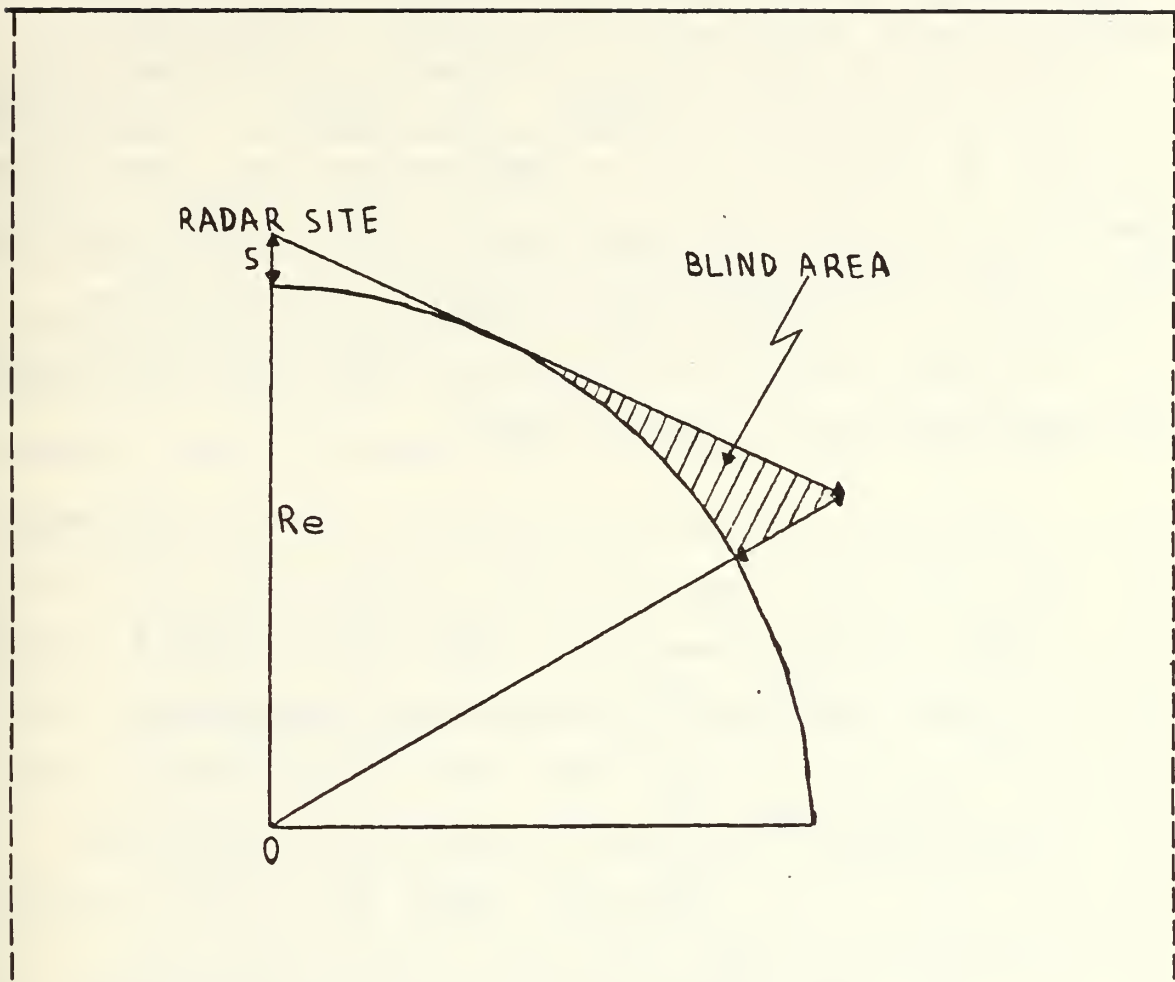


Figure 4.2 Line-of-Sight Restricted by Earth Curvature

In the program "CONTOUR" described in Appendix C, the determination of radar line-of-sight uses the minimum altitude look up table described in Chapter III. Figure 4.3 is the same as the Figure 3.6 in Chapter III. It contains the minimum altitudes that a/c over other grids must fly if radar site 1, located in grid (3,3), is to see a target.

Figures 4.4, 4.5 and 4.6 are outputs of the computer program "CONTOUR". The data used by this program are the data shown in Table 2 and Figure 3.6 in chapter II and III

respectively. Assume that the target flies at 500, 2000 and 6000 feet above the surface of the earth. This means that the target uses terrain masking. For example, if the average altitude of the grid (2,2) is 1000 feet and the target flies 500 feet above this grid, then the altitude of the target is 1500 feet. By comparing this altitude with the minimum altitude that the radar site can see in the grid (2,2) we can determine if there is line-of-sight.

7	0 0	0 0	140 140	490 490	787 892	625 1443	1000 1586	1812 4745
6	0 0	0 83	177 177	527 527	787 862	1312 1312	1312 3757	1587 4327
5	0 0	62 359	350 438	550 913	562 876	1425 2899	2075 3418	2275 4016
4	0 23	438 438	821 813	1000 1000	925 2176	737 2652	1637 3203	2262 3823
3	0 0	500 500	RADAR SITE LOCATION	1625 1625	1620 2063	937 2565	725 3129	1162 3757
2	0 0	125 125	1375 1375	1625 2625	2509 3482	1625 3110	587 3801	337 3823
1	0 0	0 1617	750 1563	2375 3482	2875 4127	2150 5006	1200 6031	412 7163
	1	2	3	4	5	6	7	8

Figure 4.3 Minimum Altitudes

In Figures 4.4, 4.5 and 4.6 we can see how the ability of the radar site increases as the altitude of the target increases. In these Figures there is a flight path which starts from grid (2,1) and ends at grid (11,9). In Figure 4.4, a target which is flying across this flight path, at 500 feet over the ground (using terrain masking), will not be detected by the radar site located at the grid (3,5). However, when the target uses the same path at 2000 feet, above ground level, it may be detected over the grids (3,2), (3,3), (4,3), (5,4), (6,5), (7,6), (8,6) and (8,7) (see Figure 4.5). If the target uses the same path at 6000 feet, above ground level, it will not be seen over the grids (10,3) and (11,3).

This method can be used to create a look up table for each site in the air defense system.

C. DETERMINING THE POSSIBILITY OF DETECTION

In the previous chapter we described the method for determining the existence of line-of-sight from the radar to the target. In this section, we will describe how to determine if there is a possibility of detection of the target by the radar site, given that there is line-of-sight. We use the term possibility of detection, because, even if there is line-of-sight and the target flies inside the maximum range of the radar site, radar may not be able to detect the target. For example, the performance of the radar could be reduced by heavy precipitation. In some cases, the target uses ECM which can degrade radar performance.

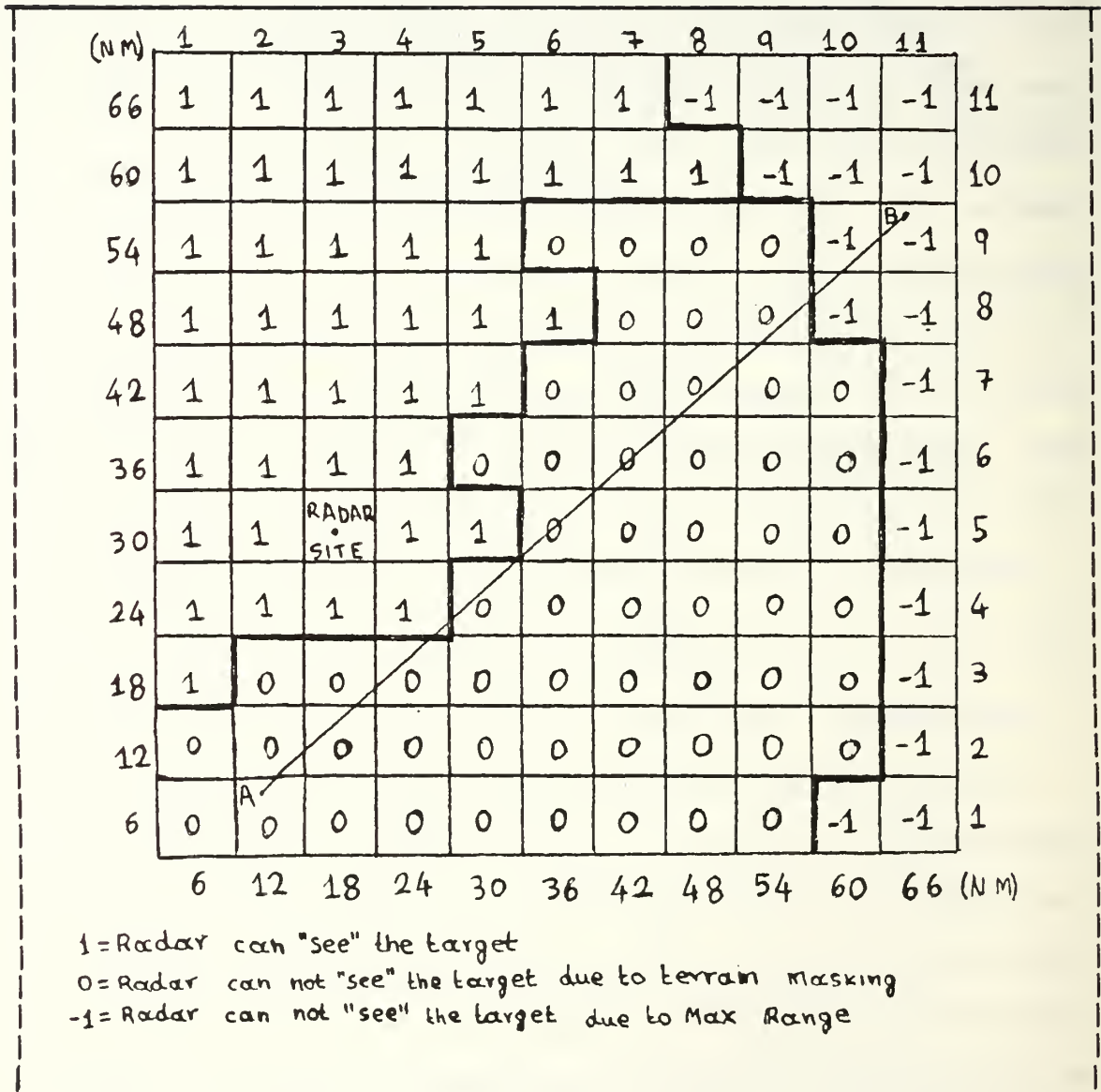


Figure 4.4 Visible Area for Target Flying at 500 Feet

(N.M.)	1	2	3	4	5	6	7	8	9	10	11	
66	1	1	1	1	1	1	1	-1	-1	-1	-1	11
60	1	1	1	1	1	1	1	1	-1	-1	-1	10
54	1	1	1	1	1	1	1	0	0	-1	-1	9
48	1	1	1	1	1	1	0	0	0	-1	-1	8
42	1	1	1	1	1	1	1	1	0	-1	-1	7
36	1	1	1	1	1	1	1	1	0	0	-1	6
30	1	1	RADAR SITE	1	1	1	0	0	0	0	-1	5
24	1	1	1	1	1	1	0	0	0	0	-1	4
18	1	1	1	1	1	0	0	0	0	0	-1	3
12	1	1	1	0	0	0	0	0	0	-1	-1	2
6	0	0	0	0	0	0	0	0	0	-1	-1	1
	6	12	18	24	30	36	42	48	54	60	66	(N.M.)

1 = Radar can "see" the target
 0 = radar can not "see" the target due to terrain masking
 -1 = Radar can not "see" the target due to Max Range

Figure 4.5 Visible Area for Target Flying at 2000 Feet

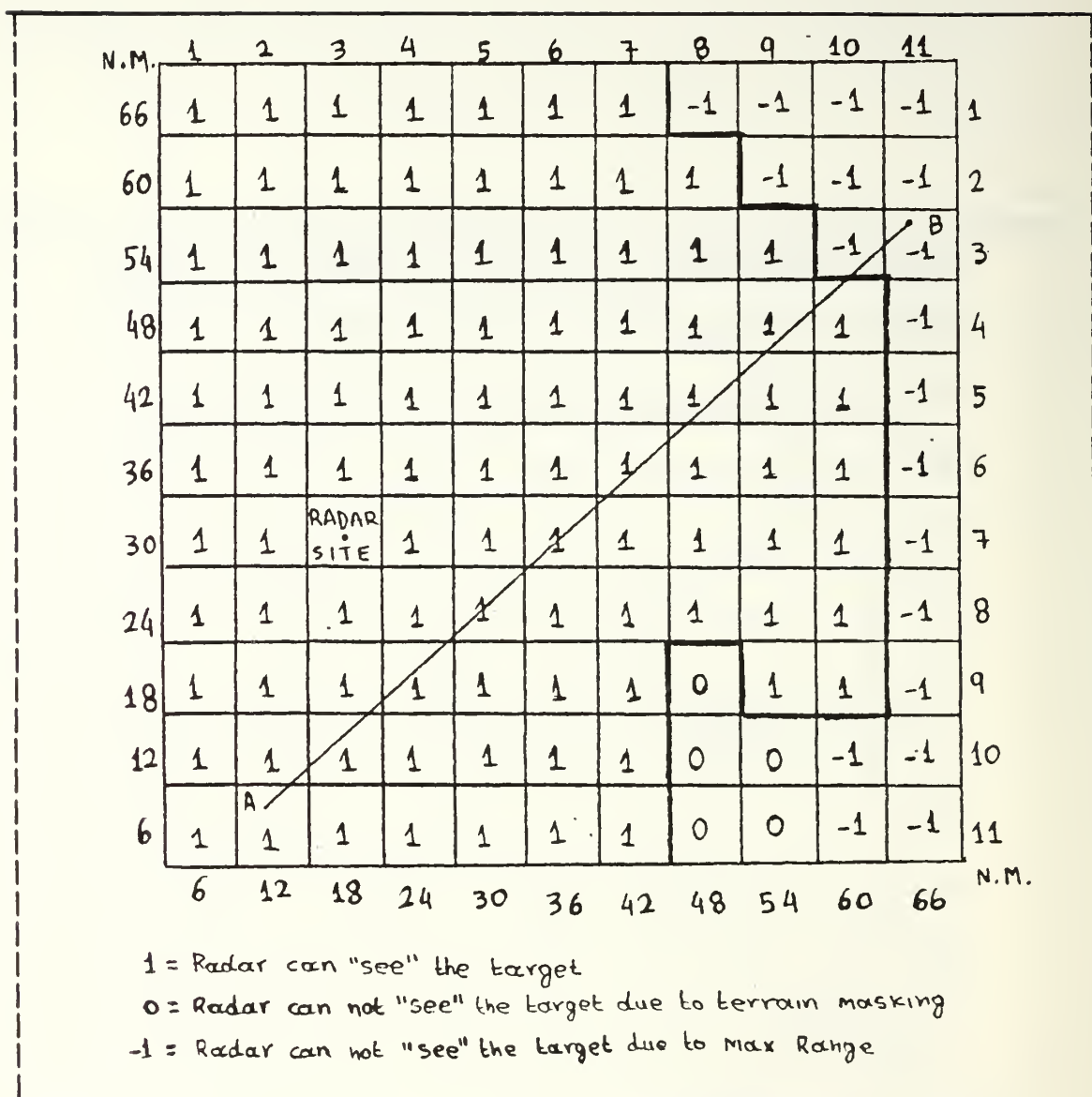


Figure 4.6 Visible Area for Target Flying at 6000 Feet

The procedure for deciding if a site can detect a given target involves the following steps.

1. Using a minimum altitude look up table, determine if there is radar line-of-sight to the target. If line-of-sight does not exist, no detection will occur.

2. If radar line-of-sight exists, calculate the slant range X, from the site to the target. If the slant range is more than the maximum acquisition range R of the radar, no detection will occur.

If the slant range is less than or equal to the maximum acquisition range, a detection is possible.

The calculation of the slant range can be performed as follows: (see Figure 4.7)

Consider a target at time t with the following parameters:

1. $[X_2(t), Y_2(t)]$ is the target grid coordinates at time t
2. $a(t)$ is the target altitude at time t

The lateral range D_1 of the target from the site at time t is:

$$D_1(t) = [(X_1 - X_2(t))^2 + (Y_1 - Y_2(t))^2]^{1/2}$$

Where (X_1, Y_1) are the grid coordinates of the radar site.

The angle W between ray OA and OB is $D_1(t)/R_e$, measured in radians.

The slant range X (AB) can be calculated from the law of cosines:

$$X^2 = (R_e + S)^2 + (R_e + a(t))^2 - 2(R_e + S)(R_e + a(t))\cos\left(\frac{D_1(t)}{R_e}\right)$$

Where S = the altitude of the radar site and R_e = radius of the earth.

If $X^2 > R_e^2$, no radar detection occurs.

If $X^2 < R_e^2$, a detection is possible.

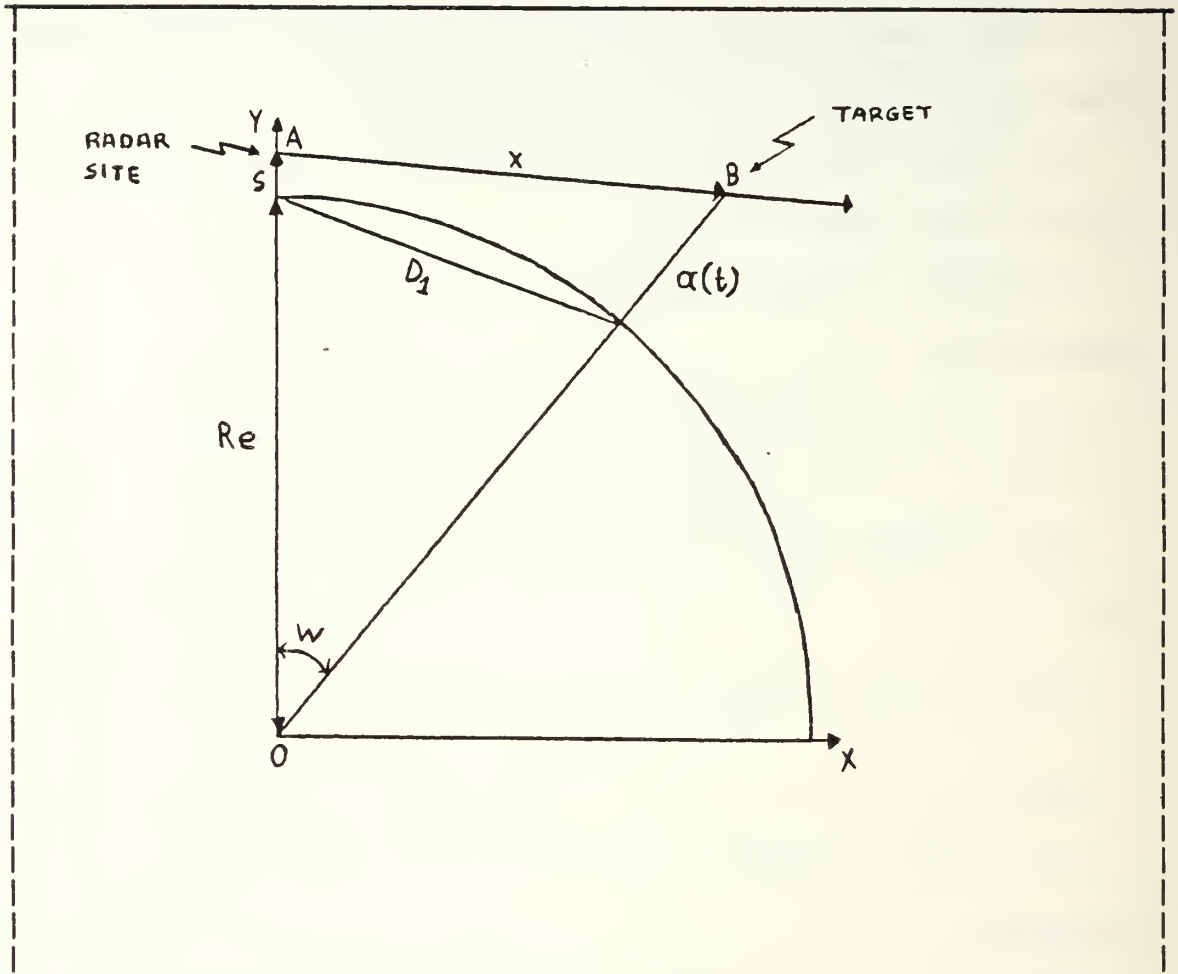


Figure 4.7 Calculation of the Slant Range

The computer program "CONTOUR", explained in Appendix C, calculates the possibility of detection. Figures 4.4, 4.5 and 4.6 are outputs of this program. This output will later be used by the target movement simulation.

D. ADVANTAGES AND DISADVANTAGES

1. Advantages

Determination of radar line-of-sight and possibility of detection for a given radar site and target altitude has to be done only once.

Figures like 4.4, 4.5 and 4.6 can be used by pilots to plan their routes. They can choose a flight altitude to minimize possible detection. This result is extremely useful to the pilots and it may be one of the most important spinoffs of this thesis.

This procedure can be employed in air models as well as other military models which are interested in determining line-of-sight.

2. Disadvantages

Since the model uses the average grid square altitudes given by the computer program "TERRAIN" described in Chapter II it is not an accurate calculation. The determination of line-of-sight is therefore an approximation. However the approximation becomes better and better as the dimensions of the square grid are reduced.

V. A/C MOVEMENT MODEL

A. INTRODUCTION

The tactics used by the aircraft to penetrate the hostile area is one of the most important factors affecting the probability of survival. The flight path chosen across the enemy country depends on the threat. For example, if there are radar sites along the aircraft route, the penetration flight path may consist of small connected paths in order to minimize detection. On the other hand, if there is no radar threat, long straight paths are chosen in order to minimize navigational errors and the time it takes to get to the objective.

B. DESCRIPTION

The simulation of aircraft movement can be performed in several ways. It is possible to design the simulation so that many of the detailed calculations can be accomplished off-line. Like the other models in the previous chapters, the aircraft movement model chosen here is performed totally off-line. Aircraft flights can be planned to take advantage

Aircraft flights can be planned to take advantage of terrain masking. A typical flight path was shown in Figure 5.1.

A flight path can be described as follows:

- . Start time of enemy area penetration.
- . Initial position.

- . Heading of each leg of flight.
- . Distance of each leg of flight.
- . Speed of each leg of flight.
- . Altitude of each leg of flight.

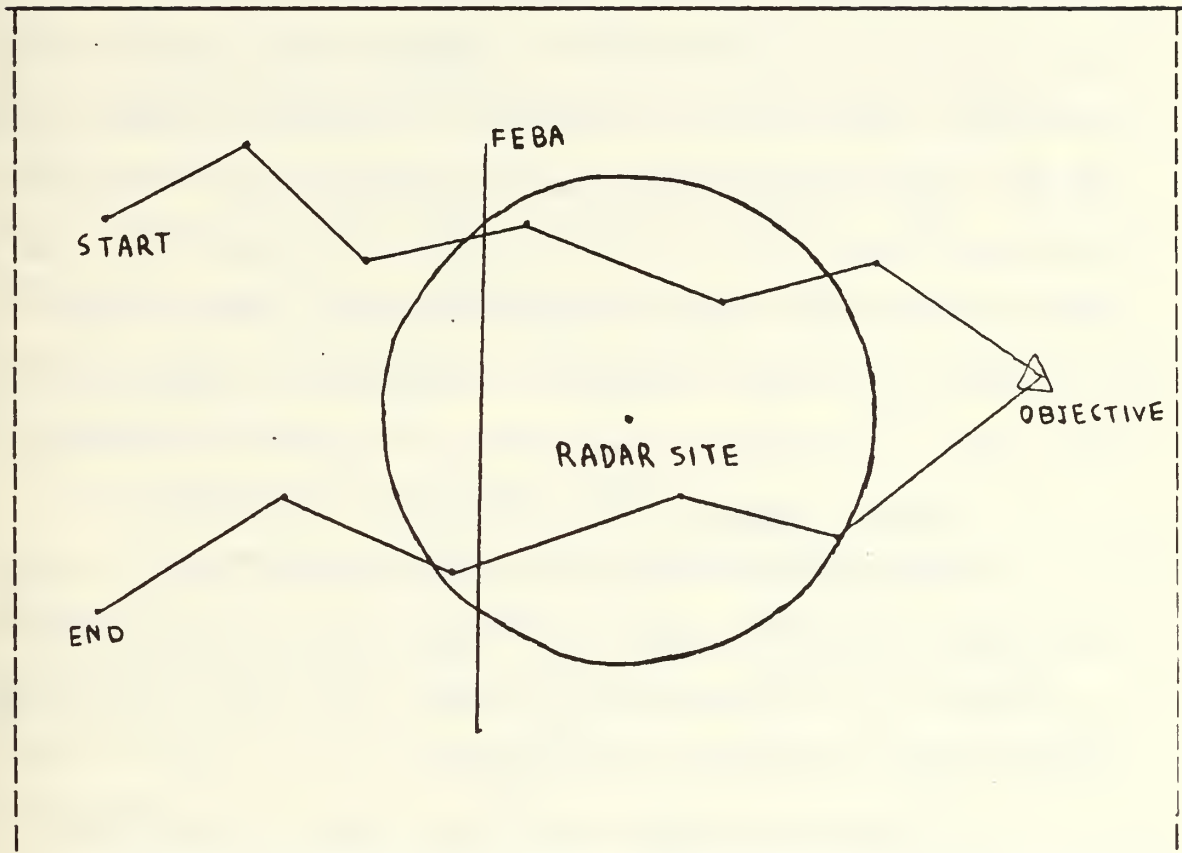


Figure 5.1 A Typical Flight Path

1. Start Time of Enemy Area Penetration

In actual air battles, the time attacking formations choose to enter the hostile area depends on the target and the enemy defense system. For example, if the enemy uses a missile defense system, the attacking aircraft may attack during daylight in order to use terrain masking.

In this model, the start time of the first penetrating attack formation is arbitrary. For example, if the first a/c enters the hostile area at 07:00 o' clock in the morning, then this is considered to be time zero. If a second formation crosses the enemy area at 07:30 then, its time start t is 30 minutes. For computation purposes, the time steps from 07:00 to 07:30 are filled with zeros, so that the air combat model knows that this particular formation enters the battle at 07:30. In Figure 5.2 the fixed time is 07:00 so the start time of the formation is 30 minutes. In the simulation model "MOVEMENT", described in Appendix D, the start time is prompted and it must be entered in minutes.

2. Initial Position

The point that the attacking aircraft use to cross the Forward Edge of Battle Area (FEBA) is very important. If the enemy area is protected by radars, then the initial point must be chosen to minimize detection.

In this air combat model, the FEBA is the line defining the area where attacking aircraft are subject to attrition. This line is chosen by the model designer and it depends on the enemy interception capability. For computation purposes, this line is represented by the Y axis of the Cartesian coordinate system. The X axis is the bottom boundary of the enemy area which is to be simulated. In Figure 5.2 a 48x30 NM enemy area is shown. The (0,0) point is the lower left point of the map. The point that any attacking formation uses to penetrate the hostile area is

described by its relation to $(0,0)$ point of the coordinate system. For example, in Figure 5.2, the start point for the formation is $(0,5)$, which means, that the formation crosses the FEBA 5 NM north of the $(0,0)$ point. In the same fashion, any other point of the formation is described by relating to $(0,0)$ point. For example, the new point $(39,2)$ of the formation in Figure 5.2 means that the formation enters the simulated battle again, after attacking the target, at the point 39 NM east and 2 NM north of the $(0,0)$ point. In the "MOVEMENT" model for each segment in the flight path, the initial point of aircraft penetration is prompted and it must be entered in NM.

3. Heading of the Flight Path

The heading of the flight path depends on the terrain masking that the pilot wishes to use. Usually, when the pilot wants to avoid radar detection, he tries to find routes inside the hostile area that gives him the maximum protection.

For computation purposes, the direction is computed by measuring the angle between Y axis and flight path. In Figure 5.2 the angle between Y axis and the first flight path (OA) is 60 degrees. In the "MOVEMENT" model, for each segment of the flight path, the direction of the a/c movement is prompted and it must be entered in degrees.

Figure 5.2 Flight Path Design

4. Distance

Like the heading, the distance depends on the desired terrain masking. The more terrain masking, the shorter the distance of each flight path. In an extreme case, if the pilot wants to take full advantage of terrain masking, he must follow the terrain form and continually change course. Under these conditions, however, there is a good chance that the pilot will lose orientation. On the other hand, the pilot can neglect terrain masking and fly the entire mission in one straight flight leg. However, his aircraft is much more easily detected and intercepted.

For computation purposes, the distance is computed by measuring the length of each flight path. In Figure 5.2, the distance of the first flight leg is 30 NM. In the "MOVEMENT" model, for each segment in the flight path, the distance is prompted and it must be entered in NM.

5. Speed

The speed that penetrating formations use is a function of many factors. A speed must be chosen to allow for the pilot to maneuver and to avoid interceptors. Fuel consumption and navigational errors must also be considered. Additionally, pilots use different speeds for penetrating the enemy area and for attacking the target. In Figure 5.2 the first two flight legs are flown by using speed equal to 360 Knots and the third one, after the formation has attacked the target, is flown by using speed equal to 420 Knots.

For computation purposes, the speeds are chosen by the scenario designer for each flight leg. In the "MOVEMENT" model the speed for each flight path segment is prompted and it must be entered in Knots.

6. Altitude

Like direction and distance, the altitude depends on the terrain masking. A high speed, low level flight will minimize radar detection and interceptions. On the other hand, low level flights use more fuel which sometimes restricts the aircraft range capability. High altitudes are normally used during the return route in order to save fuel. For computation purposes, the altitudes are chosen by the scenario designer for each flight leg. In reality, the altitude is expected to be the most critical factor, as far as the attrition rate of the a/c is concerned. In Figure 5.2, the altitudes in each square grid are the average terrain altitudes. Also, the three flight legs use a height of 1000, 500 and 10,000 respectively. Finally the total altitude (average grid altitude + altitude of a/c above the terrain) is shown inside the parenthesis for each flight path and for each square grid. This total altitude will be compared in the next chapter with the smallest altitude for each site (computed in Chapter 4) to determine the capability of the radar sites to detect the attacking aircraft.

In the "MOVEMENT" model the altitude is prompted and it must be entered in feet above the terrain.

The a/c movement model is supported by the computer program "MOVEMENT" described in Appendix D. It uses inputs from other models and its output will be used for "FDETECT" and "PRIORITY" sub programs described in later chapters. The data necessary to run the "MOVEMENT" program are shown in Figure 5.2 above. In Table 3, an output of this program is shown. The first row is the time step, the second and third rows are the position of the a/c (X/Y), the fourth row is the altitude over each position. The fifth row is the direction of the flight legs.

TABLE 3
OUTPUT OF "MOVEMENT" PROGRAM

TIME STEPS:	1	2	3	4	.	.	.	N
X:	1	2	3	4	.	.	.	12
Y:	6	7	8	9	.	.	.	16
ALTITUDES:	1000	1125	2375	2875	.	.	.	10000
COURSES:	60	60	135	135	.	.	.	300

C. ADVANTAGES AND DISADVANTAGES OF THE A/C MOVEMENT MODEL

1. Advantages

a. The calculation of the a/c position (X,Y) is accurate (not an approximation).

b. The calculation for each target route has to be done only once and can be done off-line.

c. Since the movement model is independent of the air combat model, it can be used for other air models and simulations.

2. Disadvantages

a. The calculation of the altitude of each aircraft over its position is done by summing the average altitude of the terrain and the altitude of the a/c above the terrain. Since, the average altitudes are an approximation, then the altitude determination of the of the attacking aircraft are, similarly, an approximation.

VI. TARGET DETECTION, INTERCEPTION AND PRIORITY MODELS

In Chapter 4, the minimum altitude that a radar site can detect a target was calculated and in Chapter 5 the flight data (position, altitude, course, etc) were generated for each time step of the simulation. In this chapter, the analysis of the air model will be continued by combining Chapters 4 and 5 and by finding the points that a particular radar site can detect a specified target given by the airmodel simulation scenario. Furthermore, this Chapter will describe the interception model and target priority model which will help the radar site commander to determine missile firing capability against the target.

A. TARGET DETECTION MODEL

The purpose of the target detection model is to determine if there is line-of-sight between a particular radar site and a target and if it is within the radar site's maximum range. For this purpose, the target detection model combines the data given by the "MINIMUM ALTITUDE" model and the data given by the "A/C MOVEMENT" model. The "MINIMUM ALTITUDE" model, as described in Chapter 4, gives the minimum altitudes that a radar site can detect a target over its area. The "A/C MOVEMENT" model as described in chapter 5, gives the flight data of a target (a/c position, altitude, course, speed) flying across the enemy country.

The algorithm the target detection model uses the following steps:

1. It takes the position of the radar site and the position of a/c in time step I .
2. It checks to see if the distance between the radar site and the target is less than the maximum range of the radar site.
3. If no, set $I = I+1$ and go to step 1.
4. If yes, it compares the minimum altitude of the radar site with the minimum altitude of AC in grid square for detection by radar site 1. If the first altitude is smaller than the second, then a detection is possible. Set $I = I+1$ and go to step 1. If the first altitude is greater than the second one, no detection is possible. Set $I = I+1$ and go to step 1.

In Figure 6.1, the minimum altitudes of the radar site 1 (in parenthesis), the route and the altitudes of a/c are shown. By applying the above algorithm, a possible detection occurs in grid squares (1,7), (2,7), (2,6), (3,6), (3,5), (4,5) and (6,4). On the other hand, there is no detection in grid squares (1,8), (5,5), (6,5), (7,4) and (8,4) because the radar site can not see the target and in grid squares (8,5), (9,5) and (9,6) because the target is out of the maximum range of the radar site.

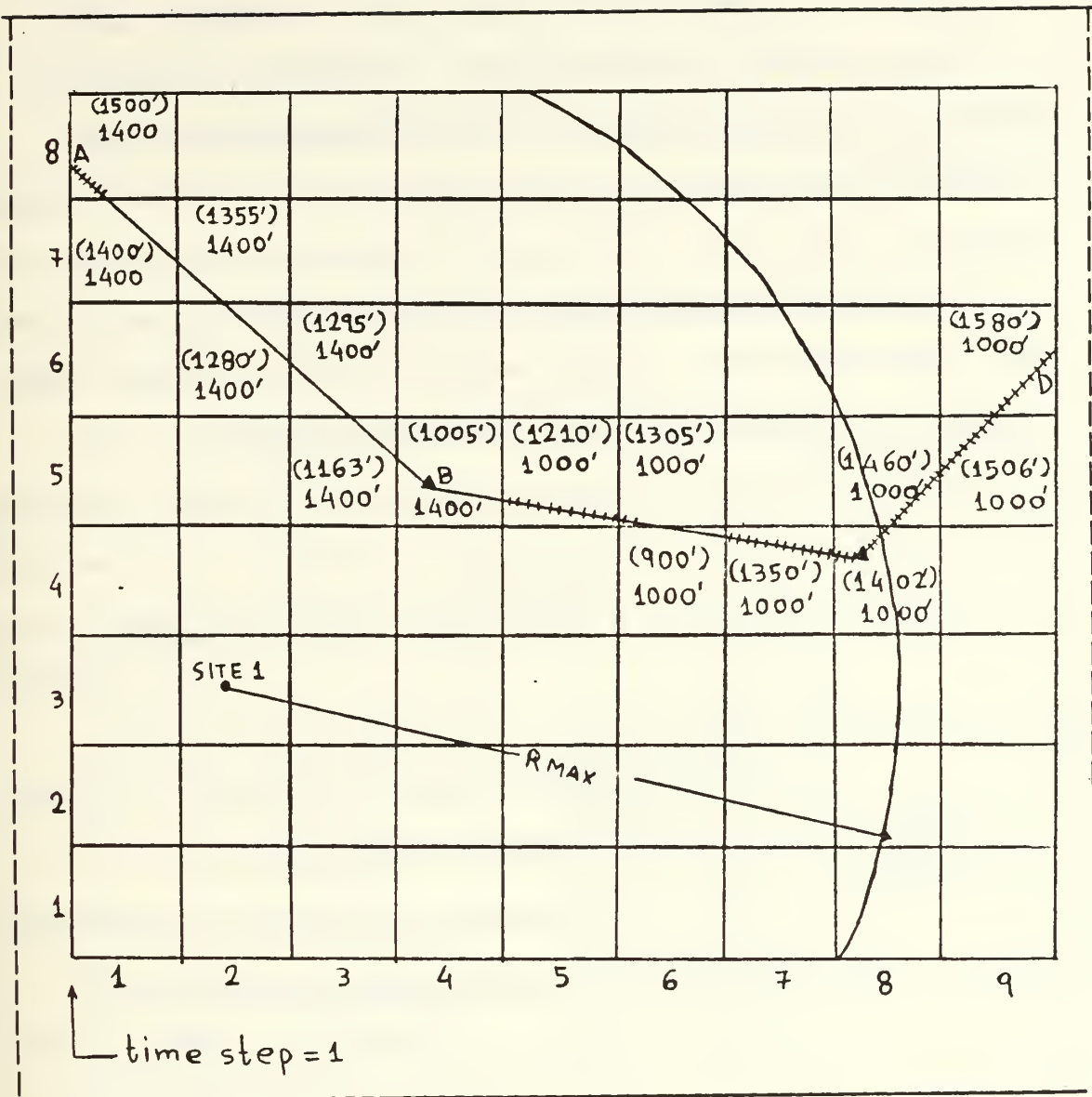


Figure 6.1 Radar Site-Target Flight Route Relation

In this way, the detection state vector is defined for each time step t and it has the following form:

$$D(t) = d_1(t) , d_2(t) , d_3(t) , \dots , d_n(t)$$

Where n = number of targets in the scenario.

$d_i(t) = 0$, when the site cannot detect target i .

$d_i(t) = 1$, when the site can detect target i .

The outcomes 1 or 0 are only a function of detection geometry and depend only on the maximum range and the minimum altitude of the radar site and the altitude of the target.

All the detection vectors form the detection matrices. Each radar site has its own detection matrix for all the targets. In Figure 6.2 such a matrix is shown:

		TARGETS				
		1	2	3	...	N
K TIME STEPS ↓	1	0	1	1		
	2	0	1	1		
	3	1	0	1		
		
		
		
	k	1	0	0		

Figure 6.2 A Detection State Matrix for One Site

For example, the detection matrix for radar site 1, in Figure 6.1 for target 1, for time step 1 to 9 is (in row form to save space):

Time step: 1 2 3 4 5 6 7 8 9

Detection (Y/N): 0 1 1 1 0 0 0 0 0

During the simulation at time step k , if the air model needs to find if the radar site 1 can detect the target 1, the only thing to be done is to check the element $(k,1)$ in the detection state matrix of radar site one, to see if the value is 0 or 1.

The target detection model is supported by the computer program "FDETECT" (File DETECT) described in Appendix E. The purpose of the computer program is to construct the detection state matrix for each Radar site by prompting the following inputs:

a. The minimum altitudes of the radar site given by the "MINALT" program, described in Appendix C.

b. The flight data of the targets given by the program "MOVEMENT" described in Appendix D.

This computer program can be run for any radar site and for any number of targets.

B. TARGET INTERCEPTION MODEL

The next step, after the radar site has detected the target, is to start the procedure of intercepting it. In real war, the determination of whether the missile site can intercept the target or not is given automatically by the radar computer which solves the geometry of the interception considering all the needed parameters. In simulation, a program is required to solve the geometry of the interception. Unfortunately, different kinds of

radar-missile sites use different methods of interception geometry. In Figure 6.3, two different methods are shown: The target following method and the interception point prediction.

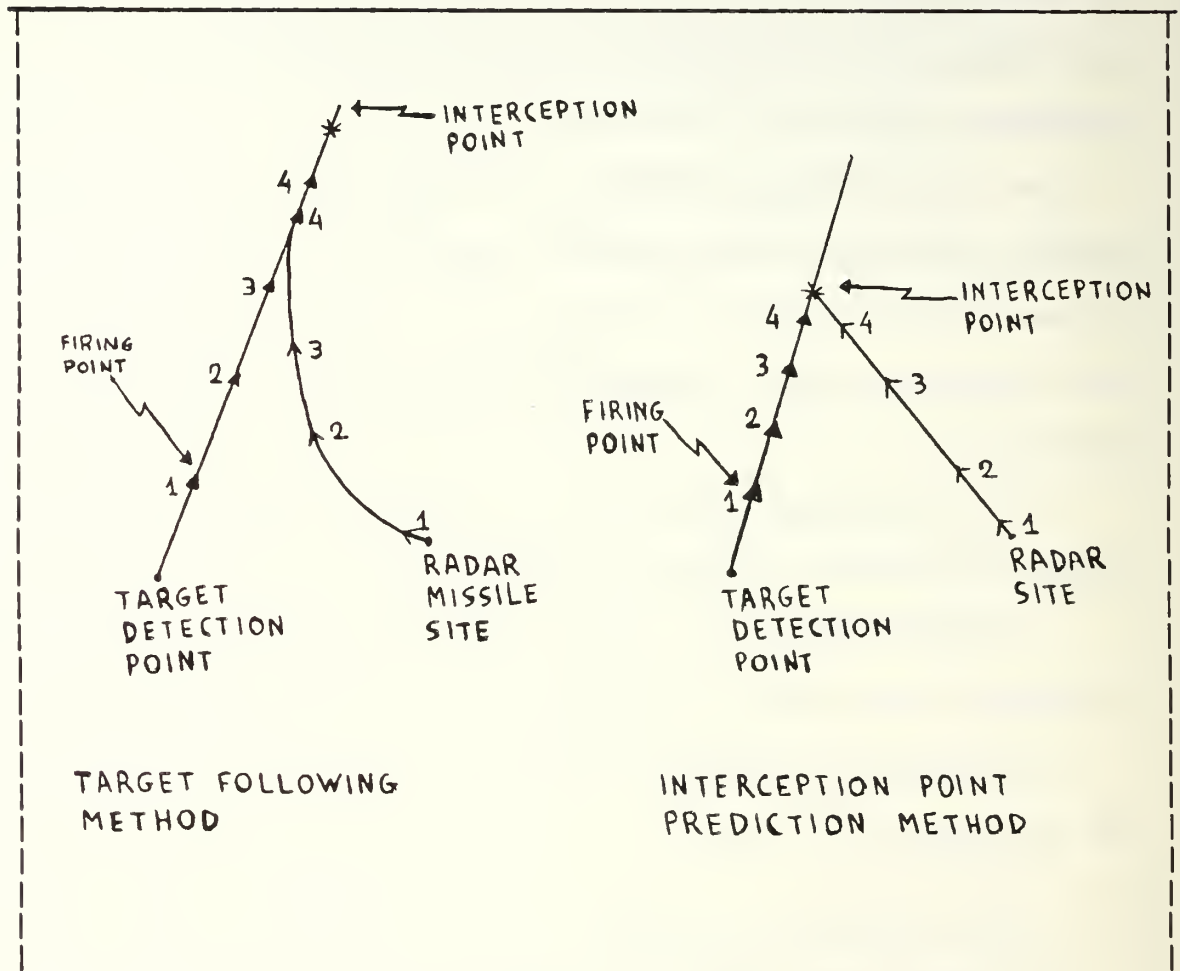


Figure 6.3 Two Methods of Interception Geometry

In first method, the firing missile follows the target until it reaches and kills it. This method is used by old radar missile systems or by missiles which use infrared radiation guidance system. The second method is used by the most modern radar missile systems and it is very

efficient because it minimizes the interception time. In this method the missile is guided to the point that the radar computer has calculated, so that the collision between target and missile will take place. The method is simulated in this air model and it is described here.

To predict the point at which a launched missile and the target will collide is not difficult. This point depends on the distance (D) between target and radar-missile site, on the angle (W) between flight path and radar-missile site and on the speeds of the target and the missile.

In Figure 6.4 the analyzed geometry of the interception point prediction method is shown:

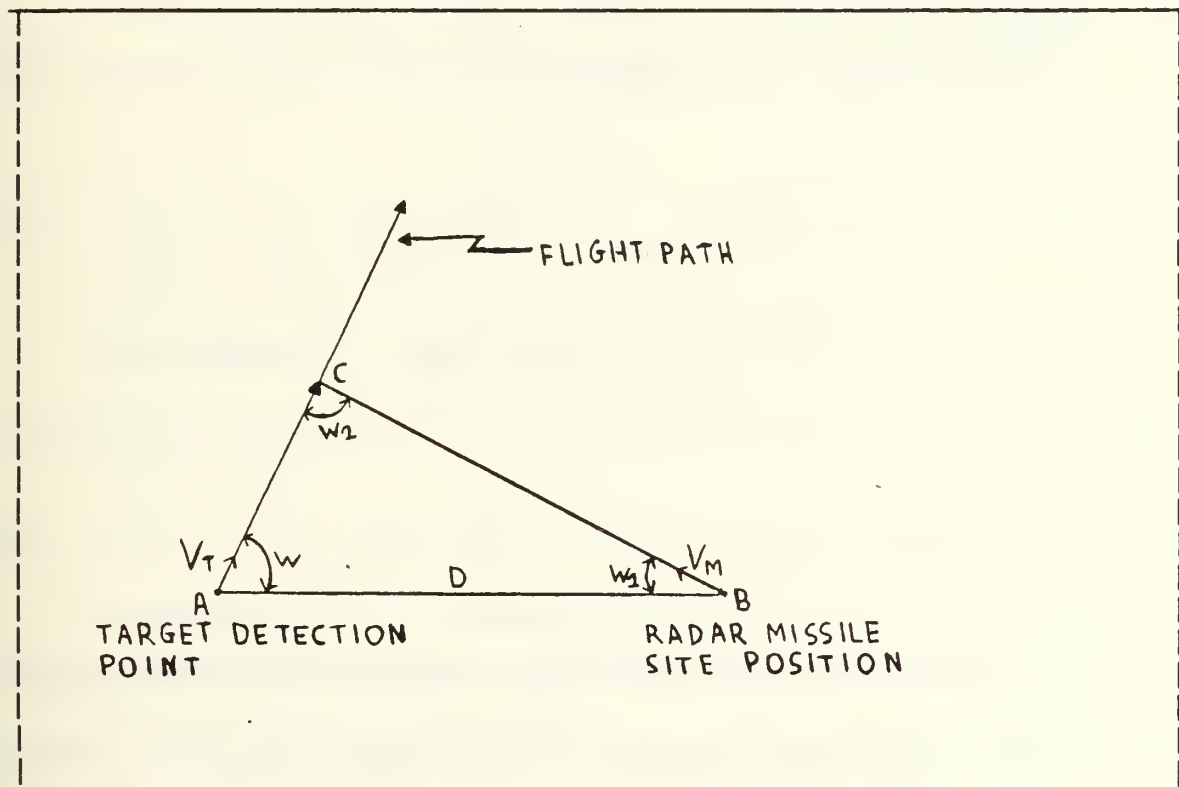


Figure 6.4 Interception Geometry

The calculation of the collision point is described as follows:

Let

W = The angle between flight path of the target AC and the radar - missile site position (X,Y).

D = Distance between the position of the target at the time t and the missile site position.

VT = The speed of the target (KNOTS/h).

VM = The speed of the missile (KNOTS/h).

T = The time the interception takes.

The interception point can be computed if the distance AC is found. To do that, the law of SINES is used:

$$\frac{\sin(W)}{BC} = \frac{\sin(W_1)}{AC} \implies \frac{\sin(W)}{\sin(W_1)} = \frac{BC}{AC} \quad (1)$$

$$BC = VM * T \quad \text{and} \quad AC = VT * T \quad (2)$$

$$\text{From (1) and (2)} \implies \frac{\sin(W)}{\sin(W_1)} = \frac{VM * T}{VT * T} \implies \sin(W_1) =$$

$$\frac{VT}{VM} * \sin(W) \implies W_1 = \arcsin \left[\frac{VT}{VM} \sin(W) \right] \quad (3)$$

The three angles of one triangle sum to 180 degrees, i.e.

$$W + W_1 + W_2 = 180 \text{ degrees} \implies W_2 = 180 - W - W_1 \quad (4)$$

and by substituting the equation (3) into (4) yields:

$$W2 = 180 - W - \arcsin \left[\frac{VT}{VM} \sin W \right] \quad (5)$$

By using again the law of SINES, the distance AC can be found:

$$\frac{\sin(W1)}{AC} = \frac{\sin(W2)}{AB} \implies AC = \frac{AB * \sin(W1)}{\sin(W2)} = \frac{D * \sin(W1)}{\sin(W2)} \quad (6)$$

Finally by comparing the equations (3), (5) and (6) the distance AC is calculated:

$$AC = \frac{VM}{VT} * \frac{D * \sin(W)}{\sin \left[180 - W - \arcsin \left(\frac{VT}{VM} * \sin(W) \right) \right]} \quad (7)$$

The time, that the interception takes, can be calculated by dividing the distance AC by the speed of target VT:

$$T = \frac{D}{VM} * \frac{\sin(W)}{\sin \left[180 - W - \arcsin \left(\frac{VT}{VM} * \sin(W) \right) \right]} \quad (8)$$

The distance BC, the distance the missile travels, is calculated by multiplying the missile speed VM by the time T.

$$BC = T * VM \quad (9)$$

In summary, if the parameters D, W, VT and VM are known, we can find the distances that the target and the missiles travel until the collision occurs and the time at which the interception takes.

It is obvious that an interception is not always possible for the following reasons:

When the distance that the missile has to travel is greater than its maximum flight range.

When the angle W is greater or equal to 90 degrees and the VM is less or equal to VT . In this case the missile will never catch the target.

The Target Interception Model is supported by the computer work space "INTERCEPT", described in Appendix E, whose purpose is to calculate, for a given radar missile site and targets, the intercept state vector. For each time step t , the intercept state vector has the following form:

$$I(t) = (i_1(t), i_2(t), i_3(t), \dots, i_N(t)) \quad \text{where:}$$

N = the number of targets generated in the entire simulation.

$I_j(t) = 0$, implies that a missile fired at target j during this time step will have a predicted intercept point beyond the range capability of the missile system.

$I_j(t) = 1$, implies that a missile fired at target j during the time step will have a predicted intercept point within the capability of the missile system for one of the reasons listed above.

All the intercept state vectors form the intercept state matrix, whose form is shown in Figure 6.5. The interception

state matrix and the time that the possible interceptions require will be used later by the air model to determine whether or not an interception is successful. It will also be used to schedule the interception as future events.

		TGT1		TGT2		...		TGTN	
		RESULT	TIME	RESULT	TIME			RESULT	TIME
TIME STEPS ↓	1	1	10	0	0				
	2	0	0	1	15				
	3	1	9	1	14				
				
				
				
	M	1	12	0	0				

Figure 6.5 An Interception State Matrix for One Site

C. TARGET PRIORITY MODEL

Modern radar sites can track and fire on more than one target and almost all radar sites (old and modern) can detect more than one target simultaneously. In such cases, each radar site has to know the priority of target engagement.

To simulate the priority of the target, either simple or complex techniques can be used. In this air model, the following technique is employed. The priority of each target

is determined from its flight route for each time step. Analytically, the target priority model uses the following rules:

Rule 1: Two or more attacking targets

When two or more targets are penetrating the defended area at the same time, the aircraft which heads more directly towards the defender's critical assets, has highest priority. Figure 6.8 shows this case. The difference between the critical heading of the course and the heading of target 1 is smaller than the difference between heading critical course and heading course of target 2. Therefore target 1 has priority one and target 2 has priority two.

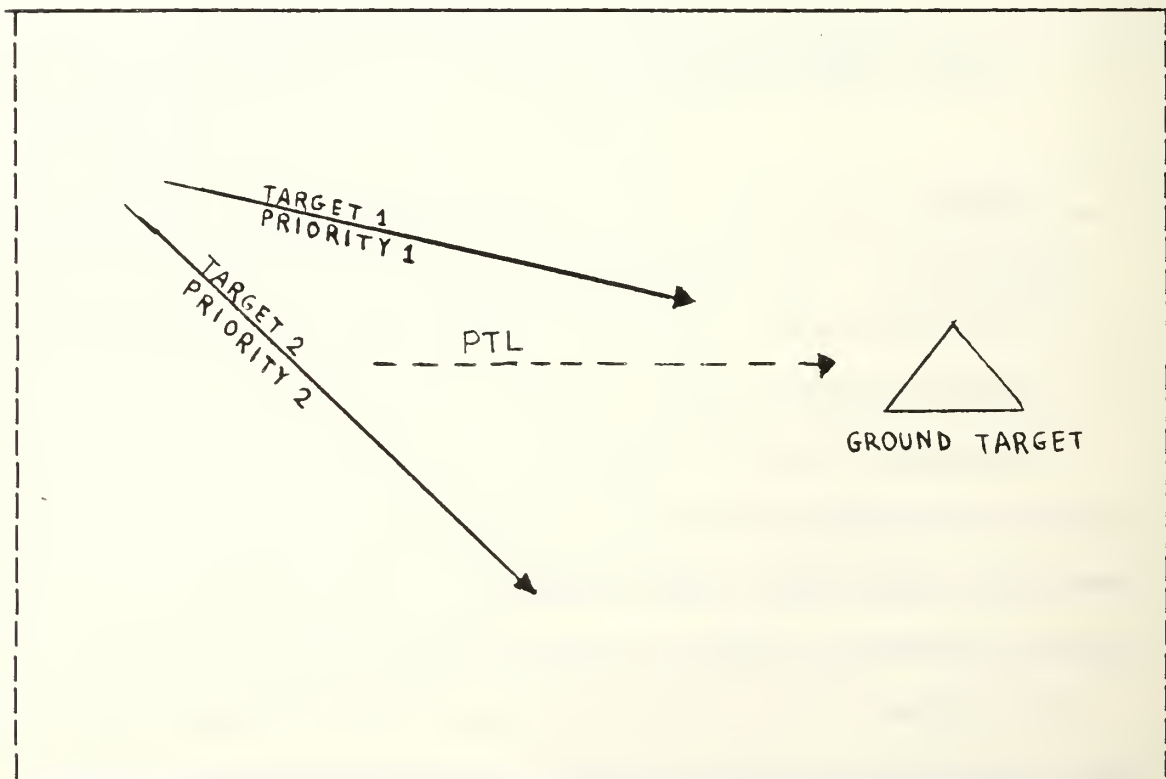


Figure 6.6 Two Attacking Targets

Rule 2: Attacking and Returning Aircraft

When the priority model simulates two targets one of which is attacking and the other is returning to its own territory, it assigns a higher priority to the first target than to the second. The reason is that the attacking targets are more dangerous than the returning ones. This case is shown in Figure 6.7. Target 1 has higher priority than target 2.

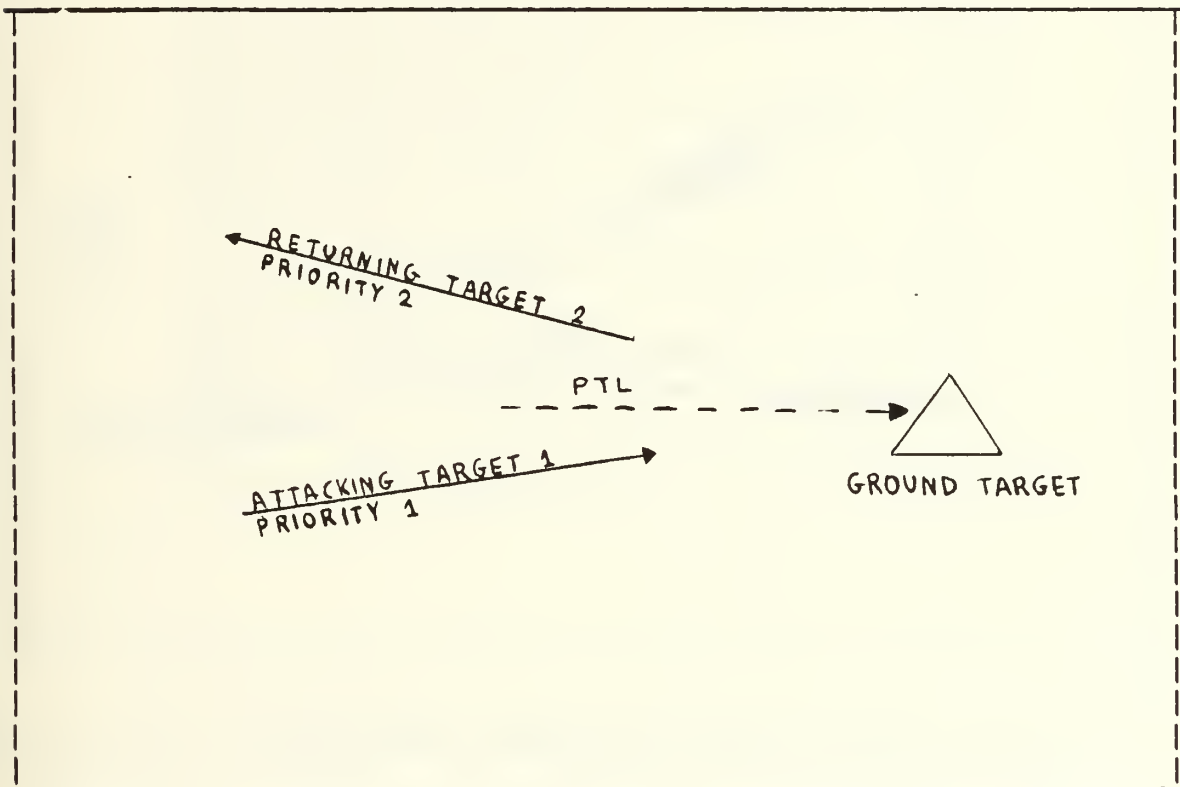


Figure 6.7 Attacking and Returning Targets

Rule 3: Two or more Returning targets

In the case of two or more returning targets, the target which heads more directly away from the defender's critical assets has the higher priority. The reason is that

the interceptor missile has less time to intercept the first target than the second one. Figure 6.8 shows this case. The difference between the heading of the critical course and the heading of target 1 is smaller than the difference between the heading of the critical course and the heading of target 2. Therefore, target 1 has priority one and target 2 has priority two.

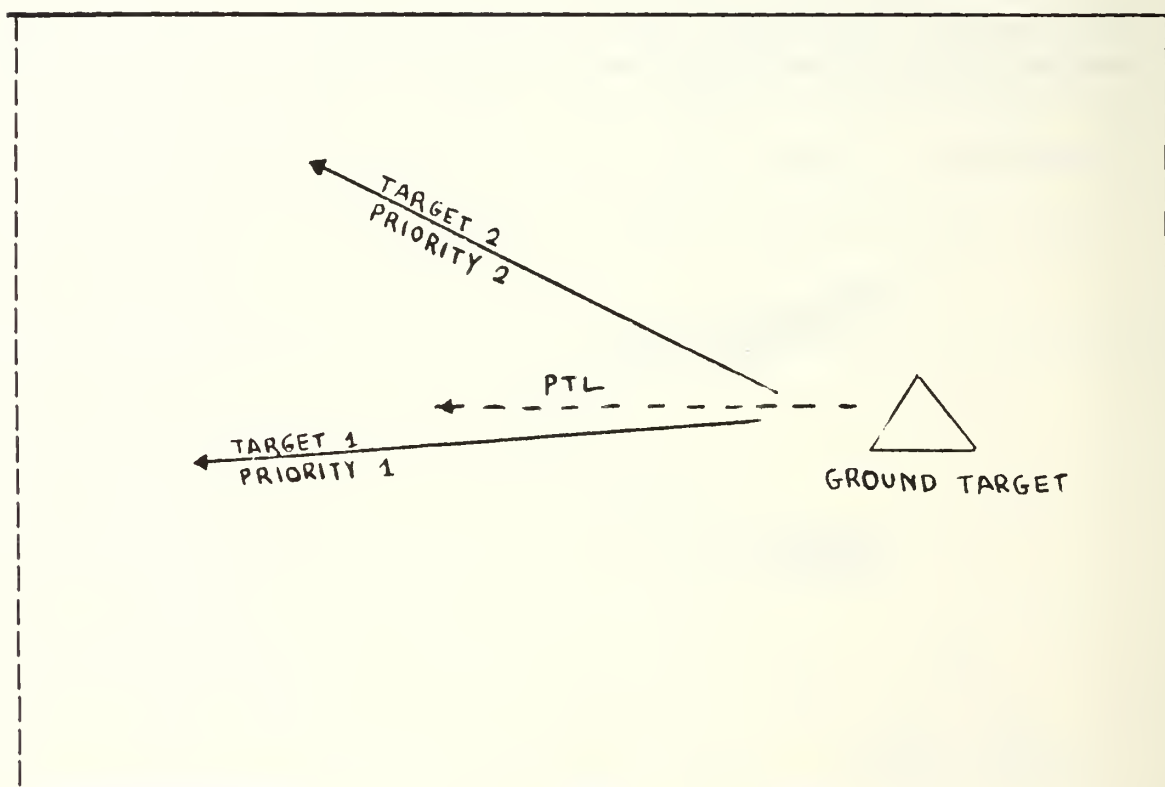


Figure 6.8 Two Returning Targets

All three rules define the prioritization state vector which has the following form:

$$P(t) = P_1(t), P_2(t), P_3(t), \dots, P_N(t)$$

where

N = Number of targets in the entire simulation

$P_i(t) = 1$ when the target i has priority 1 etc.

All the priority state vectors form the priority state matrix whose form, for 5 targets, is shown in Figure 6.9. For example in time step 1, in Figure 6.9, target 4 has priority one, target 2 has priority two, target 1 has priority three and so on.

		TARGET					
		1	2	3	4	5	N
TIME STEP	1	3	2	4	1	5	N
	2						
	.						
	.						
	.						
	K						

Figure 6.9 Priority State Matrix

The target priority model is supported by the "PRIORITY" computer work space described in Appendix E. The inputs of this program are the critical course of the ground target that the attacking aircraft are going to attack and the flight data of each attacking formation. The output of the

priority program will be used by the airmode1 to determine the priority of each target when one radar site detects more than one target.

VII. ADDITIONAL MODELS

Chapter seven describes the following models:

- A. IDENTIFICATION FRIEND OR FOE MODEL (IFF)
- B. ELECTRONIC WARFARE (ECM) MODEL
- C. COMMAND AND CONTROL MODEL
- D. RADAR PERFORMANCE MODEL
- E. PROBABILITY OF KILL MODEL

A. IDENTIFICATION FRIEND OR FOE (IFF) MODEL

1. Introduction

Another problem that a radar site commander has when a target is detected by the radar site, is to determine if a target is friend or enemy. Since this identification is impossible to obtain by optical means, both radar sites and aircraft are equipped with electronic devices which cooperate to give the identification of the aircraft.

2. Description

The IFF process, during operations, is very complicated. There are many decisions which must be made, as far as the identification of a target is concerned. For example, what must be decided if the IFF of radar site is not working? Will the target be regarded as a friend or a foe?

In this air model, the IFF process is illustrated in Figure 7.1.

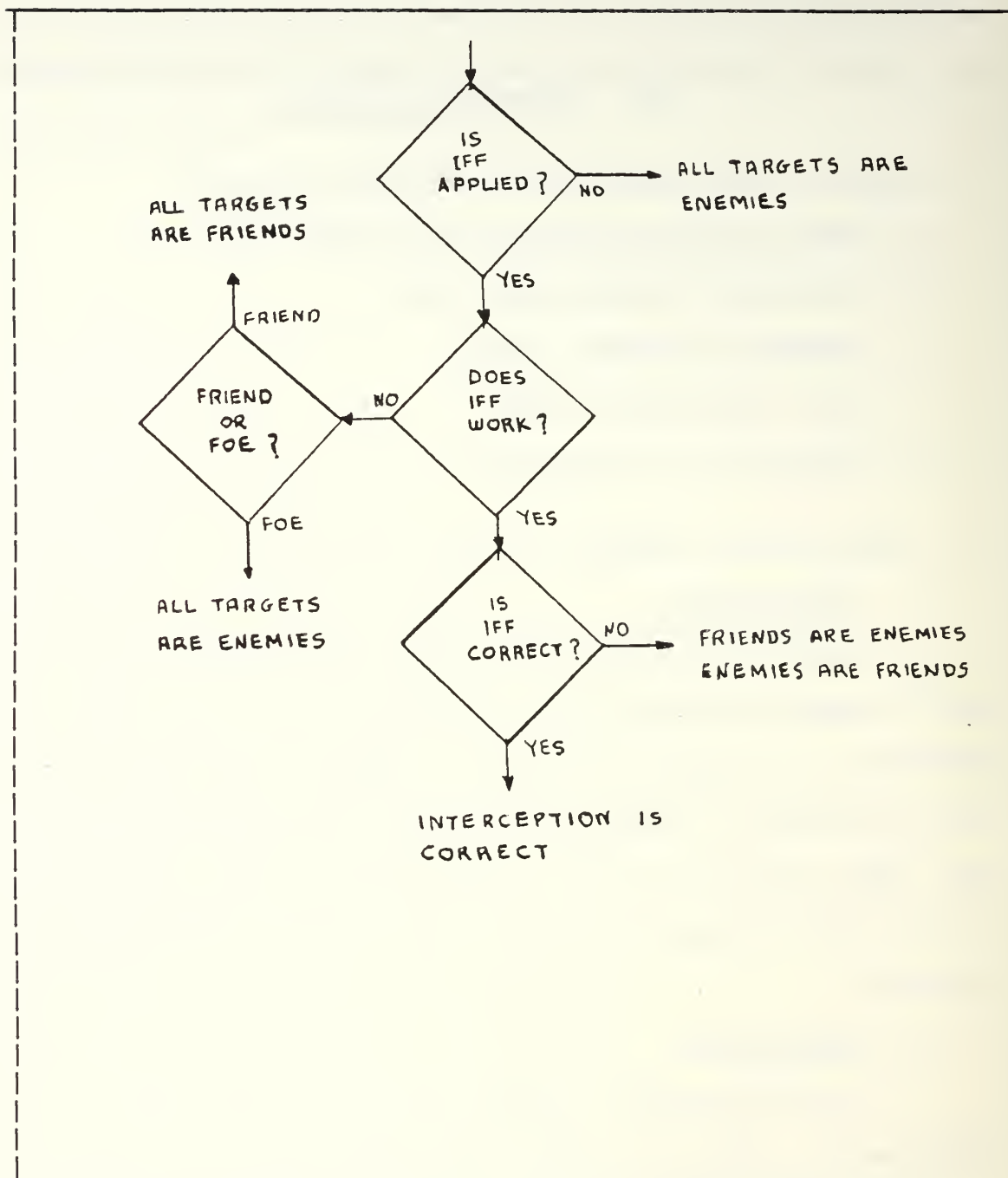


Figure 7.1 Logic Diagram of IFF Model

The above diagram is explained as:

- a. **Is IFF Applied?** Sometimes, radar sites do not apply IFF and they consider all targets to be enemies. That

may happen, for example, during a certain period of time, when there are no friendly aircraft scheduled to fly within range of the particular radar site. In this case radar operators gain time during the interceptions, but they assume that all detected targets are enemies and they can be killed. On the other hand, if IFF is applied the next question must be answered.

b. Is IFF working? Like other electronic devices, the IFF equipment is not always working. This may happen because either the IFF equipment of the aircraft or the IFF equipment of the radar site is not responding properly. If IFF is not working, the user must decide whether to treat the target as friend or as foe. If a target is friend the radar site stops the interception process and searches for another target. If the target is enemy, the interception process continues.

c. Is IFF correct? Unfortunately, IFF systems do not always give correct results. There is a possibility that even if the target is an enemy, the IFF system will indicate that the target is a friend. On the other hand, there is a possibility that, even if the target is a friend, the IFF system will indicate that the target is an enemy. If the first case happens, there is no big problem, just one enemy aircraft will pass without being intercepted. If the second case happens, friends will kill friends and a fratricide may occur.

The air model prompts the following inputs for IFF model:

1. If IFF is applied.
2. What is the probability that IFF works.
3. What is the identification of the target if the IFF does not work (friend of foe).
4. What is the probability that the IFF gives a correct answer (given that the IFF works).

B. ECM MODEL

1. Introduction

As the technology of the antiaircraft weapons (missiles, radar guided AAA etc) has been improved, the aircraft self protection means against the antiaircraft weapons have also been improved. Today, almost all airplanes use electronic devices for antimissile purposes such as electronic countermeasure means (ECM), chaffs, flares etc. Since this airmodel deals only with radar sites which use guided missiles to destroy the aircraft, only the electronic countermeasure means (ECM) will be simulated.

2. Description

The electronic countermeasure means are electronic devices which first recognize that the formation has been detected and acquired by the enemy radar sites. Then they try, by transmitting electronic energy, to brake the acquisition and if possible to "blind" the enemy radar for as

long as the aircraft formation flies within its range. Figure 7.2 shows how a radar site detects and acquires an aircraft formation.

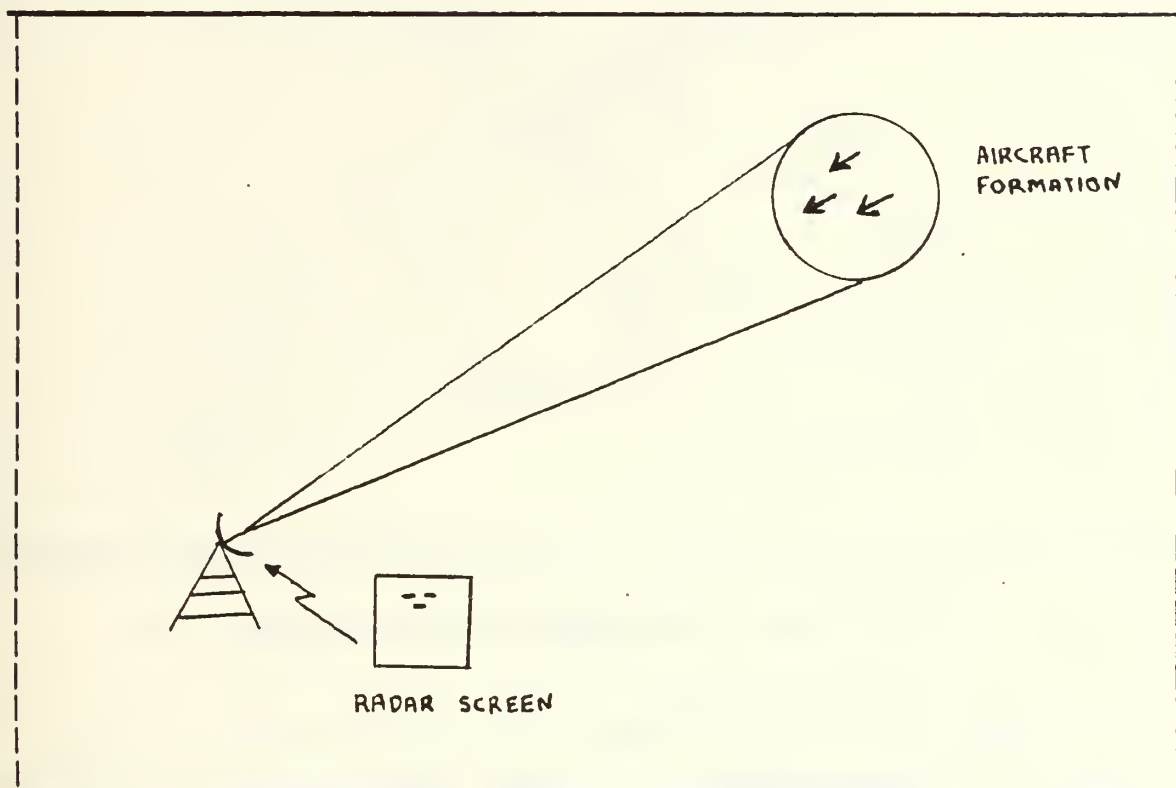


Figure 7.2 Aircraft Formation Detected by Radar Site

Modern radar sites can detect and acquire attacking formations, even if they fly in very low altitudes. On the other hand, modern aircrafts can realize both enemy radar detection and acquisition and they can, in most cases, break the lock-on if it exists or "blind" the enemy radar partially or totally. Figure 7.3 shows an aircraft formation which transmits electronic energy in order to break the radar site acquisition.

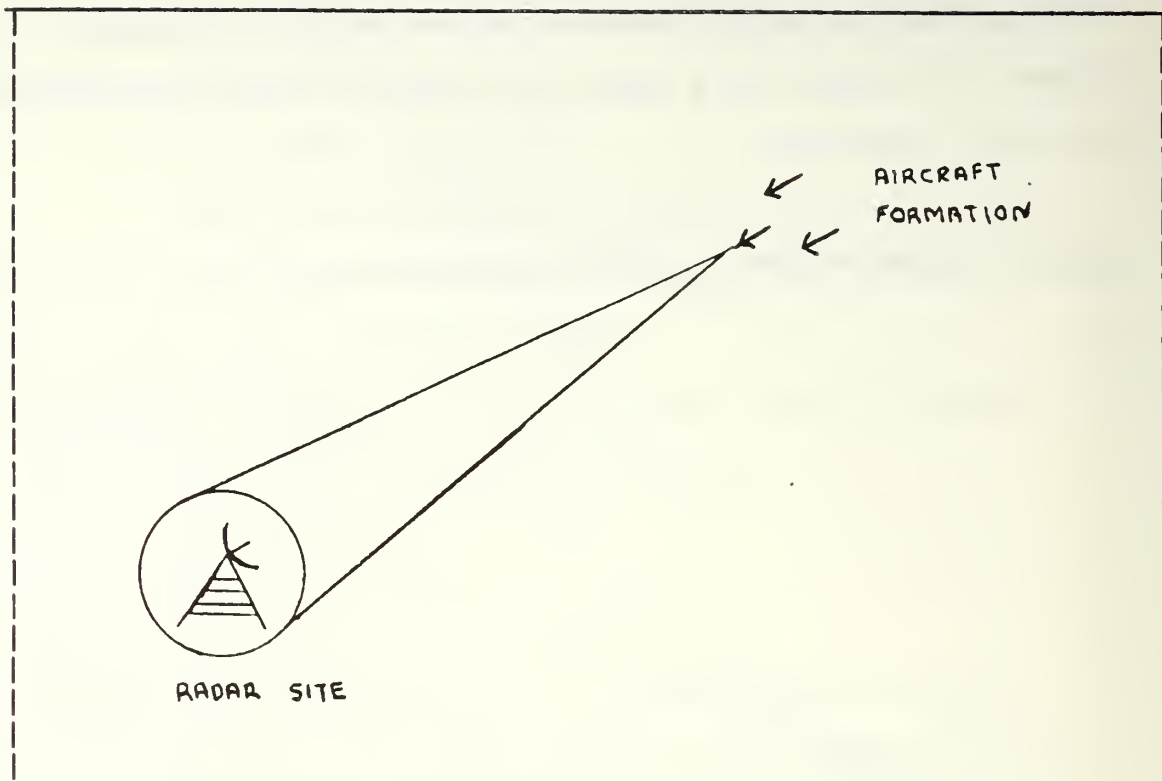


Figure 7.3 Aircraft Formation Using ECM

a. ECM Parameters

The success of the ECM employed by the aircraft formation depends on many factors but the most important are the power of the ECM device (P), the transmit angle (W) and the distance between aircraft formation and radar site (R). This is shown in Figure 7.4.

(1) Power. Like every electronic device, the ability of ECM depends on how much electronic energy is transmitted. The more energy there is, the more efficient the ECM. Unfortunately, large power ECM devices are very heavy and only special electronic aircrafts can carry them.

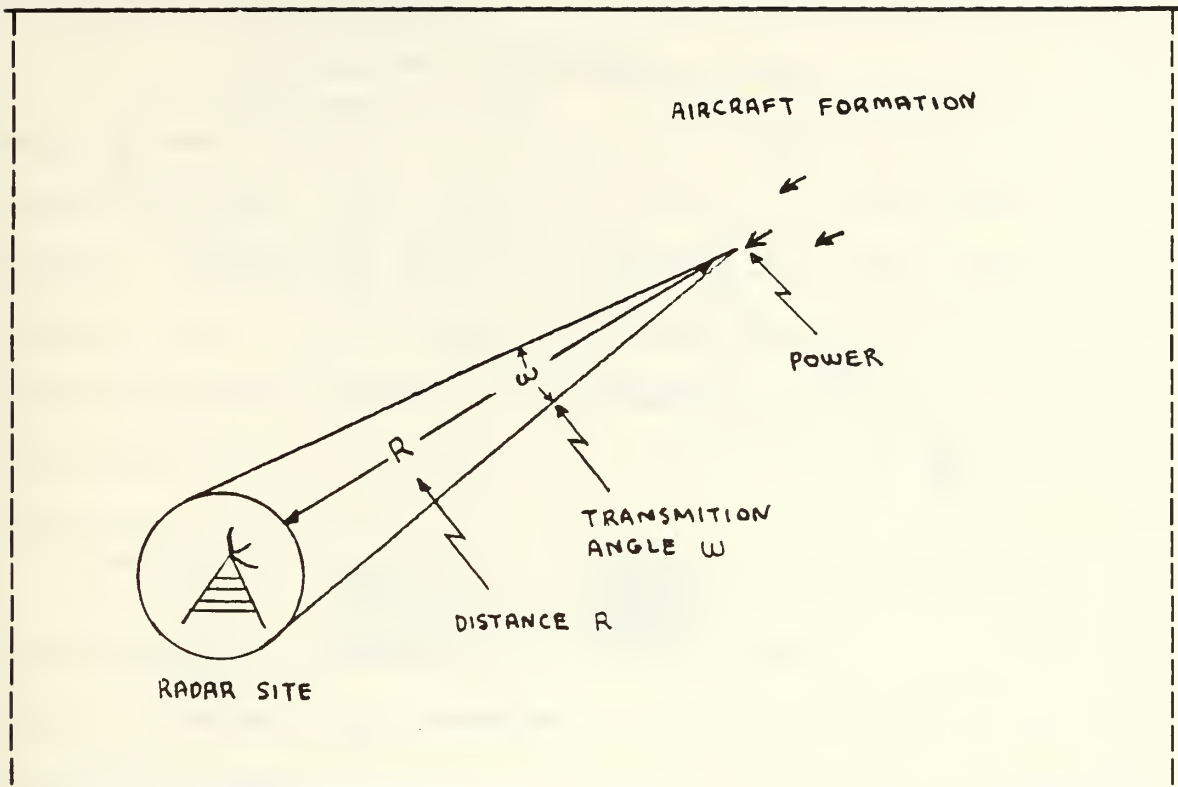


Figure 7.4 Parameters of ECM Device

Most fighter aircrafts use small or moderate power ECM and improve the ECM efficiency by narrowing the used transmitting angle w .

(2) Angle of transmitting energy. As radar sites, aircraft which apply ECM uses the angle of transmitting energy, in order to improve their ability to blind or break the acquisition of the radar site. By decreasing the angle, less electronic energy is being used to achieve the same purpose.

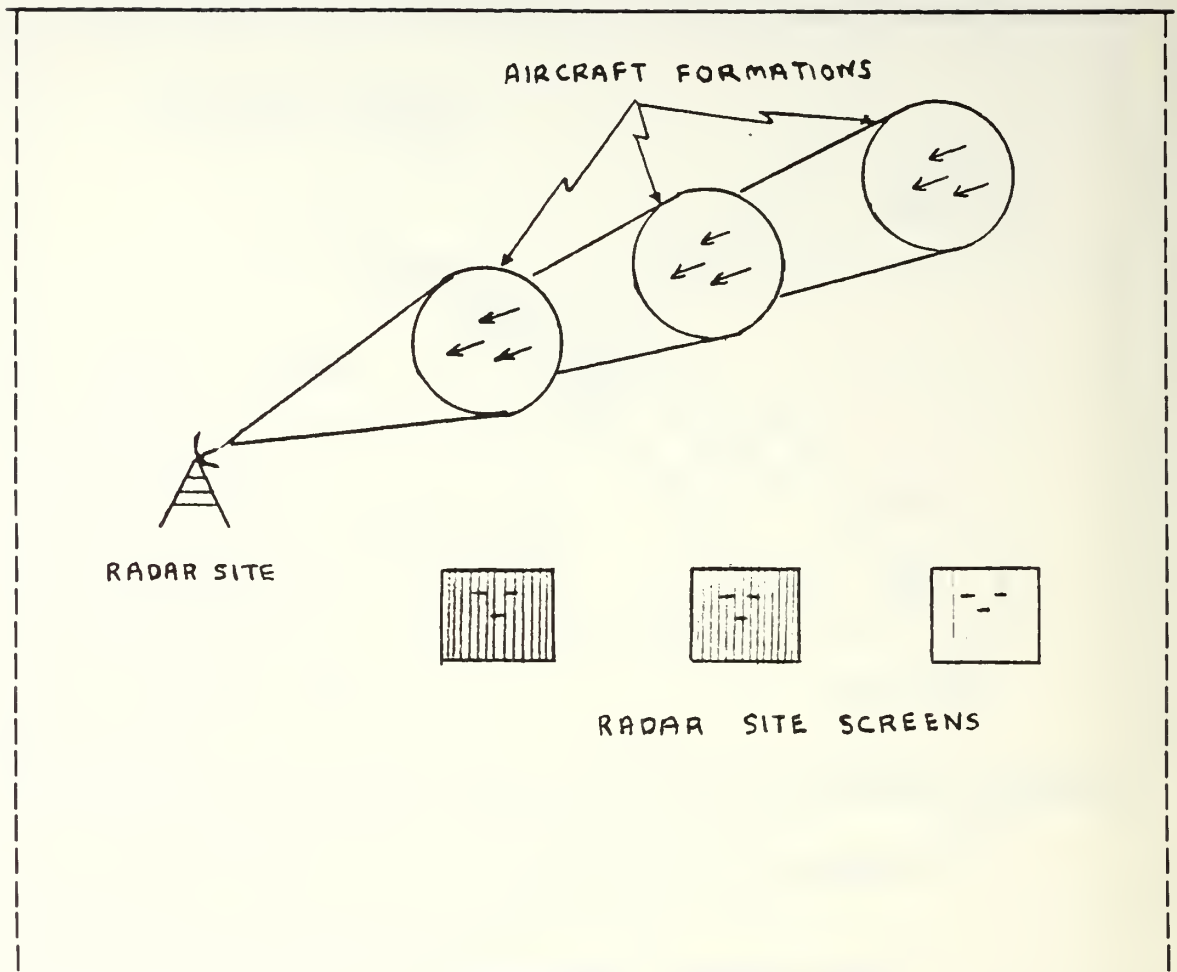


Figure 7.5 ECM Efficiency - Distance

(3) Distance between ECM and Radar Site. The distance is very important. The efficiency of ECM is inversely proportional to the distance square. How ECM efficiency changes by decreasing the distance between aircraft formation and radar site is shown in Figure 7.5.

b. ECM Function

Electronic countermeasure means can break the acquisition (lock-on) or increase the required time for identification, track, fire and target kill assessment events. To simulate the whole ECM process, two functions are needed. One function which increases the required time for the interception events and another function which changes the probability of breaking the acquisition by the radar site during the interception process.

(1) Interception Events Function. The function which increases the required time for identification, track, fire and target kill assessment events is assumed linear and has the following form:

$$\text{Time Events Matrix} = (\text{Time Events Matrix}) * \text{Increase Factor} \quad (1)$$

where time events matrix is a (N,3) matrix shown in Figure 7.6, and the increase factor is a factor that the events matrix must be multiplied with, in order that all time events be increased. For example, if the increase factor is equal to 1.5 (this value is used by the air model) the time events matrix will be increased by 50%.

	IDENT.	TRACK	FIRE	TARGET KILL ASSESSMENT
RADAR SITE 1	2	2	3	2
RADAR SITE 2	2	3	3	2
.
RADAR SITE N	3	3	4	3

Figure 7.6 Time Events Matrix

(2) Breaking Acquisition Function. When an aircraft formation is acquired by a radar site and employs ECM, there is a high probability that the radar site acquisition can be broken. The breaking acquisition function simulates this probability by using the mathematics model shown in Figure 7.7.

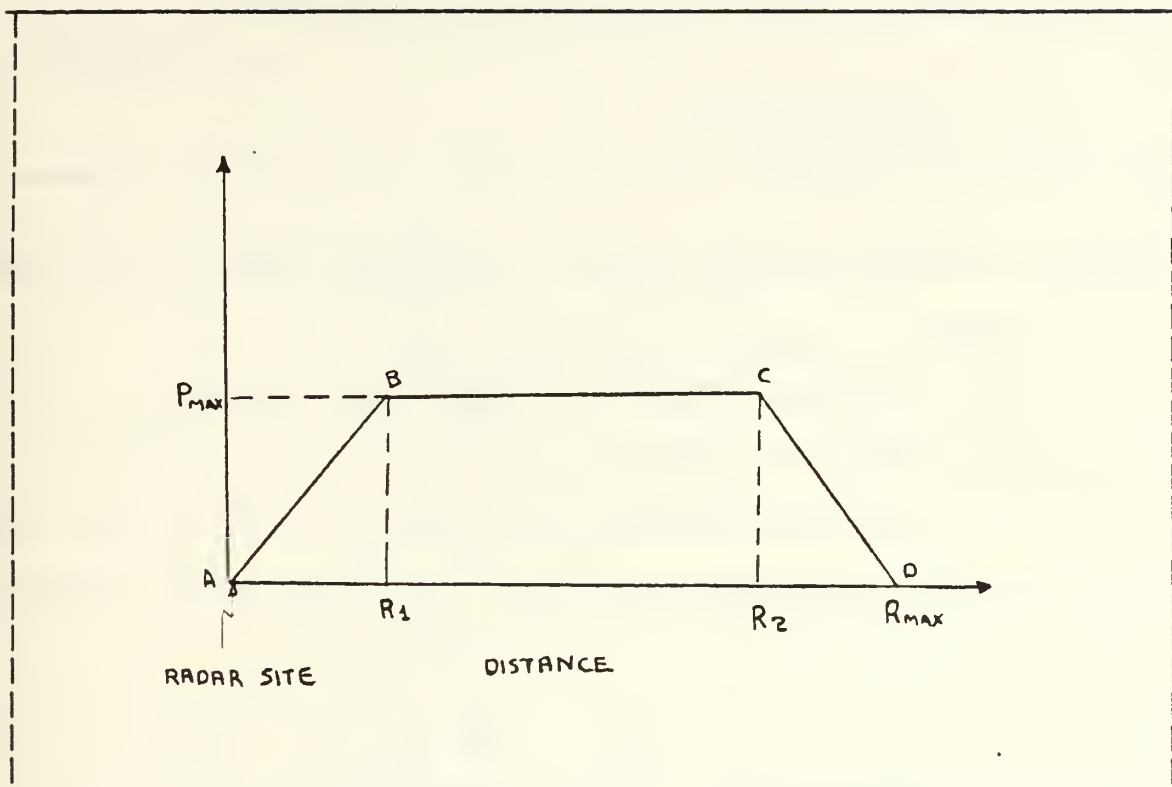


Figure 7.7 Breaking Acquisition Model

This model assumes that the probability of breaking the radar acquisition (P_r) is zero when the distance (R) between aircraft formation and radar site is greater than R_{max} , increases as the distance R decreases, reaches a maximum value (P_{max}) when the distance R is equal to R_2 , remains constant for the distance between R_2 and R_1 and then decreases when the distance R is less than R_1 . R_1 , R_2 , R_{max} and P_{max} are parameters of the breaking acquisition function specified by the user. The equations which gives the probability of acquisition breaking are as follows:

$$P_r = \frac{(P_m) \times (R)}{R_1} \quad \text{IF} \quad 0 < R < R_1$$

$$Pr = P_m$$

IF

$$R_1 < R < R_2$$

$$Pr = \frac{(PK_{max}) * (R_2 - R)}{R_2 - R_m}$$

IF

$$R_2 < R < R_m$$

where: R is the distance between aircraft formation and radar site.

R_1 , R_2 , R_{max} , P_{max} are parameters of breaking aquisition function (Figure 7.7).

Each aircraft formation has its own R_1 , R_2 , R_{max} and P_{max} and these data are given to the air model in matrix form as follows:

	R_1	R_2	R_m	P_{max}
a/c formation 1	5	30	30	0.7
a/c formation 2	5	40	70	0.5
a/c formation 3	0	0	0	0
.
a/c formation N	5	20	50	0.5

The first column is the R_1 distance for a/c formations.

The second column is the R_2 distance for a/c formations.

The third column is the R_{max} distance for a/c formations.

The fourth column is the P_{max} for a/c formations.

The fifth column is the probability than ECM works.

The third row is zero because the third a/c formation does not employ ECM.

The logic diagram for the ECM process is shown in Figure 7.8.

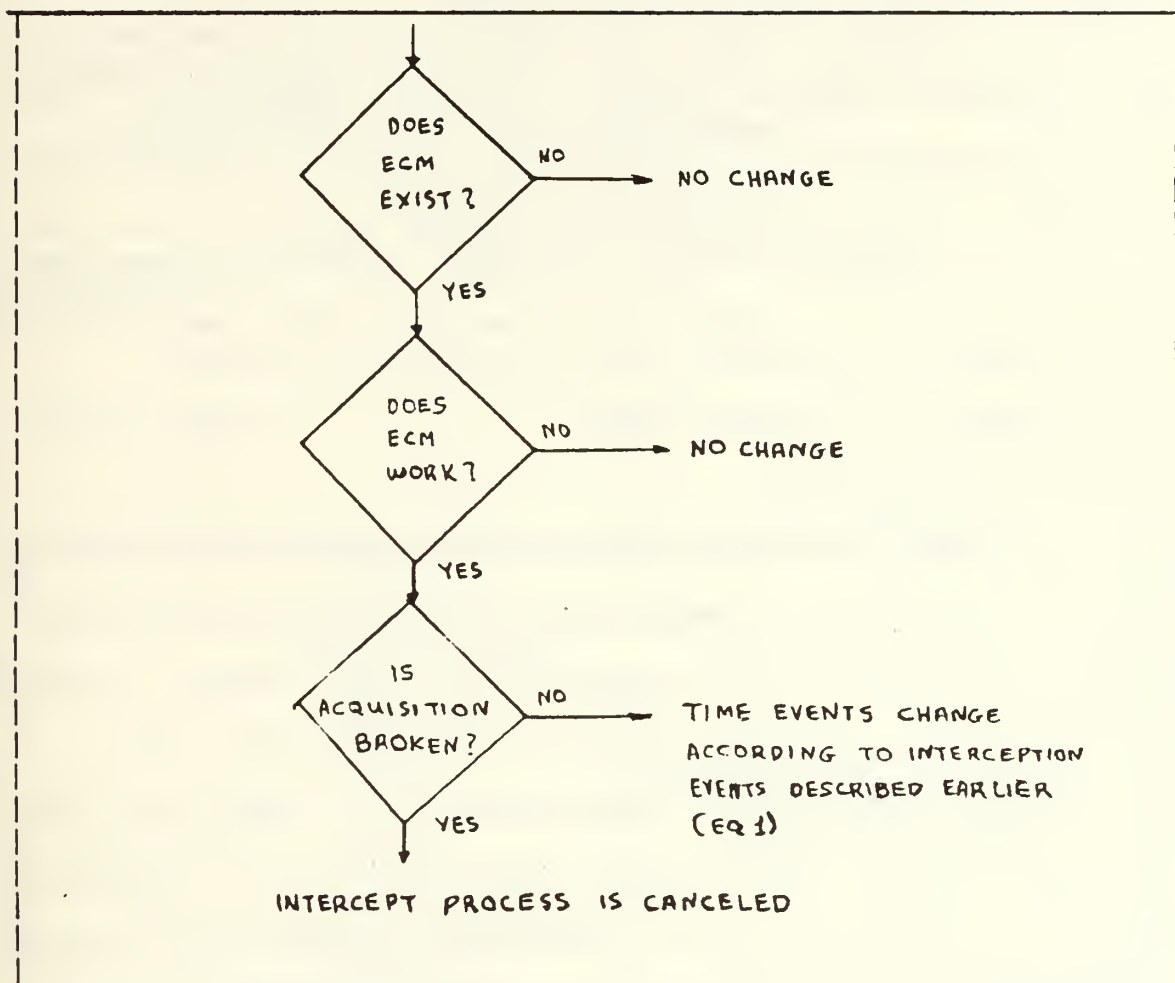


Figure 7.8 ECM Process Logic Diagram

The algorithm of the ECM process follows the steps:

Step 1: Does the aircraft formation apply ECM?

If NO: No changes to interception time events.

If YES: Go to step 2.

Step 2: Does ECM work?

If NO: No changes to interception time events.

If YES: Go to step 3.

Step 3: Is radar acquisition broken?

If NO: Identification, track, fire and target assessment time events will increase according to equation (1).

If YES: Further intercept process is cancelled and target goes again for identification.

C. COMMAND AND CONTROL MODEL

1. Introduction

When two or more radar sites cooperate to defend an area, a centralized command and control organization must exist to control all the radar sites. For example, if there are more than two targets flying over this area, the centralized organization will decide what target radar site one will engage, what target radar site two will engage and so on. In this way, more targets will be destroyed because each radar site will engage only its own targets.

2. Description

Since a complex command and control model is very difficult to simulate, the airmodel uses the following simple algorithm: No target will be engaged by more than one radar site. That means that when a particular target is engaged by a radar site, no other radar site is allowed to engage it until the target is released (not destroyed) by the original radar site. By using this algorithm there is not possibility for two radar sites to destroy the same target. This rule

can be revised and the aircraft formation can be engaged by more than one radar site if the number of aircraft in the formation is greater than a certain number N . This number is prompted by the air model and it must be entered by the user. For example, if $N = 3$ and the aircraft formation has five aircraft, then this formation can be engaged by more than one radar site until only 3 aircraft remain in this formation.

Figure 7.9 shows the logic diagram of command and control model.

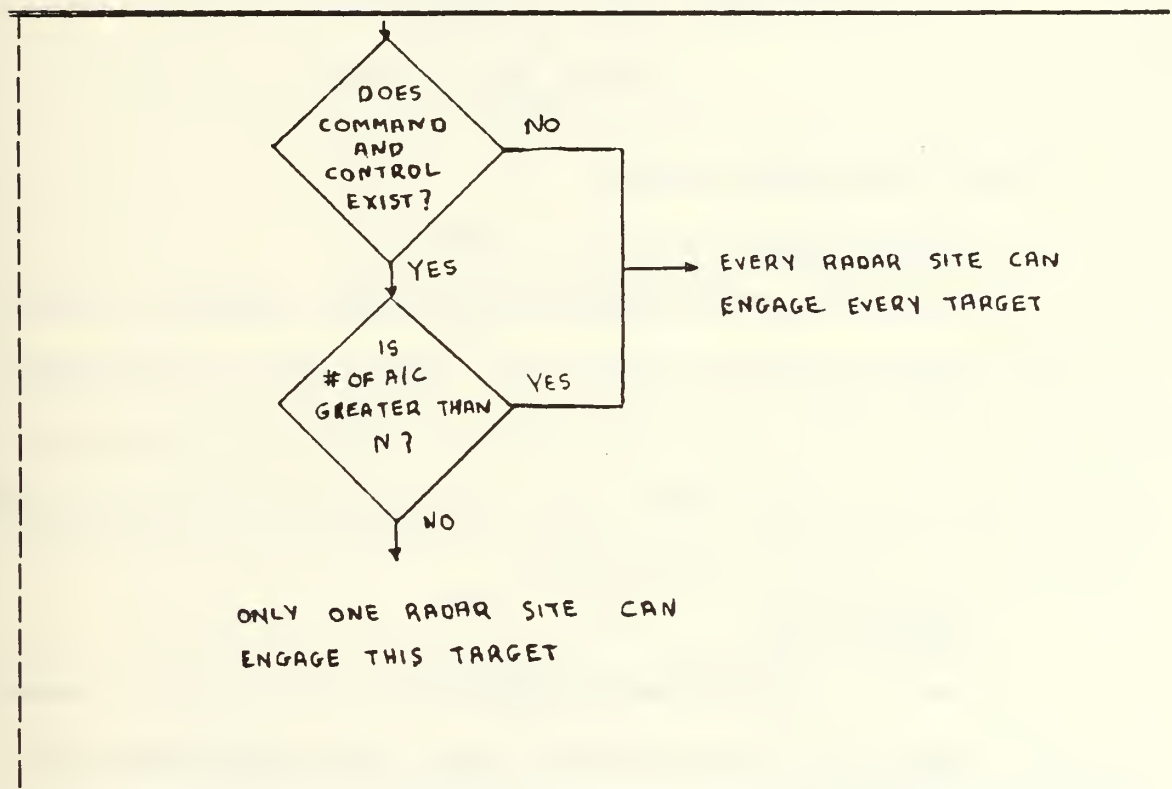


Figure 7.9 Logic Diagram of Command and Control Model

The algorithm of the command and control model follows these steps:

Step 1: Does command and control model exist?

If NO: Every radar site can engage this target.

If YES: Go to step 2.

Step 2: Is the number of aircraft less than N (user input)?

If NO: Every radar site can engage this target.

If YES: Only one radar site is allowed to engage this target.

D. RADAR PERFORMANCE MODEL

1. Introduction

The performance of the radar sites depends on many factors such as age of radar site, experience of operators, weather conditions, and enemy ECM. In addition, there is a possibility that the radar site will be partially or totally destroyed during the operations.

2. Description

The air model uses a simple radar performance model. It aggregates all factors which effect the performance of radar site to one factor called "performance". This factor is prompted by the airmodel and it takes one of the two values that follow:

'1' if the user prefers the radar site to work in full performance, and
'0' if the user prefers the radar site to work in limited performance.

Figure 7.10 shows the logical diagram of the radar performance model:

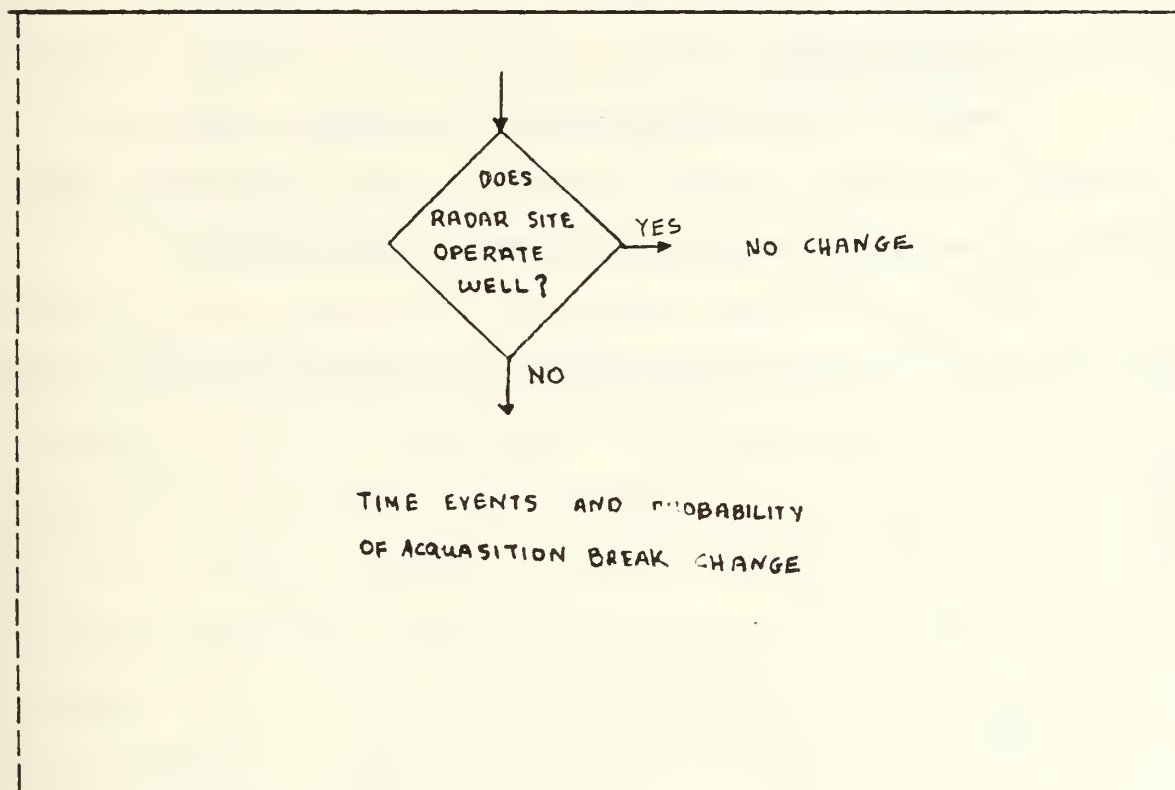


Figure 7.10 Logic Diagram of Radar Site's Performance Model

If radar sites operate in full performance (performance value is 1) there is no change to airmodel. If radar sites work in limited performance (performance value is 0) the identification, track, fire and target assessment time are increased by a factor input by the user. The probability

that a radar site acquisition will be broken due to ECM can also be increased by a factor determined by the user. If the radar site operates in limited performance situation, the time to identify, track, fire and assess a target kill increases and the chance that a target acquisition will be broken is also more likely.

E. PROBABILITY OF KILL MODEL

1. Introduction

Calculation of probability of killing (PK) an aircraft by using a guided missile is very important, but unfortunately, extremely difficult to calculate.

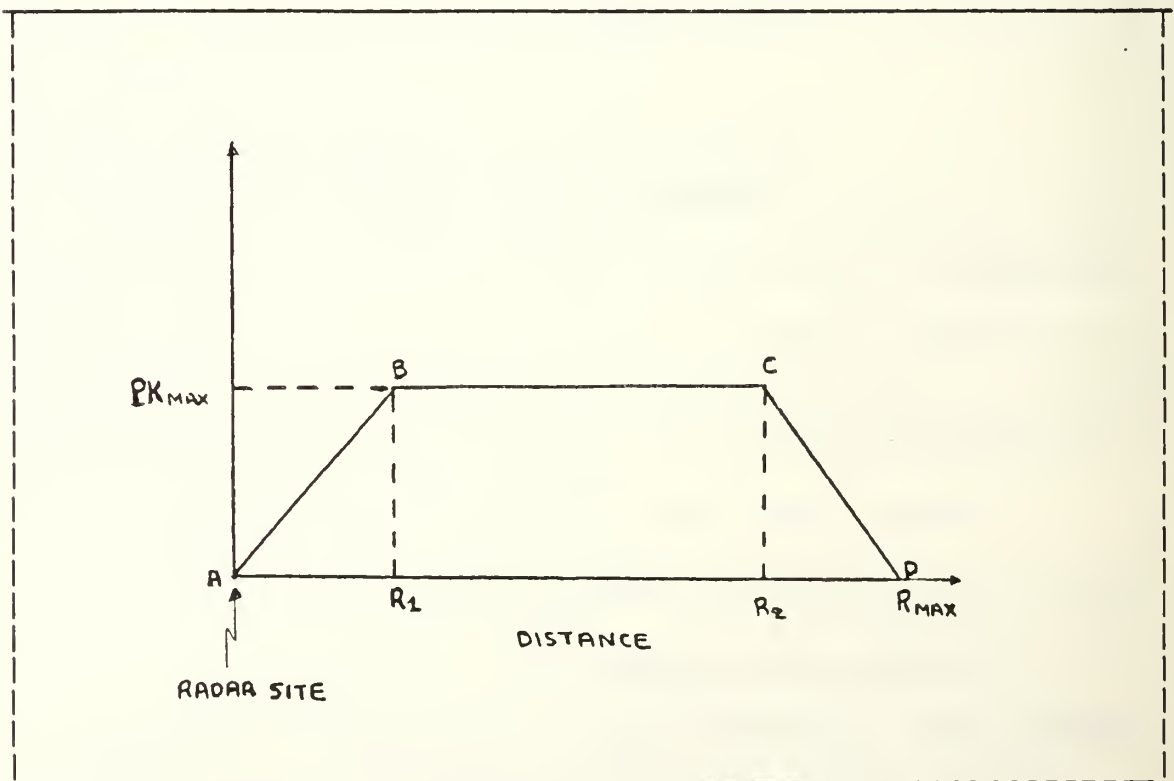


Figure 7.11 Probability of Kill Model

The problem is that the probability of kill depends on so many factors, known and unknown, that it is essentially impossible to create a relatively simple model to estimate it using all the factors.

2. Description

The airmodel uses a simple, but quite reasonable model to estimate the PK. It assumes that the probability changes Linearly as the range between the a/c and the radar site changes. Figure 7.11 shows how the PK changes relatively to R.

The PK is zero when the distance (R) between aircraft formation and radar site is greater than the maximum range (Rmax) of missile that this particular radar site uses. The propability of kill increases as R decreases (aircraft approaches the radar site) reaching the maximum value (PKmax) at R2, it stays constant for the distances between R2 and R1 and then decreases when the distance R is less than the distance R1. R1, R2, Rmax and PKmax are values prompted by the airmodel.

The equation used to calculate the PK, are the same as in the ECM model, is:

$$PK = \frac{(PK) \times (R)}{R1} \quad \text{IF} \quad 0 < R < R1$$

$$PK = PKmax \quad \text{IF} \quad R1 < R < R2$$

$$PK = \frac{(PKmax) \times (R2 - R)}{R2 - Rmax} \quad \text{IF} \quad R2 < R < Rmax$$

where: R = the distance between aircraft target and radar site.

R1, R2, Rmax, Pmax are parameters of the probability of kill function and must be entered in the air model by the user for each radar site in matrix form as follows:

	R1	R2	Rmax	PKmax
Radar Site 1	5	15	20	0.50
Radar Site 2	7	35	40	0.55
.
Radar Site N	10	50	55	0.40

The first column is the R1 distance for each radar site.

The second column is the R2 distance for each radar site.

The third column is the Rmax distance for each radar site.

The fourth column is the PKmax for each radar site.

VIII. COMPUTER PROGRAM "AIRMODEL"

Chapter VIII describes the "AIRMODEL" computer work space. It defines the functions, inputs, and outputs of the program.

A. INTRODUCTION

In the previous chapters, the pre-processing models were described in detail. All these models were deterministic because the outputs are the same, given the same inputs. These models calculate all the data that the "AIRMODEL" work space needs to run. The purpose of "AIRMODEL" is to calculate the attrition rate of the attacking aircraft formation by using the data given by the models described in Chapter II through VII. This program simulates the aircraft formation engagement sequence by the radar sites. An air defense radar site follows a well defined engagement sequence as it attempts to destroy enemy aircraft. The steps of the sequence are:

Step 1: Detection. The system/operator observes the presense of an aircraft formation on the radar screen in the assigned airspace.

Step 2: Identification. The operator identifies the target as friend or foe.

Step 3: Track. The site tracking radars obtain radar lock on the target.

Step 4: Fire. The site launches a missile attempting to destroy the target.

Step 5: Intercept. The missile arrives at a predicted point in space. This point is assumed to be the location of the collision of the missile and the target.

Step 6: Aircraft Kill Assessment. The system/operator decides if target destruction has been achieved.

These steps are illustrated in Figure 8.1.

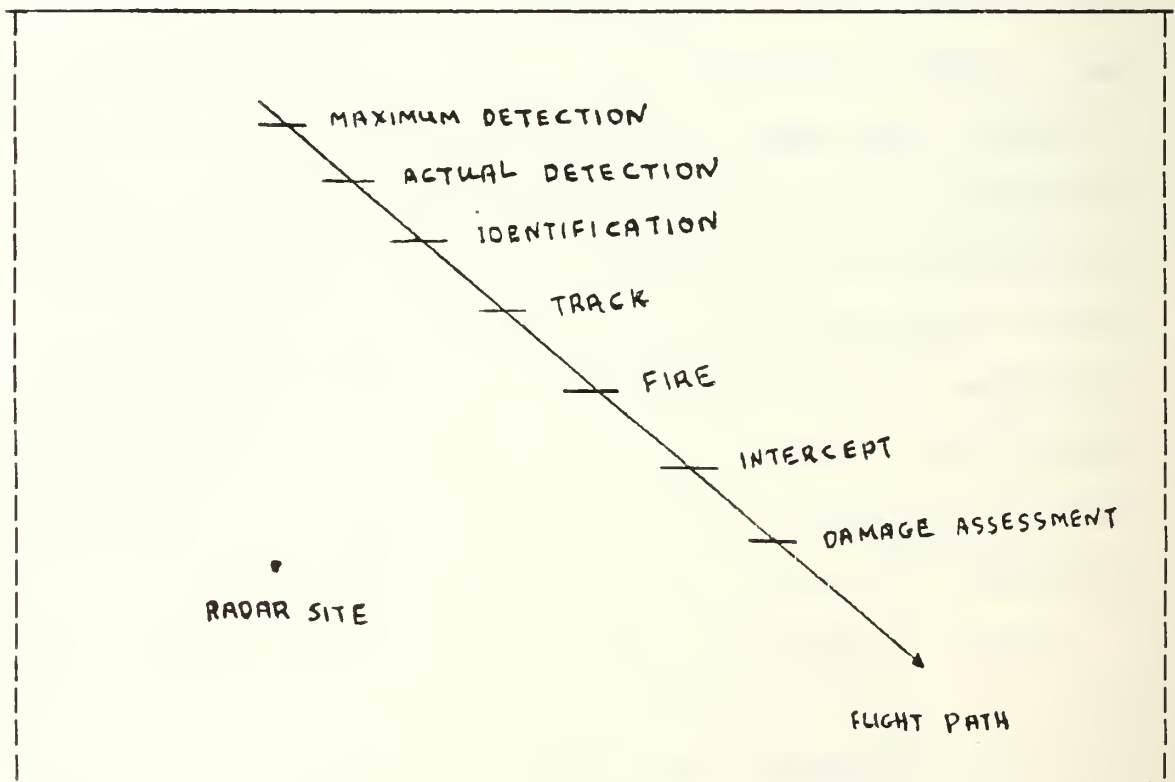


Figure 8.1 The Engagement Sequence

If the target leaves radar surveillance (either acquisition or tracking), the sequence is terminated. When

the target returns to the site detection envelop, it is considered to be a new acquisition.

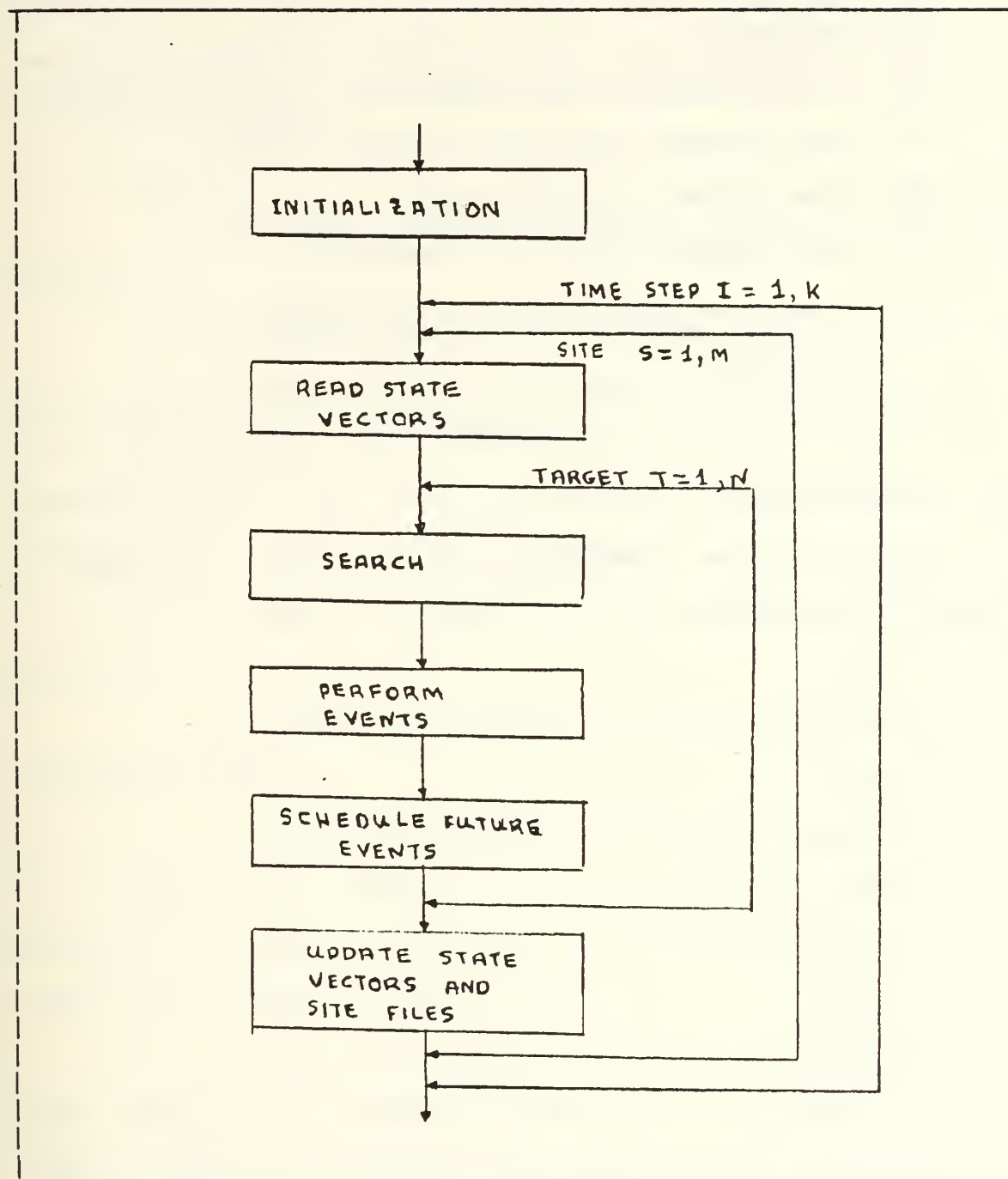


Figure 8.2 Airmodel Flow Chart

The time delays associated with each step of the sequence are defined as follows:

T_d = time between maximum possible detection and actual detection.

T_{id} = time between actual detection and identification.

T_t = time between identification and track.

T_f = time between track and fire.

T_i = time between fire and interception.

T_a = time between intercept and assessment of the intercept.

The flow chart of the "AIRMODEL" is shown in Figure 8.2.

B. DESCRIPTION

The work space "AIRMODEL" consists of the following computer functions:

1. MAIN
2. SITE
3. IDIF
4. TRACK
5. FIRE
6. INTER
7. ASSES
8. PKILL
9. RANDOM

1. Main

- a. Header

The header of the "MAIN" program is ""MAIN" and the computer program is listed in Appendix F.

b. Purpose

The purpose of the main computer function is to prompt all the inputs from the user and to call the site function in order to calculate the attrition rate of the aircraft formations.

c. Input

The "MAIN" computer program prompts the following inputs:

1. RL: The seed for the random number function. This seed is needed to generate random variable inputs. If the main program runs the same data twice, the same sequence of the output will be produced unless the seed is changed.
2. Times: The number of times that the program will run.
3. NSITES: The number of radar sites in the particular scenario.
4. DS2: The detection matrix of each radar site, given by the "FDETECT" computer work space. The "MAIN" program will prompt the entering of the detection matrix based on the number of radar sites.
5. IS2: The interception matrix of each radar site, given by the "INTERCEPT" computer work space. The "MAIN" program will prompt the entering of the interception matrix based on the number of radar sites.
6. TGT: The number of aircraft that each formation has. If the number of aircraft is zero during the

simulation, the aircraft formation is deleted from the simulation process. The TGT input is a vector whose number of elements must be equal to the number of aircraft formations (each element equal to the number of a/c).

7. CAP2: The number of aircraft that each radar site can engage. If a particular radar site has engaged its maximum number of aircraft, it is considered to be satutated and is not allowed to engage more targets. The CAP2 input is a vector whose number of elements must equal the number of radar sites (each element for each radar site).

8. MCAP2: The number of missiles that each radar site possesses. If a particular site has launched all its missiles, then it is deleted from the simulation process. The input MCAP2 is a vector whose number of elements must be equal to the number of radar sites (each element for each radar site).

9. PKM: The probability of kill matrix, given by the "PROBABILITY OF KILL" model.

10. IFF: The IFF input takes one of two values as follows:

1 = IFF is applied in the simulation process.

0 = IFF is not applied.

If IFF is not applied, the "MAIN" program assumes that a detected target is always friend.

11. IFFWORK: The probability that the IFF works

12. IFFFOE: The IFFFOE input takes one of two values as follows:

1 = a target is friend if IFF does not work.

0 = a target is foe if IFF does not work.

13. IFFCOR: The probability that IFF is correct given that it works.

14. ECM: The electronic countermeasure matrix, given by the "ECM" model.

15. CMD: The input CMD takes one of two values as follows:

1 = command and control model is applied.

0 = command and control model is not applied.

16. PR: The priority matrix, given by "THE PRIORITY" model.

17. AUTO: The condition which determines whether the radar sites operate autonomously, given that command and control model is applied.

18. WTH: The input WTH takes one of two values as follows:

1 = radar site operation is normal.

0 = radar site operation is degraded.

19. LBR: The factor describing the increase in acquisition time, given that the operation of the radar sites is degraded.

20. ETSF: The factor describing the increase in firing time given that the operation of radar sites is degraded.

21. TSTEP1: The (N,4) event time steps matrix. The columns of the TSTEP1 matrix are the required time for identification, track, fire and target damage assessment. The number of rows (N) is the number of radar sites.

d. Output

The "MAIN" program gives the following outputs:

1. Summary of the User Scenario.
2. Attrition Matrix in details. The form of the attrition matrix is as follows:

MISSILE SITE:	1	1	2	2	1	2	2	1
TIME STEP:	10	32	45	102	105	105	14	250
NUMBER OF								
TARGETS KILLED:	1	3	2	3	1	1	2	3

The first row consists of the number of the radar sites which have achieved a target kill. The second row documents the time steps. The third row consists of the numbers of target kills. For example, the first column means that the first radar site destroyed one aircraft from formation one in time step ten.

3. Remaining missiles for each site.
4. The number of targets which are destroyed but not assessed by the radar site. In some cases, it is possible to intercept a target without receiving clear indications of destruction.
5. The number of target kills per aircraft formation.

2. Site

a. Header

The header of "SITE" function is "SS SITE I" and the computer program is listed in Appendix F.

b. Purpose

The function "SITE" combines the database and the other functions used by the work space "AIRMODEL" to calculate the attrition rate of the attacking aircraft formations against ground targets. This function is called by the main program once for each radar site for each time step.

c. Input

1. The left argument (SS) is the number of the radar site.

2. The right argument (I) is the time step.

d. Output

The function SITE does not provide any output, instead it calls the IDIF, TRACK, FIRE, INTER, ASSES, RANDOM and PKILL functions in order to schedule future events and calculate the attrition rate.

3. IDIF

a. Header

The header of the "IDIF" function is "ID <- ISIT IDIF R"; the computer program is listed in Appendix F.

b. Purpose

This function is called by the program "SITE" to perform the identification of the targets.

c. Input

1. The left argument (ISITE) is a vector whose first element is the number of the radar site and whose second is the time step.

2. The right argument (R) is the number of the target.

d. Output

The output is the future identification event.

4. Track

a. Header

The header of the function "TRACK" is "TT <- ISITE TRACK T"; the computer program is listed in Appendix F.

b. Purpose

The function TRACK is used by the SITE program to perform the track target event.

c. Input

1. The left argument (ISITE) is a vector, whose first element is the radar site number and whose second is the time step.

2. The right argument (T) is the number of the target.

d. Output

The output is the future track event.

5. Fire

a. Header

The header of the function "FIRE" is
"FR <- ISITE FIRE F"; the computer program is listed in
Appendix F.

b. Purpose

The function FIRE is called by the SITE program
to perform the missile fire event.

c. Input

1. The left argument (ISITE) is a vector, whose
first element is the radar site number and whose second is
the time step.

2. The right argument (F) is the number of the
target.

d. Output

The output is the future missile Fire event.

6. INTER

a. Header

The header of the function "INTER" is
"INT <- ISITE INTER IN"; the computer program is listed in
Appendix F.

b. Purpose

This function is called by the SITE program to
perform the interception of the target.

c. Input

1. The left argument (ISITE) is a vector whose first argument is the radar site number and whose second is the time step.

2. The right argument (IN) is the number of the target.

d. Output

1. The time required for interception.

2. The distance that the target flies until it is intercepted.

3. The distance that the interceptor flies until the interception is performed.

4. The future target interception event.

7. ASSESS

a. Header

The header of the function "ASSES" is "AM <- ISITE ASSWS AS"; the computer program is listed in Appendix F.

b. Purpose

This function is called by the SITE program to perform the target damage assessment event.

c. Input

1. The left argument (ISITE) is a vector whose first element is the radar site number and whose second is the time step.

2. The right argument (AS) is the number of the target.

d. Output

The output is the time required to assess target damage. This is used to schedule the assessment future event.

8. PKILL

a. Header

The header of the function "PKILL" is "PK <- PKM PKILL R"; the computer program is listed in Appendix F.

b. Purpose

This function is called by the SITE program to calculate the probability of kill for each radar site and the effectiveness of ECM.

c. Input

1. The first argument (PKM) is the PK of the ECM matrix given by the Probability of Killing model and ECM model respectively.

2. The second argument (R) is a two element vector whose first element is the number of the target and whose second is the distance between the radar site and the target.

d. Output

1. The probability that a missile, launched by a radar site, will kill an aircraft.

2. The probability that the acquisition achieved by a radar site, will cease because of electronic countermeasures.

9. RANDOM

a. Header

The header of the function "RANDOM" is
"RN <- RANDOM"; the computer program is listed in Appendix F.

b. Purpose

This function is called by the SITE program to
generate a uniform random variable between zero and one.

c. Input

None.

d. Output

The output is a random number used to determine
probabilities when a stochastic output is required.

IX. SIMULATION OF A PARTICULAR SCENARIO

A. INTRODUCTION

The technique of simulating aircraft attacks against a ground target and their interception by a missile site was described in Chapter II through VIII. In this chapter, a particular scenario is described and simulated with various combinations of inputs to calculate aircraft attrition. It also summarizes all the steps which must be followed to simulate the scenario and to calculate the aircraft attrition rate. Furthermore, the output data given by the airmodel using this particular scenario, will be analyzed and subjected to a sensitivity analysis of critical variables.

B. DESCRIPTION OF THE SCENARIO

The particular scenario used for simulation is shown in Figure 9.1.

1. Map

The map used for the scenario design is an Air Force map. It is used by pilots to plan aircraft routes for specific missions. The map scale is 1:500,000 and has sufficient contour lines to read the terrain altitudes and to plan the aircraft routes so as to take advantage of terrain masking. A 162 NM by 120 NM area is chosen to represent the enemy country which the attacking formations will fly over.

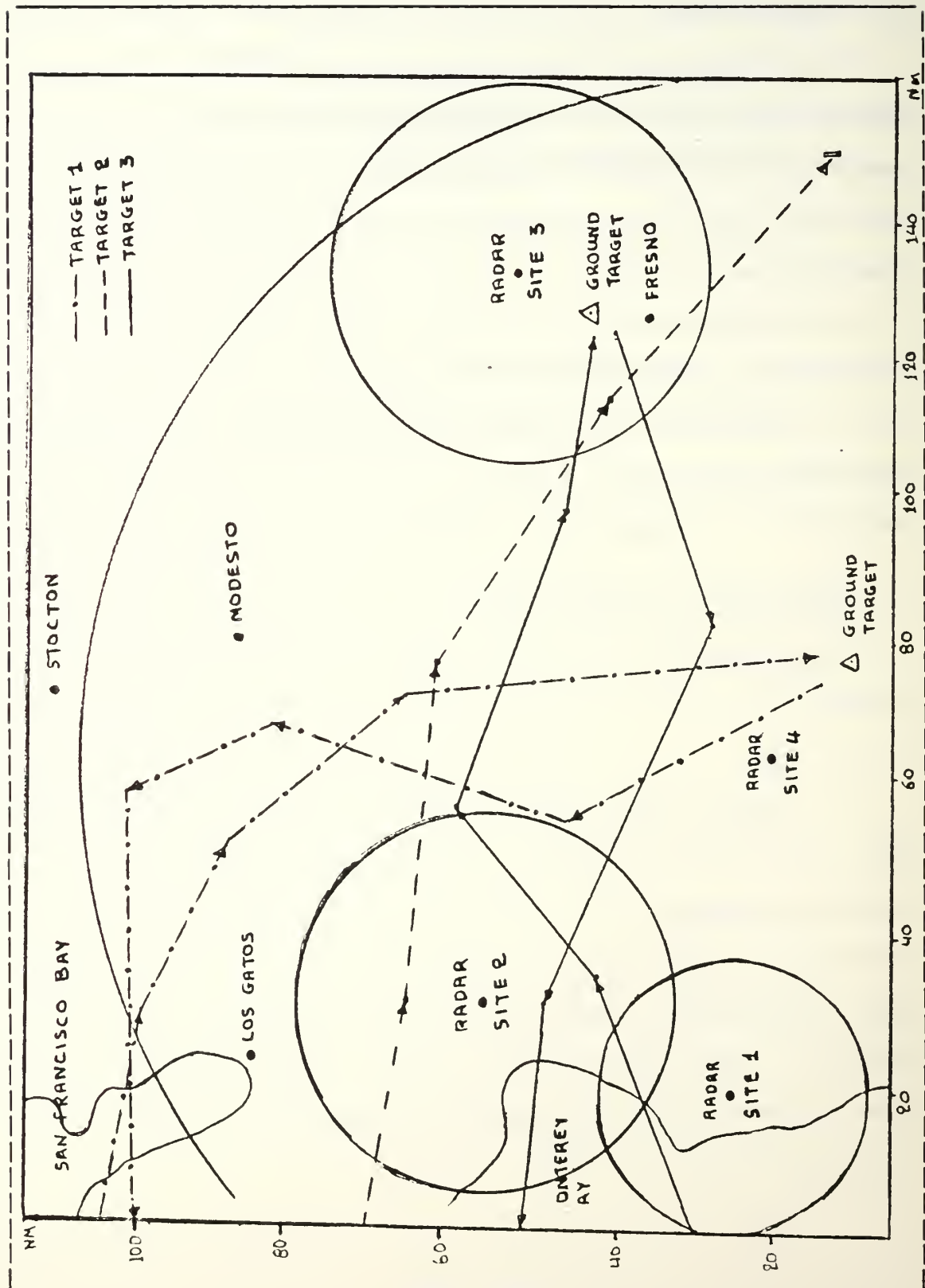


Figure 9.1 Scenario

The area is divided into grid squares. The time steps chosen for this simulation are 10 seconds.

2. Aircraft Formations

There are three aircraft formations simulated in this particular scenario.

a. Aircraft Formation 1 (Target 1)

(1) Type. The aircraft formation 1 is an enemy formation and it consists of 9 bomber aircraft.

(2) Purpose. The mission of the formation is to attack an airport whose coordinates are $X = 98$ NM and $Y = 9$ NM inland. This target will fly over the NIKE radar site.

(3) Initial point and Start Time. Formation 1 enters the enemy terrain at $X = 0$ NM, $Y = 111$ NM point and at time zero. (This is the first target entering the simulation).

(4) Flight Data. The flight routes of formation 1 consist of eight straight lines and the flight data of each flight route are listed below:

Route	Course (degrees)	Length (NM)	Speed (knots)	Altitude (feet)
1	17	35	2120	1000
2	120	44	420	1000
3	157	27	420	1000
4	165	46	480	1000
5	334	38	480	2000
6	004	30	420	1000
7	342	28	420	1000
8	270	69	420	10,000

(5) Comments. The speed in routes 4 and 5 is increased from 420 to 480 knots because the aircraft formation is in its attack approach at this time. The altitude in route 5 is increased from 1000 ft to 2000 ft because the aircraft formation needs to be formed again after the airport attack. In route 8 altitude is increased because the aircraft formation need to save fuel in order to return to its base.

b. Aircraft Formation 2 (Target 2)

(1) Type. The aircraft formation 2 is a friendly formation and it consists of four interceptor airplanes.

(2) Purpose. The mission of this formation is to intercept enemy aircraft and return to its base (X = 163 NM, Y = 2 NM) for refueling. It penetrates both "HAWK" and "NIKE" radar sites and is included here to demonstrate the accidental attrition of friendly aircraft due to human errors (fratricide).

(3) Initial Point and Start Time. Target 2 enters the area at X = 0 NM, Y = 81 NM point 6 minutes after time zero.

(4) Flight Data. The flight routes of Formation 2 consist of three straight lines and the flight data of each flight route are listed below:

Route	Course (degrees)	Length (NM)	Speed (knots)	Altitude (feet)
1	109	37	420	20.000
2	118	44	420	20.000
3	131	64	420	10.000

(5) Comments. The altitude in route 3 changes from 20,000 ft to 10,000 ft because the aircraft formation descends for landing.

c. Aircraft Formation 3 (target 3)

(1) Type. The Aircraft Formation 3 is an enemy formation and it consists of 11 bomber airplanes.

(2) Purpose. The mission of the formation is to attack the airport whose coordinates are X = 130 NM, Y = 32 NM inside enemy territory. This target's flight plan takes it through two overlapping HAWK radar sites. This will allow an investigation of the command and control model.

(3) Initial Point and Start Time. The aircraft formation enters the enemy area at the point whose coordinates are X = 0 NM, Y = 31 NM and at 5 minutes after time 0.

(4) Flight Data. The flight routes of aircraft Formation 3 consist of seven straight lines and the flight data of each route are listed below:

Route	Course (degrees)	Length (NM)	Speed (knots)	Altitude (feet)
1	088	40	420	1000
2	050	35	420	1000
3	111	31	420	1000
4	082	28	480	1000
5	249	40	480	2000
6	299	45	420	1000
7	280	49	420	1000

(5) Comments. The speed in route 4 and 5 changes from 420 to 480 knots because the formation is in its attack phase. The altitude in route 3 increases from 1000 ft to 2000 ft because the formation needs to regroup after attacking the target.

3. Radar Sites

In this particular scenario, there are three HAWK radar sites and one NIKE site. The NIKE site covers almost all the country; the first two HAWK sites are overlapping and cover the entrance to the defended area. The third HAWK site protects a very important industrial town inside the country.

The parameters of four radar sites are shown on Table.

Radar Site	Position (X,Y)	Alt. (feet)	Maximum Detection Range (NM)	Maximum Range of Used Missile (NM)	Radar Missile Capacity	Number of Engaged Targets
HAWK1	(25,26)	1250	25	20	5	1
HAWK2	(37,58)	725	40	30	8	2
HAWK3	(132,62)	1550	40	30	8	2
NIKE	(85,87)	2587	25	87	10	1

C. SUMMARY STEPS OF CALCULATING THE ATTRITION RATE OF ATTACKING AIRCRAFT

In this particular part of chapter IX, a summary of the steps which are required in order to calculate the attrition rate of the attacking aircraft formations are described. The entire process is divided into two parts: preprocessing and dynamic simulation.

1. Preprocessing Phase

Step 1: Initialize the scenario. The user must specify a scenario similar to the scenario described above.

Step 2: Calculate the average terrain altitudes by using the instructions of Chapter II and the computer program "TERRAIN" given in Appendix A. An output of the Average Terrain Model, using the data of the scenario described above, is shown in Appendix G.

Step 3: Calculate the minimum detection altitudes for each radar site by using the instructions of Chapter III

and the computer program "MINALT" given in Appendix B. An output of the Minimum Altitudes Model, using the data of the scenario described above, is shown in Appendix G.

Step 4: Calculate the flight data of each aircraft formation by using the directions of Chapter V and the computer program "CPM" given in Appendix D. An output of the Flight Data Model, using the data of the scenario described above, is shown in Appendix G.

Step 5: Calculate the interception data by using the instructions of Chapter VI and the computer program "INTER" given in Appendix E. An output of the Interception Data Model, using the data of the scenario described above, is shown in Appendix G.

Step 6: Calculate the priority matrix by using the instructions of Chapter VI and the computer program "PRIORITY" given in Appendix E. An output of the Priority Matrix Model, using the data of the scenario described above, is shown in Appendix G.

2. Dynamic Phase

Step 7: Run the "AIRMODEL" program, using the instructions of chapter VIII and the computer program "AIRMODEL" given in Appendix F. An output of the "AIRMODEL" program, using the data of the scenario described above, is shown in Appendix G.

D. EXECUTING THE AIRMODEL

1. Database

This portion of Chapter IX describes and analyzes a complete simulation process following steps one through seven. The scenario which has been used to generate this output is described in the beginning of this chapter. The constant inputs of the computer program "MAIN", in the "AIRMODEL" computer workspace, are as follows:

a. seed = various seeds have been used

b. times = 50 times

c. NSITES= 4

d. DS2 = listed in Appendix G

e. IS2 = listed in Appendix G

f. TGT = 9 4 11

g. MKAP2 = 1 2 2 1

h. MCAP2 = 5 8 8 10

i. PKM =

5	20	25	0.5
5	25	30	0.55
5	25	30	0.55
10	70	85	0.4

j. IFFFOE= 1

k. ECM =

5	30	80	0.7	0.85
5	40	70	0.5	0.8
10	50	80	0.7	0.9

l. PR = listed in Appendix G.

m. AUTO = 12

n. LBR = 15%

p. TSTEP1=	1	2	3	2
	2	2	3	2
	1	2	3	2
	2	3	3	3

o. ETSF = 50%

The inputs which will be varied in the airmodel
are:

IFF

Probability that IFF works

Probability that IFF is correct given that it works

Command and Control Model

Radar Site Performance Model

Electronic countermeasure means model

2. Result

a. Base Line Situation

The airmodel has been executed with the following
various parameters:

IFF = Yes

Probability that IFF works = 0.98

Probability that IFF is correct, given that it
works = 0.96

Command and Control Model = Yes

Radar Operation = Normal

ECM = Effective

The setting of these parameters represents a
situation which is feasible during conflict operations. The

output of the airmodel is listed in Appendix G. The data analysis is as follows:

(1) Summary Statistics. Some summary AC

Attrition statistics are listed below. This data is result of replicating the simulation 50 times.

Statistics	Target 1	Target 2	Target 3
Number of Killed a/c (average)	0.64	0.46	2.2
Sample Variance	0.72	0.25	1.106
Minimum Value	0	0	0
Maximum Value	3	1	5
Range	3	1	5
Median	0	0	2
Low Quantile	0	0	1
Upper Quantile	1	1	3

(2) Distribution Fitting. The most appropriate

distribution for the attrition data of the three targets is the binomial with the following parameters:

Parameters	Target 1	Target 2	Target 3
n	9	4	11
p	0.058	0.115	0.24
X square	1.28	3.56	0.87

2

Since the critical value of X^2 ($\alpha = 0.05$) to reject the null hypothesis ($H_0: F(X) = \text{Binomial Distribution}$) is equal to 7.81 for two degrees of freedom, we accept that the distribution of the attrition rate data is binomial with the parameters shown above.

(3) Confidence Intervals for Probability of Kill.

Confidence intervals for the probability of kill are given below for α of 0.05.

Target	Probability Function	Confidence Interval	
		Low	Upper
Target 1	$P\{X=0\}=0.56$	0.42	0.69
	$P\{X=1\}=0.28$	0.15	0.40
	$P\{X=2\}=0.12$	0.02	0.21
	$P\{X=3\}=0.04$	0.0	0.09
Target 2	$P\{X=0\}=0.54$	0.4	0.67
	$P\{X=1\}=0.46$	0.32	0.59
Target 3	$P\{X=0\}=0.04$	0.0	0.09
	$P\{X=1\}=0.24$	0.12	0.35
	$P\{X=2\}=0.34$	0.208	0.47
	$P\{X=3\}=0.26$	0.13	0.38
	$P\{X=4\}=0.1$	0.01	0.18
	$P\{X=5\}=0.02$	0.0	0.05

b. Other Outputs

In this section, some other outputs of "AIRMODEL" are given. These outputs are a result of changing:

1. Probability that IFF works and probability that IFF is correct, given that it works.

2. Command and Control model.

3. Radar site operation model.

4. Electronic countermeasure means model.

(1) Changing the IFF probabilities. In this case, the "AIRMODEL" computer program uses the following input variables.

IFF = Yes

Probability that IFF works = 0.90

Probability that IFF is correct given that it works = 0.90

Command and Control Model = Yes

Radar Operation = Good

Electronic countermeasure means model = Yes

These inputs are the same as in the Base Line Situation, above, except the probabilities of IFF.

The means of the output of the target attrition rate data are:

# of A/C	Target 1	Target 2	Target 3	Probabilities
Mean of Attrition Rate	0.44	1.42	2.06	IFFWORK = 0.90
				IFFWORK = 0.90
	0.64	0.46	2.2	IFFWORK = 0.98
				IFFWORK = 0.96

This table shows that the number of attrited aircraft is less in both targets one and three because more enemy aircrafts pass without interception (recall that the IFF model assumes that if IFF does not work, the detected target is considered to be friend). On the other hand, the the number of destroyed aircraft of target two is greater because the IFF has a lower degree of reliability. Consequently, there are more fratricides. (Recall that target two is a friendly aircraft formation which is returning for a landing).

(2) Changing Command and Control Input. In this case, there is no command and control model applied. That means that the radar sites operate autonomously. The input variables of "AIRMODEL" are:

IFF = Yes

IFFWORK = 0.98

IFFCOR = 0.96

Command and Control Model = No

Radar Operation = Good

Electronic countermeasure means = Yes

These inputs are the same as in the Base Line Situation, except that the command and control model is not applied.

The table, below, shows that the number of destroyed aircraft is greater when command and control is not applied. This result is a surprise because the opposite was expected.

The means of the output of target attrition are given below:

# of A/F	Target 1	Target 2	Target 3	Command and Control model
Attrition Rate	1.08	1.1	2.36	not applied
	0.64	0.46	2.2	applied

However, the result came about because the scenario has only three targets and four radar sites. When one target formation was engaged by radar site one, radar site two was not allowed to engage this target time (IDLE). Therefore, the formation was intercepted only by radar site one and it suffered less attrition. On the other hand, when command and control is not applied, the same target formation is intercepted by more than one radar site and it suffers more attrition (both radar sites are active). This phenomenon would not happen if the scenario had more targets.

(3) Changing the radar site operation model. In this case, the operation of all the radar sites is degraded. The variable inputs of "AIRMODEL" are:

IFF = Yes

IFFWORK = 0.98

IFFCOR = 0.96

Command and Control model = Yes

Radar Operation = degraded

Electronic countermeasure means = Yes

These inputs are the same as in the Base Line Situation, above, except that all radar operations are degraded.

The means of the output of target attrition rate data are shown below:

# of A/C	Target 1	Target 2	Target 3	Radar Operation
Attrition Rate	0.60	0.41	1.42	Degraded
	0.64	0.46	2.2	Good

The table shows that the number of destroyed aircraft for all three targets is less, as it is expected, when the radar sites work in a degraded mode. This attrition rate has been reduced almost 40%. in the case of Table 3.

(4) Changing the electronic countermeasure means model. In this case, the electronic countermeasure means model (ECM) is not applied. That means that no target formation uses ECM.

The variable inputs of "AIRMODEL" are:

IFF = Yes

IFFWORK = 0.98

IFFCOR = 0.96

Command and Control Model = Yes

Radar Operation = Good

Electronic countermeasure means model = No

These inputs are the same as the Base Line Situation, above, except that the electronic countermeasure means model is not applied.

The means of the output of target attrition rate data is shown below:

# of A/C	Target 1	Target 2	Target 3	ECM Model
Attrition Rate	0.76	0.93	4.06	not applied
	0.64	0.46	2.2	applied

The table shows that the number of destroyed aircraft is greater when the targets do not use electronic countermeasure means to protect themselves. The increase of number of the destroyed aircraft when ECM is not applied, is approximately 100%.

3. Sensitivity Analysis

By using the scenario described above, sensitivity analysis can be performed by changing some of the aircraft movement data. For example, by changing the routes that the aircraft formation use, one can see how the attrition rate will be changed. Other parameters that can be changed for sensitivity analysis are the flight altitude and the speed of the aircraft formation.

In this section, sensitivity analysis is performed by changing the flight altitude of the aircraft formations. A change in the flight altitude was performed to study the effects of terrain masking on aircraft attrition rate.

To perform this sensitivity analysis, five different aircraft flight levels were used (500, 1000, 2000, 5000 and 10000 feet). The outputs of the "AIRMODEL", using these five different flight level data, are listed in Appendix G.

The number of destroyed aircraft for each different flight level are given below:

Flight Level	Target 1	Target 2	Target 3	Total
500	0.83	0.13	0.77	1.73
1000	0.64	0.46	2.20	3.30
2000	0.82	0.62	2.25	3.69
5000	0.94	0.65	2.16	3.75
10000	0.96	0.66	2.20	3.82

The table shows the increase in the number of destroyed aircraft as the flight level increases.

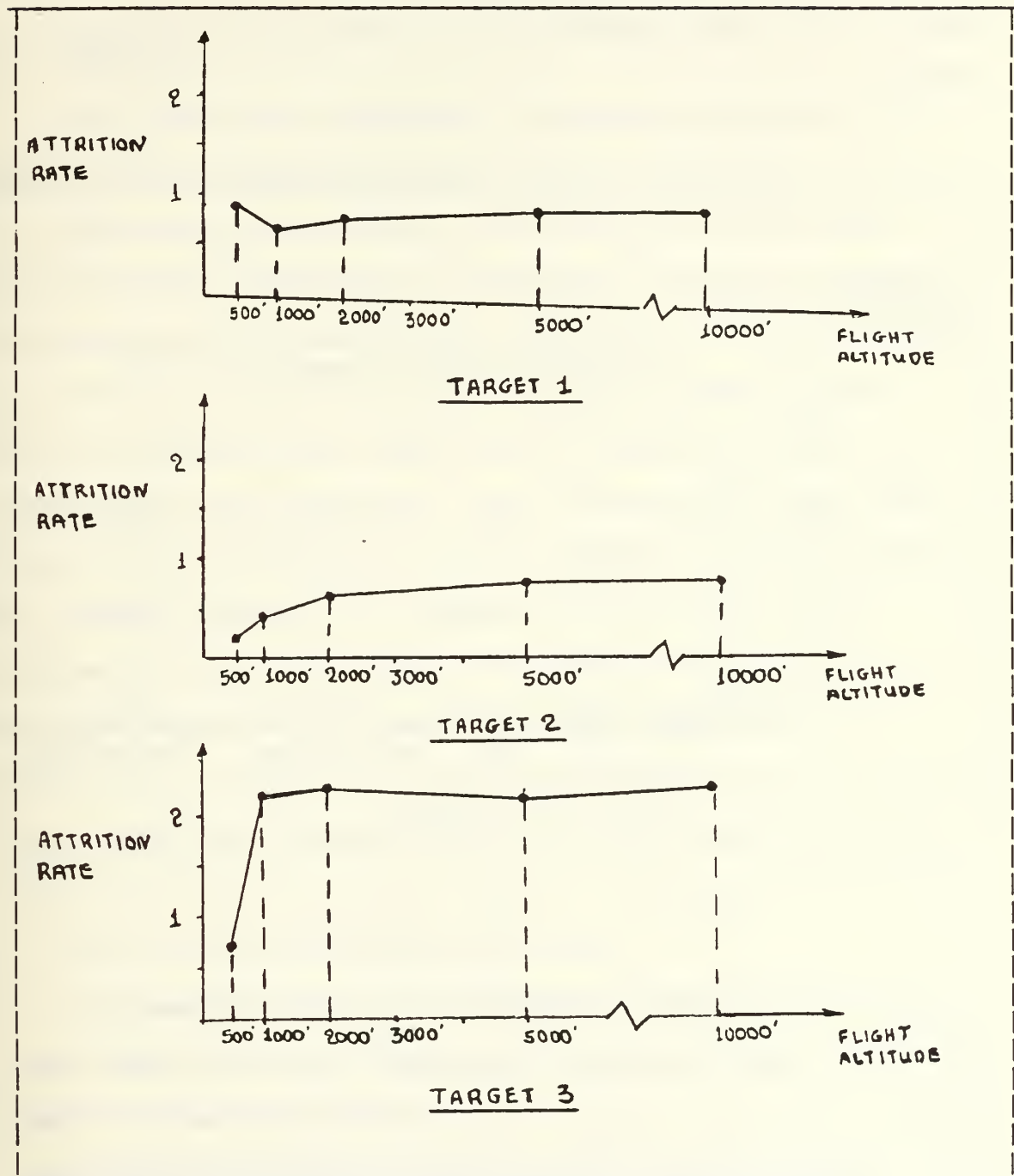


Figure 9.2 Attrition Rate of Each Target

Figure 9.2 above, shows the change in attrition rate of aircraft as a function of the flight level for each target.

Figure 9.3 below, shows the change in the total attrition rate of the three formations as a function of the flight level.

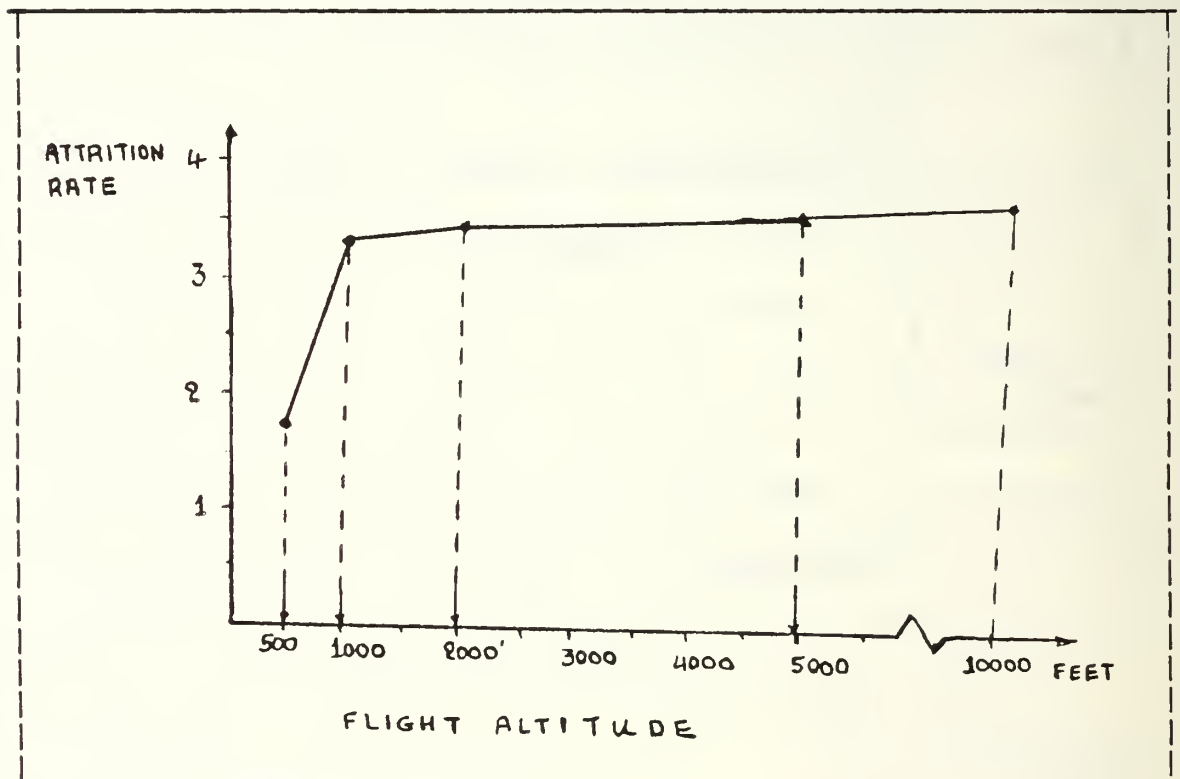


Figure 9.3 Total Attrition Rate

It is worth while considering that the increase in attrition rate, especially for target three, is very large when the formation changes altitude from 500 feet to 1000 feet. However, the attrition rate is essentially constant for altitudes above 2000 feet.

X. SUMMARY AND CONCLUSION

A. SUMMARY

This thesis has presented a high resolution model to analyze the air attack/defense combat situation.

The simulation has made efficient use of off-line, pre-processing submodels and programs in order to compute the deterministic phase of the engagement. By pre-flying the aircraft through the entire scenario, most of the detailed calculations involving the geometry of the air engagement were performed. These calculations were used to determine if detection, tracking, firing, and interception are feasible during all segments of the flight. The information was summarized and stored in the form of matrices whose only elements are zero and one. As a result, the deterministic elements of the air battle were transformed into look-up table for each time step of the simulation.

The pre-processing phase included:

1. Generating the terrain models (Chapters II and III)
2. Modeling the flight paths of all aircraft contained in the simulation(Chapter V)
3. Completing detection, tracking, firing and interception calculations (Chapters IV through VI).

4. Modeling for the effects of IFF, degraded equipment, ECM, target selection priorities, and command and control (Chapter VII).

The results of the pre-processing calculations were input into the dynamic simulation phase of the model. The stochastic portions of the air attack/defense encounter were replicated and summary statistics were gathered and analyzed. A sensitivity analysis was performed to demonstrate the relationship between aircraft altitude and attrition rate. (Chapter VIII and IX)

B. CONCLUSION

The technique of separating the deterministic and stochastic elements of the air battle proved to be very efficient. Using an IBM PC, it required approximately 25 minutes to pre-fly the aircraft and summarize the geometry of the air battle in matrix format. The stochastic portion of the air battle required approximately 8 minutes of executing time. Although these run times are scenario dependent, the three-to-one ratio is a reasonable approximation to the apportionment of time required for both phases of the simulation. Replicating the entire simulation 50 times, without a pre-processing oriented model, would require 1650 minutes of IBM PC time. Using the pre-processing approach, the time required for the same 50 replications is 425 minutes. This represents a savings of approximately 75%.

The submodels developed in this thesis can be used in several ways.

1. The attacker can use the pre-processing models to design flight paths which minimize detection and take more advantage of terrain masking.

2. The attacker can perform trade-off analyses between different approach altitudes. For a given flight path, the attacker can determine the highest altitude which will offer deception and cover and allow for efficient fuel consumption.

3. The attacker can better determine the missile sites which offer the greatest threat of attrition. Air assets can then be allocated to attack these sites and degrade their capability.

4. The defender can use the pre-processing models to improve the positioning of air defense sites, given the likely axis of advance by attacking aircraft.

AIRMODEL allows the analyst to investigate a wide range of aircraft attack/defense problems. The simulation can be efficiently replicated without re-calculating the deterministic phases of the engagement. Consequently, a more realistic and accurate perspective of the encounter can be achieved.

Further research and analyses can be directed towards developing the stochasting sub-models necessary to simulate the engagment sequence. This author has developed a general approach which is efficient and realistic.

Acquisition, tracking, and firing time delays require more study and model design. The user is invited to employ this modeling architecture as a specific framework for model building. The entire simulation model is modular. Therefore, the user can modify the sub models to suit specific design requirement and level of fidelity.

APPENDIX A

A. PURPOSE

This program is used to calculate:

1. The average altitudes for each grid square.
2. To construct a matrix named ATERRAIN whose entries are the average altitudes for grid squares.

B. DESCRIPTION OF THE TERRAIN SIMULATION PROGRAM

The header of the terrain program is "TERRAIN".

1. Input

The "TERRAIN" program prompts one input:

A matrix A whose entries are the altitudes of each grid square. How these numbers are extracted is described in section one. Matrix A does not need to be square. The number of rows is the result of the division of the length of X range by the length of the side of the square grid. For example if the length of the terrain is 60 NM and the length of the side of the grid square is 6 NM, the number of rows of the matrix will be equal to 10. The number of columns is calculated in the same way.

2. Output

The "TERRAIN" program calculates a matrix whose entries are the average heights of grid squares such as shown previously in Table 2.

```

▽ TERRAIN:B;C;I;A
[1]  A
[2]  A THIS FUNCTION CALCULATE THE AVERAGE OF THE HIGHTS OF THE GIVEN TERAİN
[3]  A----- INPUT DESCRIPTION-----+
[4]  A THE REQUARED INPUT IS A MATRIX WHOSE ENTRIES ARE THE ALTITUDE
[5]  A OF THE FOUR CORNERS OF EACH SQUARE GRID
[6]  A
[7]  A-----OUTPUT DESCRIPTION-----+
[8]  A THE OUTPUT IS A MATRIX WHOSE ENTRIES ARE THE AVERAGE ALTITUDE
[9]  A OF THE SQUARE GRID
[10] A-----+
[11] A-----MAIN PROGRAM-----+
[12] I←0
[13] P5: 'ENTER THE MATRIX OF THE SQUARE GRIND ALTITUDE'
[14] A←0 ◊ →((+/(pA))<2)/P3 ◊ →P4
[15] P3: 'THE INPUT IS NOT A MATRIX)' ◊ →P5
[16] A-----CREATE THE MATRICES-----+
[17] P4:B←((pA[;1])-1),(pA[1;])-1))p0 ◊ C←((pA[;1])-1),(pA[1;])-1))p0
[18] L1:I←I+1 ◊ →(I≥(p(A[;1])))/L2
[19] B[I;J]←A[I;J]+A[(I+1);J]
[20] →L1
[21] L2:I←0
[22] L3:I←I+1 ◊ →(I≥(p(B[;1])))/L5
[23] C[I;J]←(B[I;J]+B[(I+1);J])÷4
[24] →L3
[25] L5:AHEIGHTS←C
[26] ' THE MATRIX 'AHEIGHTS ''
[27] '-----'
[28] AHEIGHTS
[29]
▽

```

APPENDIX B

This appendix describes the workspace called "MINALT" (MINimum ALTitudes). This workspace contains two functions called "MALTI" and "GRID".

A. FUNCTION "MALTI"

HEADER : The header of the function "MALTI" is MALTI.

PURPOSE: This function calculates the minimum altitude where a given radar site can "see" a target due to terrain masking and to limitation of the maximum range.

INPUT: The function "MALTI" prompts four inputs:

1. A three element vector which contains the position and the altitude of the radar site.
 - (a) X,Y coordinates in square grid position.
For example, if the radar site is located in square grid (7,3) then first two elements are 7 3.
 - (b) Radar site altitude (in feet). Thus the completed input is 7 3 1000
2. The maximum range of the radar site in NM
3. A (N,M) matrix containings the average altitudes of the grid squares calculated by the program "TERRAIN" described in Appendix A of Chapter 2.
4. A scale factor, describing the size of the

grid squares desired. Its measurement is in Nautical Miles (N.M).

OUTPUT: The output is a (N M) matrix whose entries are the minimum altitudes above which a given radar site can detect a target.

B. FUNCTION "GRID"

HEADER : The header of the function "GRID" is SITE GRID CORD.

PURPOSE: This function finds the grid squares which exist between the radar site and the target grid square. For example, if the radar site is located in grid square (2,1) - see Figure 3.1 in Chapter 3 - and the target square is (4,4), then the intermediate grid squares given by the function "GRID" are (2,2), (3,2) and (3,3). This function supports the previous function "MALTI" but it can be run separately, as well.

INPUT: The function "GRID" prompts two inputs:

1. A three element vector which contains the coordinations of the radar site X, Y and its altitude. This vector is the left argument of the function's header (SITE).
2. The coordinations of the target square grid X,Y. this input is the right argument of the function's header (CORD).

OUTPUT: The output of this program is a (2 N) matrix whose columns are the coordinates of the square

grids which lay between the radar site and the target square grid.

```

▽ GR=SITE GRID CORD:I:A;XX1:XX2:A1:X1;X2:XX:YY;Y1;Y2;F;VEC:X;Y;R
[1]  A
[2]  A===== PURPOSE =====+
[3]  A THIS FUNCTION IS USED TO FIND THE SQUARE GRIDS WHICH ARE
[4]  A BETWEEN THE RADAR SITE AND THE SQUARE TARGET GRID.
[5]  A
[6]  A===== INPUT =====+
[7]  A 1. THE CORDINATIONS OF THE RADAR SITE: X,Y AND ALTITUDE (IN FEET)
[8]  A 2. THE CORDINATIONS OF THE SQUARE TARGET GRID: X,Y .
[9]  A
[10] A===== OUTPUT =====+
[11] A A (2 N) MATRIX WHOSE COLUMNS ARE THE CORDINATES OF THE SQUARE
[12] A GRIDS WHICH LAY BETWEEN THE RADAR SITE AND THE SQUARE
[13] A TARGET GRID.
[14] A===== MAIN PROGRAM =====+
[15] I=1
[16] X1=SITE[1]-0.5 ♦ X2=CORD[1]-0.5
[17] Y1=SITE[2]-0.5 ♦ Y2=CORD[2]-0.5
[18] A-----THE DISTANCE -----+
[19] R=((X2-X1)*2)+((Y2-Y1)*2)*0.5
[20] A-----THE VECTOR -----+
[21] VEC=((X2-X1)*5)/5
[22] X=X2-X1
[23] X2=X2+0.1
[24] L13=F-(X2)*((Y2-Y1)/(X2-X1))
[25] A----- X Y CALCULATION -----+
[26] X=(2*F)*VEC ♦ Y=(1*F)*VEC
[27] X=((X2-X1)>0),(Y2-Y1)<0)/L3,L3
[28] XX=X1-X ♦ YY=Y1-Y ♦ →L6
[29] L3=((Y2-Y1)<0)/L5
[30] YY=Y1+Y ♦ XX=X1+X ♦ →L6
[31] L5=YY-Y1-Y ♦ XX=X1-X
[32] X=((X2-X1)<0),(Y2-Y1)>0)/L6,L6
[33] YY=Y1+Y ♦ XX=X1+X
[34] L6=A+(2,(pVEC))*pXX,YY
[35] X=((pA[1;])>0)/RR10
[36] GR= 2 1 pL(SITE[1],SITE[2]) ♦ →LLL2
[37] RR10:A1-A[1;]
[38] A-- REJECT THE CASE WHEN THE GRID[I] IS = GRID[I+1] -----+
[39] L2=((A[1;I])=(A[1;I+1]))/L1
[40] →L12
[41] L1=((A[2;I])=(A[2;I+1]))/L11
[42] L12:A1-A1,A[1;I+1]
[43] L11:I-I+1
[44] X=((I<(pVEC))/L2 ♦ GR=0((pA1)/2),2)*pA1
[45] XX1=GR[1;]
[46] XX2=GR[2;]
[47] A-- REJECT THE CASE WHEN THE GRID IS THE SAME WITH THE SITE -----+
[48] X=((1+XX1)*(LSITE[1]))/LL5
[49] X=((1+XX2)*(LSITE[2]))/LL5
[50] XX1=1+XX1 ♦ XX2=1+XX2 ♦ GR=(2,(pXX1))*pXX1,XX2
[51] A-- REJECT IF THE CORDINATIONS ARE ZERO-----+
[52] LLS=((1+XX1)=0)/LLL3
[53] X=((1+XX2)=0)/LLL3
[54] →LLL2
[55] LLL3:XX1-1+XX1 ♦ XX2-1+XX2
[56] GR=(2,(pXX1))*p(XX1,XX2)
[57] LLL2:GR=GR,CORD

```



```

[68] 7 MALT1;COS1;COS2;SIN1;SIN2;L;P;A1;G;GR;D1;D2;GGR;GO;GRM;H;I;J;K;R;SC
ALE;ALT1;ALT2;CORD;D3;NM;TH;TH1;TH2;TH3;TH4;TH5;SSITE
[1] A
[2] A===== PURPOSE =====+
[3] A THIS FUNCTION CALCULATE THE MINIMUM ALTITUDE THAT A THE GIVEN
[4] A RADAR SITE CAN SEE A TARGET DUE TO MAXIMUM RANGE AND TO TERRAIN
[5] A MASKING
[6] A
[7] A===== INPUT =====+
[8] A 1. A THREE ELEMENT VECTOR FOR THE RADAR SITE POSITION
[9] A (A). X Y COORDINATES IN SQUARE GRID POSITION
[10] A (B). RADAR SITE ALTITUDE (IN FEET)
[11] A
[12] A 2. THE MAXIMUM RANGE OF THE RADAR SITE IN N.M
[13] A
[14] A 3. A (N M) MATRIX WITH THE AVERAGE ALTITUDES (GIVEN BY THE TERRAIN
[15] A SIMULATION)
[16] A
[17] A 3. THE SCALE FACTOR (THE LENGTH OF THE SQUARE GRIDS) IN N.M
[18] A
[19] A===== OUTPUT =====+
[20] A THE OUTPUT IS A (N M) MATRIX WITH THE MINIMUM ALTITUDES
[21] A ABOVE OF WHICH A GIVEN RADAR SITE CAN SEE A TARGET
[22] A
[23] A===== MAIN PROGRAM =====+
[24] A
[25] T2: 'ENTER THE SITE DATA (X,Y,ALTITUDE)'
[26] SITE=0 0 SSITE=((-((2+SITE)+6)), -1+SITE 0 SITE 0 SSITE
[27] +((PSSITE)=3)/T1
[28] 'THE VECTOR IS NOT CORRECT !!! TRY AGAIN' 0 ->T2 0 '
[29] '
[30] T1: 'ENTER THE MAXIMUM RANGE OF THE RADAR SITE (IN N.M)'
[31] RANGE=0
[32] '
[33] T4: 'ENTER THE AHEIGHTS MATRIX'
[34] H=0
[35] +((PH)+1)/T3
[36] 'THE MATRIX DOES NOT HAVE CORRECT DIMENTIONS TRY AGAIN' 0 ->T4
[37] '
[38] T3: 'ENTER THE SCALE FACTOR'
[39] SCALE=0
[40] J=1 0 H1=-(PH)P0
[41] PP4: I=1
[42] PP3: CORD=(I),(J) 0 K=1 A0 'I,J = ',3I,J
[43] GO=(((I*SCALE)-(SCALE+2)),((J*SCALE)-(SCALE+2))) A0 'GO=',3GO
[44] R=3455 0 NM=6067 0 ASITE=(((LSSITE[1,2]*SCALE))-(SCALE+2)),SSITE[3]
[45] L=(((GO[1]-SITE[1])*2)+((GO[2]-SITE[2])*2))*0.5
[46] +((L+RANGE)/T4
[47] H1[I;J]=-1 0 -END
[48] A-----+
[49] A FIND THE GRID BETWEEN THE RADAR SITE AND THE TARGET GRID
[50] T4: GR=SSITE GRID CORD
[51] A-----+
[52] GR=0GR 0 GRM=-(P(GR[1;1]))P0 A0 GR
[53] PP1: GGR=GR[K]
[54] G=(((GGR[K]*SCALE))-(SCALE+2)),H((GGR[1]):(GGR[2])) A0 'G=',3G
[55] A-----+
[56] A CALCULATION OF THE DISTANCE (CURVE)
[57] D1=(((GO[1]-SITE[1])*2)+((GO[2]-SITE[2])*2))*0.5 A0 ' D1= ',3D1
[58] D2=(((GO[1]-SITE[1])*2)+((GO[2]-SITE[2])*2))*0.5 A0 ' D2= ',3D2
[59] A-----+
[60] A CALCULATE THE ANGLES
[61] TH1=D1/R 0 TH2=D2/R 0 TH=TH1+TH2 A0 TH1,TH2,TH
[62] ALT1=R+(SITE[3]+NM) 0 ALT2=R+(G[3]+NM) A0 ALT1,ALT2
[63] COS1=2*TH1 0 COS2=2*TH2 A0 COS1,COS2
[64] A-----+
[65] A CALCULATION OF THE ACTUAL DISTANCE
[66] D1=3455*((2*(1-COS1))*0.5) A0 'DD1=',3D1
[67] D2=3455*((2*(1-COS2))*0.5) A0 'DD2=',3D2

```

```

[68]  $\rightarrow (D2 \neq 0) / TT2$ 
[69]  $A1 \leftarrow 10 \diamond \rightarrow TT1$ 
[70]  $TT2: D3 \leftarrow (((ALT1 \times 2) + (ALT2 \times 2)) - (2 \times ALT1 \times ALT2 \times \cos 1)) \times 0.5$   $\text{A} \diamond 'D3 = ', \&D3$ 
[71]  $TH3 \leftarrow (((D3 \times 2) + (ALT1 \times 2)) - (ALT2 \times 2)) \div (2 \times D3 \times ALT1)$   $\text{A} \diamond 'TH3 = ', \&TH3$ 
[72]  $TH4 \leftarrow 2 \times TH3$   $\text{A} \diamond 'TH4 = ', \&TH4$ 
[73]  $TH5 \leftarrow (91) - (TH4 + TH2)$   $\text{A} \diamond 'TH5 = ', \&TH5$ 
[74]  $SIN1 \leftarrow 1 \times TH5 \diamond SIN2 \leftarrow 1 \times TH4$   $\text{A} \diamond SIN1, SIN2$ 
[75]  $A1 \leftarrow (((SIN2 \times ALT1) \div SIN1) - R) \times (NM)$   $\text{A} \diamond 'AA1 = ', \&A1$ 
[76]  $\text{A} \leftarrow$ -----+
[77]  $TT1: GRM[K] \leftarrow A1$   $\text{A} \diamond A1$ 
[78]  $K \leftarrow K + 1 \diamond \rightarrow (K > (\rho GR[1; 1])) / PP2$ 
[79]  $\rightarrow PP1$ 
[80]  $\text{A} \leftarrow$ -----+
[81]  $\text{A TAKE THE LARGEST ALTITUDE}$ 
[82]  $PP2: H1[I; J] \leftarrow 1 \uparrow (GRM[\uparrow GRM])$   $\text{A} \diamond 'FIN ALT = ', \&H1[I; J]$ 
[83]  $\text{A} \leftarrow$ -----'
[84]  $END: I \leftarrow I + 1$ 
[85]  $\rightarrow (IS(\rho H[; 1])) / PP3$ 
[86]  $J \leftarrow J + 1$ 
[87]  $\rightarrow (JS(\rho H[1; ])) / PP4 \diamond H1[(SSITE[1]); (SSITE[2])] \leftarrow 10$ 
[88]  $'$  THE SMALLEST ALTITUDE ARE'
[89]  $'$ -----'
[90]  $H1 \leftarrow H1$ 
[91]  $'$ 
[92]  $'$ 
[93]  $'NOTE'$ 
[94]  $'-----'$ 
[95]  $'$ 
[96]  $'$  +-----+
[97]  $'$  THE OUTPUT IS STORED UNDER THE VARIABLE H1'
[98]  $'$  +-----+

```

▽

APPENDIX C

Appendix C describes the computer function named "CONTOUR".

HEADER : The header of the function CONTOUR is "CONTOUR"

PURPOSE: This function calculates if a given radar site can detect a target flying at a given altitude level for all the square grids which are located inside the radar site maximum distance.

INPUT : The computer function "CONTOUR" prompts three inputs:

1. A (N M) matrix given by the terrain simulation functions "TERRAIN" described in Appendix A.
2. The altitude of the target (in feet).
3. A (N M) matrix given by the minimum altitude simulation function "MALTI", described in Appendix B.

OUTPUT : The output is a (N M) matrix the entries of which are -10, -1, 0 and 1. The meaning of these numbers are as follows:

-10 = Position of radar site.

-1 = Radar site can not detect the target because it flies out of the radar maximum range.

0 = Radar site can not detect the target

because there is no line-of-sight, and
 1 = Radar site can detect the target.

The output matrix is stored under the variable CON.

```

▽ CONTOUR;ALT1;ALT2;ALT3;ALT4;I;J;H
[1]  A
[2]  A===== PERPOSE =====+
[3]  A THIS FUNCTION CALCULATE A TABLE WHICH ILLUSTRATE IF A
[4]  A A PARTICULER RADAR SITE CAN SEE THE TARGET OR NOT.
[5]  A
[6]  A===== INPUT =====+
[7]  A 1. A (N M) MATRIX OF TERRAIN ALTITUDE(FROM TERRAIN SIMULATION)
[8]  A 2. THE ALTITUDE OF THE TARGET
[9]  A 3. A (N M) MATRIX OF RADAR SITE MINIMUM ALTITUDE
[10] A
[11] A===== OUTPUT =====+
[12] A A (N M) MATRIX WITH ELEMENT OF -10 -1 0 AND 1.
[13] A
[14] A -10 = RADAR SITE POSITION
[15] A -1 = RADAR SITE CAN NOT SEE THE TARGET BECAUSE OF THE MAX. RANGE
[16] A 0 = RADAR CAN NOT SEE THE TARGET BECAUSE OF LINE-OF-SIGHT
[17] A 1 = RADAR CAN SEE THE TARGET
[18] A
[19] A===== MAIN PROGRAM =====+
[20] 'ENTER THE TARGET ALTITUDE (IN FEET)'
[21] H=0 ◊ H
[22] A H=1000
[23] 'ENTER THE MATRIX OF THE AVERAGE TERRAIN ALTITUDES'
[24] ALT1=0 A◊ ALT1
[25] AALT1=MM
[26] 'ENTER THE MATRIX OF THE MINIMUM ALTITUDES OF THE RADAR SITE'
[27] ALT2=0 A◊ ALT2
[28] A ALT2=H2
[29] I=J+1 ◊ CON+((PALT1(I;1)),(PALT1(1;J)))P0
[30] L3:I+1
[31] L2:ALT3=ALT1(I;J)+H A◊ 'ALT1+H =',SALT3 ◊ I,J
[32] ALT4=ALT2(I;J) A◊ 'ALTSITE=',SALT4
[33] →((ALT2(I;J))*-10)/L7
[34] CON(I;J)=-10 ◊ →L4
[35] L7:-(ALT4*-1)/L1
[36] CON(I;J)=-1 ◊ →L4
[37] L1:-(ALT4SALT3)/L6
[38] CON(I;J)=0 ◊ →L4
[39] L6:CON(I;J)+1
[40] L4:I-I+1
[41] →(IS(PALT1(I;1)))/L2
[42] J=J+1
[43] →(JS(PALT1(1;J)))/L3
[44] ' THE OUTPUT IS:'
[45] ' -----'
[46] ''
[47] CON
[48] 'THE OUTPUT IS STORED UNDER THE VARIABLE CON'
▽

```

APPENDIX D

Appendix D describes the computer function named "MOVEMENT" and it has two functions: CPM and ERROR.

A. CPM

HEADER : The header of the function CPM is "CPM".

PURPOSE: This function calculates the time steps, the position, the altitude over this position and the direction of all flight legs of all aircraft for each time step.

INPUTS : The computer function "MOVEMENT" prompts the following inputs:

1. Time Step: The time of the time step of model (in seconds) i.e. if the calculation has to be done every 10 seconds, the input for time step must be 10.
2. Scale: The scale used for the terrain simulation, i.e. the length of the side of the terrain square grid.
3. Alt. Data: The average altitudes given by the terrain model (in feet).
4. X0, Y0, T0: Coordinates and time for the beginning of the flight path (in NM for coordinates and minutes for time).
5. Dir: The direction of the flight path of the aircraft (in degrees).

6. Length: The length of the flight leg of the aircraft (in NM).
7. Speed: The speed of the aircraft along the flight path (in NM).
8. Alt: The altitude of the aircraft along the flight path (in feet).

OUTPUT : The output is a (5,N) matrix whose elements are as follows:

1. First Row: Time steps of the air combat model.
2. Second and Third Row: The Cartesian coordinates of the position of all aircraft for all time steps.
3. Fourth Row: The altitude
4. Fifth Row: The course of each flight leg.
5. N: The number of the time steps.

The output is stored under the variable A1.

B. ERROR

This function is used in all the models and informs the user about a wrong input.

```

      ▽ CPM;DPTI;TSPGD;ALT;DATA;DIR;DISTANCE;I;Q1;Q2;SCALE;SPEED;TI;X;X1;Y1;X0;XYA
;Y0;Y;T0;T1;V;V1;V2;T1;Z;Z1;VECTOR;XYT;FDATA1
[1]  A
[2]  A----- PURPOSE -----+
[3]  A
[4]  A   THE PURPOSE OF THIS PROGRAM IS TO CALCULATE THE TIME STEPS,
[5]  A   POSITION(X,Y), THE ALTITUDE OF THE A/C FOR THE PENETRATION
[6]  A   ROUTE ACROSS THE HOSTILE AREA, THE COURSE AND THE SPEED FOR
[7]  A   EACH FLIGHT LEG FOR ALL THE TIME STEPS.
[8]  A

```



```

[91] A----- INPUT -----+
[101] A
[111] A 1. TIME STEP = THE TIME OF THE TIME-STEP MODEL YOU LIKE (IN SECOND)
[121] A I.E IF YOU LIKE THE CALCULATION TO BE DONE EVERY
[131] A 10 SECOND ENTER FOR TIME STEP: 10
[141] A
[151] A 2. SCALE = THE SCALE USED FOR THE TERRAIN SIMULATION. I.E THE
[161] A LENGTH OF THE SIDE OF THE TERRAIN SQUARE GRID.
[171] A (IN N.M)
[181] A
[191] A 3. ALT.DATA = THE AVERAGE ALTITUDES GIVEN BY THE TERRAIN
[201] A MODEL. (IN FEET)
[211] A
[221] A 4. X0,Y0,T0 = COORDINATES AND TIME FOR THE FLIGHT PATH BEGGINING.
[231] A ( IN N.M FOR COORDINATES AND IN MINUTES FOR TIME)
[241] A
[251] A 5. DIR = THE DIRECTION OF THE FLIGHT PATH (IN DEGREE).
[261] A
[271] A 6. LENGTH = THE LENGTH OF THE FLIGHT PATH (IN N.N).
[281] A
[291] A 7. SPEED = THE SPEED OF THE A/C ACROSS THE FLIGHT PATH (IN N.M)
[301] A
[311] A 8. ALT. = THE ALTITUDE OF THE A/C ACROSS THE FLIGHT PATH
[321] A (IN FEET)
[331] A
[341] A----- OUTPUT -----+
[351] A
[361] A THE OUTPUT IS A (4 N) MATRIX WHOSE ROWS AND N ARE AS FOLLOWS:
[371] A
[381] A 1. THE FIRST ROW IS THE TIME STEPS
[391] A 2. THE SECOND AND THE THIRD ROWS ARE THE A/C POSITION
[401] A IN X,Y COORDINATES,
[411] A 3. THE FOURTH ROW IS THE A/C ALTITUDE ACROSS THE FLIGHT PATH
[421] A 4. THE FIFTH ROW IS THE HEADING OF THE FLIGHT PATH
[431] A 5. THE SIXTH ROW IS THE SPEED OF A/C FOR EACH FLIGHT LEG.
[441] A
[451] A----- OUTPUT FOR CHECK -----+
[461] A FLIGHT DATA ARE STORED UNDER THE VARIABLE FDATA
[471] A AS FOLLOWS:
[481] A FIRST ROW = DIRECTION FOR EACH FLIGHT SEGMENT
[491] A SECOND ROW = LENGTH OF EACH FLIGHT SEGMENT
[501] A THIRD ROW = SPEED OF A/C FOR EACH FLIGHT SEGMENT
[511] A FOURTH ROW = ALTITUDES OF A/C FOR EACH FLIGHT SEGMENT
[521] A
[531] A----- PROGRAM -----+
[541] A
[551] V2=0 : A1= 6 0 p0 : FDATA1= 4 1 p0 : FDATA= 4 0 p0
[561] A----- ENTER DATA -----+
[571] 'ENTER THE TIME STEP (IN SECOND)'
[581] TI=0 :
[591] 'ENTER THE AVERAGE ALTITUDES FROM TERRAIN SIMULATION (TDATA)'
[601] DATA=0 :
[611] 'ENTER THE SCALE OF THE TERRAIN SIMULATION GRID (IN N.M)'
[621] SCALE=0 :
[631] L3:----- ENTER FLIGHT DATA -----
[641]
[651] L7: IF THE FLIGHT PATH IS A NEW ONE ENTER 0
[661] IF THE FLIGHT PATH CONTINIOUS ENTER 1
[671] Q1=0
[681] -((Q1=0),(Q1=1),(Q1=1))/L3,L6,L5
[691] L3: 'ENTER ( X0,Y0,T0 )'
[701] XYT=0
[711] -((pXYT)=3)/L12
[721] ERROR : -L3
[731] L12: X0=XYT[1] : Y0=XYT[2] : T0=XYT[3] : T1=(T0*60)/TI
[741] Z1=(6,(p,T1))p0 : Z1[1:1]=(V2+(L1T1)) : V2=T1+V2 : -L15
[751] -L6 :
[761] L5: ERROR : : -L7
[771] L6: : : Z1= 6 0 p0

```

```

[78] L15: 'ENTER THE DIRECTION OF THE FLIGHT PATH (IN DEGREE)'
[79] DIR=0 * ' ' * FDATA1[1;]←DIR
[80] →(DIR÷360)/L20
[81] ERROR * →L15
[82] L20: 'ENTER THE LENGTH OF THE LEG OF THE FLIGHT PATH (IN N.M.)'
[83] DISTANCE=0 * ' ' * FDATA1[2;]←DISTANCE
[84] L21: 'ENTER THE SPEED OF A/C (IN KNOTS)'
[85] SPEED=0 * ' ' * FDATA1[3;]←SPEED
[86] 'ENTER THE FLIGHT ALTITUDE OF A/C (IN FEET)'
[87] ALT=0 * ' ' * FDATA1[4;]←ALT * FDATA=FDATA,FDATA1
[88] A-----+
[89] DPTI=(SPEED÷3600)*TI A (DISTANCE PER TIME INCREMENT)
[90] TSPGD=DISTANCE÷DPTI A (TIME STEPS PER GIVEN DISTANCE)
[91] VECTOR=(√(LTSPGD))*DPTI APER TIME INCREMENT)
[92] V=V2+√(L(1+VECTOR)) * V1=V * V←1+V
[93] A-----+
[94] A FIND X AND Y COORDINATES
[95] A-----+
[96] X=X0+VECTOR*(1÷((01)÷180)*DIR)) A * FX
[97] Y=Y0+VECTOR*(2÷((01)÷180)*DIR)) A * FY
[98] X1=(X÷SCALE) A * X1=CORD.IN GRID
[99] Y1=(Y÷SCALE) A * Y1=CORD.IN GRID
[100] A-----+
[101] A CREATE THE TIME-POSITION-ALTITUDE-DIRECTION-SPEED MATRIX
[102] A-----+
[103] A A1=(6,(T1))p0 * A1[1;]←T1
[104] I←1 * XYA=(6,(PX1))p0
[105] L1:XYA[;I]←(LV1[I]),(FX[I]),(FY[I]),(DATA[X1[I];Y1[I]]+ALT),DIR,SPEED
[106] I←I+1
[107] →(IS(PX1))/L1
[108] A1=A1,Z1,XYA * X0←1+X * Y0←1+Y * V2←1+(A1[1;])
[109] L10: 'IF YOU LIKE TO CONTINUE ENTER' 0
[110] ' OTHERWISE ENTER' 1
[111] Q2=0
[112] →((Q2=0),(Q2=1),(Q2>1))/L2,L8,L9
[113] L9: 'WRONG ENTRY... TRY AGAIN' * →L10
[114] L8:
[115] A →(T0=0)/L11
[116] A A1← 0 1 →A1
[117] ' ' * A1 * ' ' * ' '
[118] '
[119] ' THE OUTPUT IS STORED UNDER THE VARIABLE A1'
[120] '

```

▽

APPENDIX E

The purpose of this Appendix is to describe the work spaces of the "TARGET DETECTION", "TARGET INTERCEPTION", and "PRIORITY" models.

A. TARGET DETECTION MODEL

The TARGET DETECTION work space is called "FDETECT" and it consists of two functions: DETECT and ERROR.

1. Detect

PURPOSE: The purpose of the function "DETECT" is to find out if a particular site can detect targets which are flying over the hostile terrain in specified altitudes and routes.

INPUT: This function prompts two inputs:

1. The minimum altitudes of the radar site given by the "MINALT" computer work space.
2. The flight data of the targets given by the "MOVEMENT" computer work space.

OUTPUT: The output of this function is a $(M, N+1)$ matrix where:

K = The number of time steps

The first column is the time step

N = The number of target.

2. Error

See Appendix D

B. "TARGET INTERCEPTION" MODEL

The "TARGET INTERCEPTION" work space is called "INTERCPT" and it consists of two functions: INTER and ERROR.

1. Inter

PURPOSE: The purpose of the function "INTER" is to calculate Interception Data (INTERCEPTION STATE MATRIX).

INPUT: The function INTER prompts the following inputs:

1. The time of the time step of the simulation (in sec).
2. The location (X,Y) of the missile radar site (in N.M.).
3. The detection file (detects 1 or 2 etc), given by the "FDETECT" workspace, of the radar site which supports the interceptor missile.
4. The maximum range of the interceptor missile (in N.M.).
5. The speed of the interceptor missile (in knots).
6. The flight target data (target 1 or 2 etc), given by the "MOVEMENT" workspace for each target.

Note: The order of entering the flight data of the targets must be in ascent order i.e. the target 1 must be entered

first, the target 2 second and so on
until all targets are entered in the
program.

OUTPUT: The output of this program is a $(N, 1+(M*3))$
matrix, where:

K = The number of time steps

The first column is the time steps from 1 to
 K

N = The number of targets

Each target has two columns:

First column = 1, if the interception is
possible.

0, if the interception is not possible.

Second column = The number of time steps
that a possible interception takes,
otherwise zero.

Third column = The distance between radar
site and target.

C. "TARGET PRIORITY" MODEL

The TARGET PRIORITY model computer workspace is called
"PRIORITY" and it consists of one function: PRIORITY.

1. Priority

PURPOSE: The purpose of the function "PRIORITY" is
to calculate the priority of each target
when a radar site detects more than one
target simultaneously.

INPUT: This function prompts two inputs:

1. The critical course to which the target flight courses will be compared.
2. The target flight data given by the "MOVEMENT" computer program.

OUTPUT: The output of this function is a $(m, 1+N)$ matrix, where:

K = The number of time steps from 0 to M

The first column is the time steps

N = The number of targets.

The values in the matrix represent priority number.

```

▽ DETECT;A;A2;X;SX;Y;SY;TGT;ZERO;M;D;K;R;I;A1;ALT;KK;MALT;MALTI;P
[1]  A
[2]  A----- PURPOSE -----+
[3]  A
[4]  A THIS PROGRAM IS USED TO FIND OUT IF A PARTICULAR RADAR SITE
[5]  A CAN 'SEE' TARGETS WHICH ARE FLYING OVER THE HOSTILE TERRAIN
[6]  A IN SPECIFIED ALTITUDES AND ROUTES.
[7]  A
[8]  A----- INPUTS -----+
[9]  A
[10] A THIS PROGRAM PROMPTS TWO INPUTS:
[11] A
[12] A 1. THE MINIMUM ALTITUDES OF THE RADAR SITE GIVEN BY THE 'MINALT'
[13] A PROGRAM.
[14] A 2. THE FLIGHT DATA OF THE A/C (TARGET1 OR 2 ETC) GIVEN BY THE
[15] A PROGRAM 'MOVEMENT'.
[16] A
[17] A----- OUTPUTS -----+
[18] A THE OUTPUT OF THIS PROGRAM IS A (M N) MATRIX WHERE:
[19] A
[20] A M = THE NUMBER OF TIME STEPS
[21] A N = THE NUMBER OF TARGETS
[22] A
[23] A----- MAIN PROGRAM -----+
[24] A
[25] D=A1+10
[26] 'ENTER THE MINIMUM ALTITUDES OF THE RADAR SITE ( MALTIS1,2, ETC )'
[27] MALTI=0
[28] L4: 'ENTER THE TARGET FLIGHT DATA ( TARGET1,2,ETC )'
[29] TGT=0
[30] →((PTGT[;1])=6)/L3
[31] ERROR →L4
[32] L3:K=0 → D=D,(PTGT[2;1] → SX+(TGT[2;1]÷6) → SY+(TGT[3;1]÷6) → P=PSX
[33] L10:K=K+1
[34] ALT=TGT[4;1]K → X=SX[K]
[35] →(X#0)/L12 A CHECK IF THE TARGET HAS ENTERED INTO THE HOSTILE AREA

```



```

[36] A1-A1,0 0 →L13
[37] L12:MALT-MALTI(X+SX[K];Y+SY[K]) A0 X 0 Y 0 MALT 0 ALT
[38] →(MALT*-1)/L9 A CHECK IF THE TGT IS INSIDE THE MAX RANGE OF SITE.
[39] A1-A1,0 0 →L13
[40] L9:→(ALT-MALT)/L11 A- CHECK IF THE ALT OF THE TGT IS HIGHER THAN
[41] A----- THE RADAR SITE ALTITUDE.
[42] A1-A1,0 0 →L13
[43] L11:A1-A1,1
[44] L13:→(KKP)/L10
[45] ''
[46] 'IF YOU HAVE AN ANOTHER TARGET ENTER 0'
[47] 'IF YOU LIKE TO EXIT ENTER 1'
[48] KK=0
[49] →(KK=0, KK=1, KK=2)/L4, L7, L6
[50] L6:ERROR 0 →L7
[51] L7:A2+((pD), (M-1+(D[+D]))p0
[52] I+1
[53] L8:A2[I;]→((D[I]+A1), (M-D[I])p0) 0 A1-D[I]+A1 0 I+I+1
[54] →(IS(pD))/L8
[55] A3-(((M,1)pM),0A2)
[56] A3
[57] '' 0 ''
[58] '-----'
[59] ' THE OUTPUT IS STORED UNDER THE VARIABLE A3'
[60] '-----'

```

W:W2; X0:X1;XR:XS;XT:AC;TEST:AA;DIST
 7 INTER;A;ANS;D;DF;DF1;DIR:I;K:L:M;MM;Q;RMAX;RO;RO1;SPEED;T:TGT;TI;V1;V2;VR;

```

[1] A A----- PURPOSE -----+
[2] A
[3] A THIS PROGRAM IS USED TO CALCULATE THE INTERCEPTION STATE MATRIX
[4] A FOR EACH RADAR SITE
[5] A-----INPUT -----+
[6] A
[7] A THIS PROGRAM PROMPTS THE FOLLOWING INPUTS:
[8] A
[9] A 1. THE TIME OF THE TIME STEP OF THE SIMULATION (IN SEC).
[10] A
[11] A 2. THE LOCATION (X,Y) OF THE MISSILE RADAR SITE (IN N.M).
[12] A
[13] A 3. THE DETECT FILE (DETECTS1 OR 2 ETC) GIVEN BY THE 'FDETECT'
[14] A WORKSPACE. THIS RADAR SITE IS SUPPOSED TO SUPPORT THE
[15] A INTERCEPTOR MISSILE OR A/C.
[16] A
[17] A 4. THE MAXIMUM RANGE OF THE INTERCEPTOR MISSILE (IN N.M)
[18] A
[19] A 5. THE SPEED OF THE INTERCEPTOR MISSILE (IN KNOTS)
[20] A
[21] A 6. THE FLIGHT TARGET DATA (TARGET1 OR 2 ETC) GIVEN BY THE
[22] A 'MOVEMENT' WORKSPACE.
[23] A
[24] A NOTE: THE ORDER OF ENTERING THE FLIGHT DATA OF THE TARGETS
[25] A ---- MUST BE IN ASCENT ORDER. I.E: YOU MUST ENTER THE
[26] A TARGET1 FIRST THE TARGET2 SECOND AND SO ON UNTIL
[27] A ALL TARGETS ARE ENTERED IN THE PROGRAM.
[28] A

```

```

[36] A1=A1,0  $\diamond$   $\rightarrow$  L13
[37] L12:MALT=MALT(X-SX[K];Y-SY[K])  $\wedge$  X  $\diamond$  Y  $\diamond$  MALT  $\diamond$  ALT
[38]  $\rightarrow$  (MALT#1)/L9  $\wedge$  CHECK IF THE TGT IS INSIDE THE MAX RANGE OF SITE.
[39] A1=A1,0  $\diamond$   $\rightarrow$  L13
[40] L9: $\rightarrow$  (ALT>MALT)/L11  $\wedge$  CHECK IF THE ALT OF THE TGT IS HIGHER THAN
[41]  $\wedge$  ----- THE RADAR SITE ALTITUDE.
[42] A1=A1,0  $\diamond$   $\rightarrow$  L13
[43] L11:A1=A1,1
[44] L13: $\rightarrow$  (KKP)/L10
[45] ''
[46] 'IF YOU HAVE AN ANOTHER TARGET ENTER 0'
[47] 'IF YOU LIKE TO EXIT ENTER 1'
[48] KK#0
[49]  $\rightarrow$  (KK=0, KK=1, KK#2)/L4, L7, L6
[50] L6:ERROR  $\diamond$   $\rightarrow$  L7
[51] L7:A2=(( $\rho$ D), (M+1( $\Delta$ C $\rightarrow$ D))) $\rho$ 0
[52] I+1
[53] L8:A2[I;] $\rightarrow$  (( $\Delta$ C[I] $\rightarrow$ A1), (M- $\Delta$ C[I]) $\rho$ 0)  $\diamond$  A1- $\Delta$ C[I] $\rightarrow$ A1  $\diamond$  I+I+1
[54]  $\rightarrow$  (IS( $\rho$ D))/L8
[55] A3=(( (M,1) $\rho$ M),  $\rho$ A2)
[56] A3
[57] ''  $\diamond$  ''
[58] '-----'
[59] ' THE OUTPUT IS STORED UNDER THE VARIABLE A3'
[60] '-----'

```

```

 $\nabla$  INTER:A;ANS;D;DF;DF1;DIR;I;K;L;M;MM;Q;RMAX;RO;RO1;SPEED;T;TGT;TI;V1;V2;VR;
W;W2;X0;X1;XR;XS;XT;AC;TEST;AA;DIST
[1]  $\wedge$   $\rightarrow$  ----- PURPOSE -----+
[2]  $\wedge$ 
[3]  $\wedge$  THIS PROGRAM IS USED TO CALCULATE THE INTERCEPTION STATE MATRIX
[4]  $\wedge$  FOR EACH RADAR SITE
[5]  $\wedge$  -----INPUT -----+
[6]  $\wedge$ 
[7]  $\wedge$  THIS PROGRAM PROMPTS THE FOLLOWING INPUTS:
[8]  $\wedge$ 
[9]  $\wedge$  1. THE TIME OF THE TIME STEP OF THE SIMULATION (IN SEC).
[10]  $\wedge$ 
[11]  $\wedge$  2. THE LOCATION (X,Y) OF THE MISSILE RADAR SITE (IN N.M).
[12]  $\wedge$ 
[13]  $\wedge$  3. THE DETECT FILE (DETECTS1 OR 2 ETC) GIVEN BY THE 'FDETECT'
[14]  $\wedge$  WORKSPACE. THIS RADAR SITE IS SUPPOSED TO SUPPORT THE
[15]  $\wedge$  INTERCEPTOR MISSILE OR A/C.
[16]  $\wedge$ 
[17]  $\wedge$  4. THE MAXIMUM RANGE OF THE INTERCEPTOR MISSILE (IN N.M)
[18]  $\wedge$ 
[19]  $\wedge$  5. THE SPEED OF THE INTERCEPTOR MISSILE (IN KNOTS)
[20]  $\wedge$ 
[21]  $\wedge$  6. THE FLIGHT TARGET DATA (TARGET1 OR 2 ETC) GIVEN BY THE
[22]  $\wedge$  'MOVEMENT' WORKSPACE.
[23]  $\wedge$ 
[24]  $\wedge$  NOTE: THE ORDER OF ENTERING THE FLIGHT DATA OF THE TARGETS
[25]  $\wedge$  ---- MUST BE IN ASCENT ORDER. I.E: YOU MUST ENTER THE
[26]  $\wedge$  TARGET1 FIRST THE TARGET2 SECOND AND SO ON UNTIL
[27]  $\wedge$  ALL TARGETS ARE ENTERED IN THE PROGRAM.
[28]  $\wedge$ 

```

```

[96] A----- ANGLE BETWEEN TARGET AND INTERCEPTOR = 0 DEGREE-----
[97] L3:VD=V1+V2
[98] A 'TIME FOR INTERCEPTION (IN MIN) =',3T+(D÷VD)×60
[99] A 'DISTANCE FOR TARGET = ',3T×(V1÷60)
[100] A 'DISTANCE FOR INTERCEPTOR =',3T×(V2÷60)
[101] Q=T×(V2÷60)
[102] L10:Q ÷ →(Q$RMAX)/L11
[103] A=A,0,0 ÷ DIST-DIST,0 ÷ →LP1
[104] L11:DIST-DIST,(LD) A CREATES THE DISTANCE VECTOR
[105] A=A,1,↑((T×60)÷TI) ÷ →LP1
[106] END:A1←((PDF),2)PA ÷ DIST←((PDF),1)PDIST
[107] 'AA-AA,A1,DIST ÷ A1-AA
[108] 'IF YOU HAVE ANOTHER TARGET ENTER 0'
[109] 'TO EXIT ENTER 1'
[110] AN=0
[111] →(AN=0)/L14
[112] '-----
[113] ' THE OUTPUT IS STORED UNDER THE VARIABLE A1'
[114] '-----

```

```

▽ PRIORITY:TGT1:TGT2;AN:A:A1;K:T;I:P:P1;DIR1;DIR2;DIR3;ALT1;V:M:TGT;DEGREE
[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS PROGRAM IS USED TO FIND OUT THE PRIORITY OF THE TARGETS
[5] A TO BE KILLED BY THE ENEMY RADAR SITES, AS FAR AS, HOW DANGEROUS
[6] A THE TARGET IS, IS CONCERNED.
[7] A
[8] A----- INPUTS -----+
[9] A
[10] A THIS PROGRAM PROMPTS THREE INPUTS:
[11] A
[12] A 1. THE CRITICAL COURSE THAT THE TARGET FLIGHT COURSES WILL BE
[13] A COMPARED.
[14] A
[15] A 2. THE TARGET FLIGHT DATA (TARGET1,2 ETC) GIVEN BY THE 'MOVEMENT'
[16] A PROGRAM.
[17] A
[18] A----- OUTPUT -----+
[19] A
[20] A THE OUTPUT IS A (M N+1) MATRIX WHERE:
[21] A
[22] A M = THE NUMBER OF TIME STEPS
[23] A N = THE NUMBER OF TARGETS
[24] A THE FIRST COLUMN IS THE TIME STEPS
[25] A
[26] A----- MAIN PROGRAM -----+
[27] A
[28] TGT1←TGT2←DIR1←DIR3←ALT1←V←0 ÷ P←0
[29] 'ENTER THE CRITICAL COURSE'
[30] DEGREE←0 ÷ ''
[31] L1:'ENTER THE TARGET FLIGHT DATA (TARGET1,2,ETC)'
[32] TGT←0 ÷ P←P+1 ÷ V←V,PTGT[1:]
[33] TGT1←TGT1,TGT[4:]
[34] TGT2←TGT2,TGT[5:]
[35] K←P(TGT[1:])
[36] L4:'IF YOU HAVE ANOTHER TARGET ENTER 0'
[37] ' OTHERWISE ENTER 1'
[38] AN←0
[39] →((AN=0),(AN=1),(AN=2))/L1,L2,L3
[40] L3:ERROR ÷ →L4
[41] L2:A←A1←(P,(M←(1↑(V[↑V]))))P ÷ I←1
[42] L6:A[I:]←((V[I])↑TGT1),(M-V[I])P ÷ TGT1←(V[I])↑TGT1
[43] A1[I:]←((V[I])↑TGT2),(M-V[I])P ÷ TGT2←(V[I])↑TGT2 ÷ I←I+1

```

```

[44]  $\rightarrow (ISP) / L6$ 
[45]  $K \leftarrow 1$ 
[46]  $L7: I \leftarrow 1 \diamond DIR1 - ALT1 - 10$ 
[47]  $LS: DIR1 \leftarrow DIR1, A[I:J][K]$ 
[48]  $ALT1 \leftarrow ALT1, A[I:J][K]$ 
[49]  $I \leftarrow I + 1$ 
[50]  $\rightarrow (ISP) / L5$ 
[51]  $K \leftarrow K + 1$ 
[52]  $T \leftarrow P1 \leftarrow 0 \diamond DIR1 \leftarrow (P) \rho DIR1$ 
[53]  $L8: T \leftarrow T + 1$ 
[54]  $\rightarrow (DIR1[T] \neq 0) / L9$ 
[55]  $DIR1[T] \leftarrow 1000 \diamond P1 \leftarrow P1 + 1$ 
[56]  $L9: \rightarrow (T < (\rho DIR1)) / L8$ 
[57]  $L9: DIR2 \leftarrow \rightarrow (180 - DIR1) \diamond DIR2[P1] \leftarrow 0$ 
[58]  $DIR3 \leftarrow DIR2, \oplus DIR2$ 
[59]  $\rightarrow (K \leq M) / L7$ 
[60]  $A3 \leftarrow ((M, 1) \rho \nu M), (M, P) \rho DIR3$ 
[61]  $A3$ 
[62] '-----'
[63] '      THE OUTPUT IS STORED UNDER THE VARIABLE A3'
[64] '-----'

```

▽

APPENDIX F

This Appendix contains all the computer programs of the "AIRMODEL" workspace.

```

      ▽ MAIN:CMD;WTH;STEP;CAFF2;TK1;ADSITES;AISITES;NSITES;SDD2;P;MCAFF2;I1;I2;I3;
R1;R2;R3;T;TIMES
[1]  A
[2]  A----- PURPOSE -----+
[3]  A
[4]  A  THE PURPOSE OF MAIN PROGRAM IS TO COMBINE THE DATA BASE WITH
[5]  A  THE FUNCTIONS USED TO CALCULATE THE ATTRITION RATE OF THE
[6]  A  AIRCRAFT FORMATION.
[7]  A
[8]  A----- INPUT -----+
[9]  A
[10] A  THE MAIN PROGRAM PROMPTS THE FOLLOWING INPUTS:
[11] A
[12] A  1. RL:      THE SEED FOR THE RANDOM NUMBER FUNCTION.
[13] A  2. TIMES:   THE NUMBER OF TIMES THAT THE PROGRAM WILL RUN.
[14] A  3. NSITES: THE NUMBER OF THE RADAR SITES.
[15] A  4. DS2:    THE DETECTION MATRIX OF EACH RADAR SITE (GIVEN BY
[16] A             THE FDETECT PROGRAM).
[17] A  5. IS2:    THE INTERCEPTION MATRIX OF EACH RADAR SITE (GIVEN
[18] A             BY THE INTERCPT PROGRAM).
[19] A  6. TGT:    THE NUMBER OF AIRCRAFT THAT EACH FORMATION HAS.
[20] A  7. CAP2:   THE NUMBER OF TARGET THAT EACH RADAR SITE CAN
[21] A             ENGAGE.
[22] A  8. MCAF2:  THE NUMBER OF MISSILES EACH RADAR SITE HAS.
[23] A  9. PKM:    THE PROBABILITY OF KILL MATRIX.
[24] A 10. IFF:    THE DECISION IF IFF EXISTS.
[25] A 11. IFFWORK: THE PROBABILITY THAT IFF WORKS.
[26] A 12. IFFFOF: THE DECISION IF THE TARGET IS FRIEND OR FOE, GIVEN
[27] A             THAT IFF DOES NOT WORK.
[28] A 13. IFFCOR:  THE PROBABILITY THAT IDENTIFICATION IS CORECT,GIVEN
[29] A             THAT IFF WORKS.
[30] A 14. ECM:    THE ELECTRONIC COUNTERMEASURE MEANS MATRIX FOR THE
[31] A             ECM FUNCTION GIVEN BY THE ECM MODEL.
[32] A 15. CMD:    THE DECISION FOR THE COMMAND AND CONTROL MODEL.
[33] A 16. AUTO:   THE NUMBER OF AIRCRAFTS ABOVE OF WHICH THE RADAR
[34] A             SITES OPERATE AUTONOMOUSLLY.
[35] A 17. PR:     THE PRIORITY MATRIX GIVEN BY THE PRIORITY MODEL.
[36] A 18. WTH:    THE DESITION FOR GOOD OR BAD RADAR SITE OPERATION.
[37] A 19. LBR:    THE FACTOR THAT THE PROBABILITY OF AQUASITION
[38] A             BREAKINK WILL INCREASE, GIVEN THAT THE OPERATION
[39] A             OF THE RADAR SITES IS DISGRADED.
[40] A 20. ETSF:   THE FACTOR THAT THE EVENT TIME STEPS MATRIX WILL
[41] A             INCREASE ,GIVEN THAT THE OPERATION OF RADAR SITES
[42] A             IS DISGRADED.
[43] A 21. TSTEP1: THE EVENT TIME STEPS MATRIX.
[44] A
[45] A----- OUTPUT -----+
[46] A
[47] A  THE MAIN PROGRAM GIVES THE FOLLOWING OUTPUTS:
[48] A
[49] A  1. A SUMMARY OF THE USED SENARIO.
[50] A  2. IN DETAILS ATTRITION MATRIX.
[51] A  3. REMAIN MISSILES PER RADAR SITE.
[52] A  4. THE NUMBER OF TARGETS WHICH ARE KILLED BUT NO ASSESSED.
```

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[53] A      5. THE NUMBER OF KILLED TARGETS.
[54] A
[55] A----- COMMENTS -----+
[56] A
[57] A      THE MAIN PROGRAM CALLS THE FOLLOWING PROGRAMS:
[58] A
[59] A      1. SITE
[60] A
[61] A----- MAIN PROGRAM -----+
[62] A
[63] TGTSTAT←0
[64] 'ENTER THE NEW SEED'
[65] ORL←0
[66] 'ENTER THE NUMBER OF TIMES THE PROGRAM TO RUN'
[67] TIMES←0
[68] T←0
[69] LP3:←(T≥TIMES)/TELOS
[70] T←T+1
[71] ADSITES←AISITES←0
[72] A----- RADAR SITES DATA -----+
[73] A
[74] 'ENTER THE NUMBER OF THE RADAR SITES'
[75] NSITES←4 ♦ ' ♦ TESTMCAP←0
[76] P←0
[77] PP2:P←P+1
[78] →(P>NSITES)/PP1
[79] 'ENTER THE DETECTION MATRIX OF THE SITES',(*P)
[80] DDS2←0 ♦ ADSITES←ADSITES,(,DDS2) ♦ →PP2
[81] PP1:DDS2←(NSITES,(pDDS2[;1]),(pDDS2[1;]))pADSITES
[82] STGT←((NSITES),((pDDS2[1;1;1]-1))p((pDDS2[1;1;1]-1)))
[83] TESTINT←((NSITES),((pDDS2[1;1;1]-1))p1
[84] P←0
[85] PP3:P←P+1
[86] →(P>NSITES)/PP4
[87] 'ENTER THE INTERCEPTION MATRIX FOR THE SITES',(*P)
[88] IS2←0 ♦ AISITES←AISITES,(,IS2) ♦ →PP3
[89] PP4:MIS2←(NSITES,(pIS2[;1]),(pIS2[1;]))pAISITES
[90] I1←2 ♦ I2←3 ♦ I3←4 ♦ R1←R2←R3←0
[91] II1:←((pR1)≥((pDDS2[1;1;1]-1))/II2
[92] R1←R1,I1 ♦ R2←R2,I2 ♦ R3←R3,I3
[93] I1←I1+3 ♦ I2←I2+3 ♦ I3←I3+3 ♦ →II1
[94] II2:SEF←MIS2[;R1] ♦ STS←MIS2[;R2] ♦ STD←MIS2[;R3]
[95] ER9:'ENTER THE VECTOR NUMBER OF A/C THAT EACH TARGET HAS'
[96] TGT←0
[97] →((pTGT)=((pDDS2[1;1;1]-1))/ER8
[98] ERROR ♦ →ER9
[99] ER8:TGT1←TGT ♦ ALLTGT←0 (pTGT)
[100] PP6:'ENTER THE NUMBER OF TGTS THAT THE SITE CAN ENGAGE'
[101] CAP2←0 ♦ CAPP2←CAP2 ♦ '
[102] →((pCAP2)=NSITES)/PP7
[103] ERROR ♦ →PP6
[104] PP7:'ENTER THE NUMBER OF MISSILE THAT EACH SITE HAS (VECTOR)'
[105] MCAF2←0 ♦ MCAPP2←MCAF2 ♦ '
[106] →((pMCAF2)=NSITES)/PP8
[107] ERROR ♦ →PP7
[108] PP8:'ENTER THE PK MATRIX OF THE MISSILE FUNCTION'
[109] PKM←0 ♦ '
[110] ER2:'IF YOU LIKE IFF IDENTIFICATION ENTER 1'
[111] 'OTHERWISE ENTER 0'
[112] IFF←1 ♦ '
[113] →((IFF=0),(IFF=1))/ER3,ER10
[114] ERROR ♦ →ER2
[115] ER10:'ENTER THE PROBABILITY THAT THE IFF WORKS'
[116] IFFWORK←0 ♦ '
[117] →(IFFWORK≠0)/DD1
[118] ER1:'IF YOU LIKE ALL TGTS TO BE FRIENDS (IFF NOT WORK) ENTER 1'
[119] 'IF YOU LIKE ALL TGTS TO BE FOE ENTER 0'
[120] IFFFOF←0 ♦ '
[121] →((IFFFOF=0),(IFFFOF=1))/ER3

```



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[122] ERROR 0 -ER1
[123] DD1: 'ENTER THE PROB. THAT THE IDENTIFICATION IS CORRECT/IFF WORKS)'
[124] IFFCOR=0 0
[125] ER3: 'ENTER THE ECM MATRIX OF ECM FUNCTION'
[126] ECM=0 0
[127] TT1: 'IF YOU LIKE COMMAND CONTROL MODEL ENTER 1'
[128] 'OTHERWISE ENTER 0'
[129] CMD=0 0
[130] -(CMD=0)/ER4
[131] 'ENTER THE NUMBER OF AIRCRAFTS ABOVE OF WHICH THE RADAR'
[132] 'SITES OPERATES AUTONOMOUSLY'
[133] AUTO=0
[134] ER4: 'ENTER THE PRIORITY MATRIX'
[135] PR=0
[136] ER44: 'IF YOU LIKE GOOD RADAR SITE OPERATION ENTER 1'
[137] 'IF YOU LIKE DISGRADED RADAR SITE OPERATION ENTER 0'
[138] WTH=1 0
[139] -((WTH=0),(WTH=1))/ER5,ER55
[140] ERROR 0 -ER44
[141] ER5: 'ENTER THE INCREASE FACTOR FOR ACQUISITION BREAK PROBABILITY'
[142] LBR=0 0
[143] 'ENTER THE INCREASE FACTOR FOR EVENTS TIME STEPS MATRIX'
[144] ETSF=0 0
[145] TSTEP1-TSTEP-TSTEP1+LTSTEP1*(ETSF) A 'DISGRADED OPERATION
[146] ECMC;4]+ECMC;4]+ECMC;4]*LBR
[147] ER55: 'ENTER THE EVENTS TIME STEPS MATRIX(ID,TRACK,FIRE,ASSESS)'
[148] TSTEP=0 0 0 TSTEP1-TSTEP-((PTGT),(NSITES),4)*TSTEP
[149] DS2-DDS2 A DS2=THE DETECTION MATRIX OF SITE 2 + 10 ROWS
[150] ASS=0 0 TFERROR=1
[151] AS2-((NSITES,((PDS2[1;1]+10),1)*P((PDS2[1;1]+10))),((NSITES,((PDS2[1
;1]+10),(PALLTGT)))*P0)
[152] A----- TIME STEP LOOP -----+
[153] I=0
[154] ALP2:-(I>1)/END
[155] LP2:-(I2((PDS2[1;1])))/END
[156] I=I+1 0 0 I=,51
[157] A----- RADAR SITES LOOP -----+
[158] SS=0
[159] LP1:-(SS>NSITES)/LP2
[160] SS=SS+1
[161] A -(MCAPP2[SS]>0)/LLL1
[162] A -(I>TESTMCAPP[SS])/LP1
[163] '...SITE = ',SS
[164] SS SITE I
[165] -LP1
[166] END: A-----END OF THE SIMULATION-----+
[167] ' SENARIO'
[168] '-----'
[169] 'NUMBER OF TARGET PER FORMATION = ',TGT1
[170] 'TARGET CAPACITY PER MISSILE SITE = ',(SCAPP2)
[171] 'MISSILE CAPACITY PER MISSILE SITE = ',(MCAPP2)
[172] 'IFF = ',(SIFF)
[173] 'PROB THAT IFF WORKS = ',(SIFWORK)
[174] 'PROB THAT IDENTIF. IS CORRECT/IFF WORKS = ',(SIFFCOR)
[175] 'FRIEND/ENEMY IF IFF DOES NOT WORKS = ',(SIFFFOF)
[176] 'COMMAND CONTROL MODEL = ',(SCMD)
[177] 'RADAR OPERATION(GOOD/BAD) = ',(SWTH)
[178] 'ECM MATRIX = '
[179] ECM
[180] 'PK MATRIX = '
[181] PKM
[182] '----- RESULT -----'
[183] A
[184] -(IFF=0)/AS1
[185] 'TGT 2 HAS BE ENGAGED = ',(TFERROR-1)

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[186] AS1:TK1-0(((PTK)/3),3)PTK
[187] 'IN DETAILS ATTRITION MATRIX:'
[188] 'MISSILE SITE = ',(TK1[1;])
[189] 'TIME STEP = ',(TK1[2;])
[190] 'KILLED TGT = ',(TK1[3;])
[191] TGTSTAT-TGTSTAT,(TGT1-TGT)
[192] -LP3
[193] TELOS:TGTSTAT-0(T,(PTGT1))PTGTSTAT
[194] 'REMAIN MISSILES = ',MCAPI2
[195] 'NO ASSESS TGT = ',ASS
[196] 'KILLED TGTS (TGTSTAT)= ' 0 A,(TK1,TGTSTAT))
[197] TGTSTAT
[198] A----- ERASE GLOBAL VARIABLES -----+
[199] QO=DEX 'STGT TESTINT IS2 SEF STS STD TGT TGT1 ALLTGT CAP2 MCAPI2 IFF PR TS
TEP TSTEP1 DS2 RD RN NT PK I SS INT CHECK ISITE TK TK1 ASS ECM TFERROR TK1'

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▽ SS SITE I;EV;FF;ID;II;K;MT;NN;NT;Z;NT1;P;PRIOR;TT;Z;EV;TEST;AM;PKC
[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED TO CALCULATE THE ATTRITION RATE OF THE
[5] A ATTACKING AIRCRAFT FORMATIONS AGAINST GROUND TARGETS
[6] A
[7] A----- INPUT -----+
[8] A
[9] A THIS FUNCTION IS CALLED BY THE MAIN PROGRAM AND USES THE FOLLING
[10] A INPUTS:
[11] A 1. THE LEFT ARGUMENT IS THE NUMBER OF RARAR SITE
[12] A 2. THE RIGHT ARGUMENT IS THE TIME STEP
[13] A 3. SOME OTHER GLOBAL VARIABLES
[14] A
[15] A----- OUTPUT -----+
[16] A
[17] A THIS FUNCTION CALLS THE IDIF, TRACK, FIRE, ASSES,INTER ,RANDOM
[18] A AND PKILL FUNCTIONS IN ORDER TO PERFORM THE FUTURE EVENTS AND
[19] A CALCULATE THE ATRITION RATE.
[20] A
[21] A----- MAIN PROGRAM -----+
[22] A
[23] A----- INITIALIZE -----+
[24] A-(I>1)/CONT
[25] NT1=0 0 TK=0 A TIME/KILL VECTOR
[26] CONT:ISITE=I,SS ACONTAINS THE TIME STEP + THE NUMBER OF SITE CALLED
[27] A-((+/NN-1+AS2[SS;I;])=0)/L4 A CHECK IF THERE IS AN EVENT
[28] P=0 A 0 'THERE IS EVENTS' 0 'NN=',NN
[29] LP1:-(P2(PNN))/L7 A 0 LOOP FOR EVENTS
[30] P=P+1 A 0 'P=',P
[31] EV=NN[P]
[32] A-(EV=0)/LP1 A THE END OF THE EVENTS A 'EVENT=',EV
[33] EV=EV-2(SS), '00' A FORM THE EVENTS 0 'EV=',EV
[34] A-((EV<19),(EV<29),(EV<39),(EV<49),(EV<59))/EV1,EV2,EV3,EV4,EV5
[35] EV1:NT-EV-10 0 TT-ISITE TRACK NT 0 -LP1 A CALL THE TRACK FUNCTION
[36] EV2:NT-EV-20 0 FF-ISITE FIRE NT 0 -LP1 A CALL THE FIRE FUNCTION
[37] EV3:NT-EV-30 0 INT-ISITE INTER NT 0 -LP1 A CALL THE INTER FUNCTION
[38] EV4:NT-EV-40 0 AM-ISITE ASSES NT A CALL THE ASSES FUNCTION
[39] A
[40] A----- RESULT OF INTERCEPT -----+
[41] A-(TGT[NT]>0)/TT1
[42] A 'IF ALL A/C OF FORMATION ARE KILLED THE TGT GO OUT OF SIMULATION'
[43] A-(((PDS2[SS;,(NT+1)])-(I+ASES))>0)/TT2 A NO DETECTION STOP PROCCES
[44] A-LP1
[45] DS2[SS;((I+((PDS2[SS;,(NT+1)])-(I+ASES)))+I);(NT+1)]=0 0 -LP1
[46] A ALL DETECTION COLUMN FOR THIS TGT BECAMES ZERO
[47] TT1:-(MCAPI2[SS]=0)/LP1 A NO REMAIN MISSILE SITE OUT OF SIMULATION
[48] A-(TESTINT[SS;NT]=0)/LP1
[49] A IF NO INTERCEPT NO KILL COUNT

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[50] A----- PK FUNCTION -----+
[51] PK=PKM PKILL SS,STD[SS;I;NT] A CALL THE PK FUNCTION
[52] A 'PK = ',%PK A 'R= ',%STD[SS;I;NT]
[53] RN=RANDOM A 'RN = ',%RN A CALL THE RANDOM FUNCTION
[54] -(RN*PK)/RESS1
[55] 149 OPOKE 161 A 'KILL !!! ONE TARGET ',(%NT) A 26 OPOKE 161
[56] TGT[NT]-TGT[NT]-1 A TK-TK,SS,I,NT
[57] AKILL SUBSTRUCT ONE TGT FROM FORMATION
[58] MCAF2[SS]+MCAF2[SS]-1
[59] AKILL SUBSTRUCT ONE MISSILE FROM MISSILE STOCK
[60] TSTEP[NT;SS;]-TSTEP[NT;SS;]
[61] -(TGT[NT]<0)/TT2
[62] -LP1 A IF ALL A/C OF FORMATION ARE KILLED THE TGT GO OUT OF SIM.
[63] TT2:DS2[SS;((1((PDS2[SS;:(NT+1)]-I))+I);(NT+1)]-0 A -LP1
[64] RESS1:MCAF2[SS]+MCAF2[SS]-1 A NO KILL SUBSTRUCT ONE MISSILE
[65] TSTEP[NT;SS;]-TSTEP[NT;SS;] A -LP1
[66] A
[67] A----- RESULT OF ASSESS -----+
[68] EV5:
[69] NT=EV-50
[70] ES1: A 'THE TGT ',(%NT), ' ENTER AGAIN THE DETECTION LIST'
[71] A INITIALIZE AGAIN THE INTERCEPTION PROCCESS
[72] STGT[SS;NT]+NT A ALLTGT[NT]+NT A CAP2[SS]+CAP2[SS]+1
[73] A
[74] A----- DETECTION EVENT -----+
[75] L4:-L8 A 'NO CURRENT EVENTS'
[76] L7: A 'END OF EVENTS'
[77] L8:Z-1+DS2[SS;I;]
[78] -(CAP2[SS]>0)/L3 A --CAPACITY CONTITON
[79] -END A 'THE SITE2 IS FULL=',%CAP2[SS]
[80] L3:MT++/Z
[81] -((MT=0), (MT=1), (MT=2))/L0,L1,L2
[82] L0:-END A 'NO TARGET IN TARGET DETECTION LIST'
[83] A----- CASE THAT RADAR SITE CAN SEE ONLY ONE TGT -----+
[84] L1:NT+Z-1 A 'TGT TO BE ID1=',%NT
[85] -(Z[NT]>0)/D1
[86] -END A 'THE TGT=',(%NT), ' IS NOT IN DETECTION LIST'
[87] D1:-(STGT[SS;NT]>0)/AL1
[88] -END A 'THE TGT ALLREADY ID1 =',%NT A -END
[89] A----- COMMAND AND CONTROL MODEL -----+
[90] AL1:-(CMD=0)/L5
[91] -(ALLTGT[NT]>0)/L5
[92] -(TGT[NT]>AUTO)/L5 A NUMBER OF TGT GREATER THAN ONE
[93] -END A 'THE TGT ',(%NT), ' IS ALLREADY ENGAGED BY AN OTHER SITE'
[94] L5:CAP2[SS]+CAP2[SS]-1 A STGT[SS;NT]-0 A ALLTGT[NT]-0
[95] ID=ISITE IDIF NT A -END A CALL THE IDIF FUNCTION
[96] A----- CASE THAT RADAR SITE CAN SEE TWO OR MORE TGT -----+
[97] L2:PRIOR-1+PRIOR
[98] LP2:NT-1+PRIOR A PRIOR-1+PRIOR
[99] -(NT=0)/END
[100] -(Z[NT]>0)/D2
[101] -LP2 A 'THE TGT=',(%NT), ' IS NOT IN DETECTION LIST' A -LP2
[102] D2:-(STGT[SS;NT]>0)/AL2
[103] -LP2 A 'TARGET ALLREADY ID' A 'THE TGT VECTOR=',%STGT[SS;NT]
[104] A----- COMMAND AND CONTROL MODEL -----+
[105] AL2:-(CMD=0)/L6
[106] -(ALLTGT[NT]>0)/L6
[107] -(TGT[NT]>AUTO)/L6 A IF THE NUMBER OF TGT GREATER THAN VAR. AUTO
[108] A THEN THIS TGT IS ENGAGED BY MORE THAN ONE RADAR SITE
[109] -LP2 A 'THE TGT ',(%NT), ' IS ALLREADY ENGAGED BY AN OTHER SITE'
[110] L6:CAP2[SS]+CAP2[SS]-1 A STGT[SS;NT]-0 A ALLTGT[NT]-0
[111] A 'THE TGT VECT=',(%STGT[SS;NT])
[112] ID=ISITE IDIF NT A 'THE ID2 TGT=',%NT
[113] -LP2
[114] END:

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▽ ID-ISITE IDIF R;CHECK;II;RN;RD;IDD
[1]  A
[2]  A----- PURPOSE -----+
[3]  A
[4]  A THIS FUNCTION IS USED BY THE SITE FUNCTION TO PERFORM THE
[5]  A IDENTIFICATION OF THE TARGETS.
[6]  A
[7]  A----- INPUTS -----+
[8]  A
[9]  A 1. THE LEFT ARGUMENT IS A VECTOR WHOSE FIRST ELEMENT IS THE
[10] A NUMBER OF RADAR SITE AND THE SECOND ONE IS THE TIME STEP.
[11] A 2. THE RIGHT ARGUMENT IS THE NUMBER OF TARGET.
[12] A 3. THIS FUNCTION USES SOME OTHER GLOBAL VARIABLES.
[13] A
[14] A----- OUTPUT -----+
[15] A
[16] A THE OUTPUT IS THE FUTURE IDENTIFICATION EVENT
[17] A
[18] A----- MAIN PROGRAM -----+
[19] A
[20] I-ISITE[1] ♦ RD-ISITE[2] ♦ IDD+TSTEP[R;RD;1]
[21] A 'TGT=';R ♦ 'IDD=';IDD
[22] →(MCAP2[RD]♦0)/TT1 A NO MISSILE NO FUTURE EVENT
[23] →TT2
[24] TT1: A 'TARGET TO BE ID=';R
[25] →(IDD<((ρ(DS2[RD;R+1]))-I))/TT2 A SIMULATION OF ID STOP WHEN THE
[26] A REMAINING TIME STEPS ARE LESS THAN THE NUMBER THAT THE ID PROCESS
[27] A NEEDS
[28] ID←0 ♦ DS2[RD;(1+((ρ(DS2[RD;R+1]))-I))+I;R+1]←0 ♦ →END
[29] TT3:CHECK←×/((DS2[RD;R+1])[I+IDD] A CHECK IF THERE IS DETECTION
[30] A 'CHECK OF ID=';CHECK
[31] →(CHECK♦0)/L6
[32] A 'NO DETECTION ... NO IDENTIFICATION'
[33] DS2[RD;(I-1)+1(IDD+1);R+1]←0
[34] TT2:STGT[RD;R]←R ♦ ALLTGT[R]←R
[35] A 'TARGET';(R), ' AGAIN FOR DETECTION'
[36] ID←0 ♦ CAP2[RD]←CAP2[RD]+1 ♦ →END
[37] A----- TEST FOR IDENTIFICATION -----+
[38] L6:→(IFF=0)/L1 A IFF NO IFF IS APPLIED ALL TARGET ARE ENEMIES
[39] RN←RANDOM A♦ 'RN=';RN
[40] →((RN>IFFWORK),(RN≤IFFWORK))/L3,L4
[41] L3:→(IFFOF=0)/L1 ♦ A IF IFFOF = 0 ALL TARGETS ARE ENEMIES
[42] A IF IFFOF = 1 ALL TARGETS ARE FRIENDS
[43] ID←0 ♦ STGT[RD;R]←R ♦ ALLTGT[R]←R ♦ CAP2[RD]←CAP2[RD]+1 ♦ →END
[44] A♦ 'TARGET';(R), ' ENTER AGAIN' ♦ →END
[45] L4:RN←RANDOM A♦ 'RN=';RN
[46] →((RN≥IFFCOR),(RN≤IFFCOR))/L7,L8
[47] A IF IFF IS WRONG THE FRIEND TARGET IS ENEMY, AND THE ENEMY TARGET
[48] A IS FRIEND, IF THE IFF IS CORRECT THE OPPOSITE.
[49] L7:→(R=2)/L9 A NUMBER 2 TARGET IS FRIEND BY THE SCENARIO
[50] A 'TARGET';(R), ' ENTER AGAIN'
[51] ID←0 ♦ STGT[RD;R]←R ♦ ALLTGT[R]←R ♦ CAP2[RD]←CAP2[RD]+1 ♦ →END
[52] L9:TFERROR←TFERROR+1 ♦ →L1 A NUMBER A FRIEND TARGET IS ENGAGED
[53] L8:→(R=2)/L1 A NUMBER 2 TARGET IS FRIEND BY THE SCENARIO
[54] A 'TARGET';(R), ' ENTER AGAIN'
[55] ID←0 ♦ STGT[RD;R]←R ♦ ALLTGT[R]←R ♦ CAP2[RD]←CAP2[RD]+1 ♦ →END
[56] L1:II←(AS2[RD;(I+IDD);])♦0 A FINDS WHICH ELEMENT AS2 MATRIX IS ZERO
[57] AS2[RD;(I+IDD);II]←2(RD), '1', (R) A GENERATE EVENTS (1=IDENTIFICATION)
[58] ID←AS2[RD;I+IDD;]
[59] A 'THE EVENTS ROW FOR IDENTIFICATION IS =';ID←AS2[RD;I+IDD;]
[60] END:
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7 TT=ISITE TRACK T;CHECK;IIRD;TR1
[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED BY THE SITE FUNCTION TO PERFORM THE
[5] A TRACK TARGET EVENT.
[6] A
[7] A----- INPUT -----+
[8] A
[9] A 1. THE LEFT ARGUMENT IS A VECTOR WHOSE FIRST ELEMENT IS THE
[10] A RADAR SITE NUMBER AND THE SECOND ONE IS THE TIME STEP.
[11] A 2. THE RIGHT ARGUMENT IS THE NUMBER OF TARGET.
[12] A 3. THIS FUNCTION USES SOME OTHER GLOBAL VARIABLES.
[13] A
[14] A----- OUTPUT -----+
[15] A
[16] A THE OUTPUT IS THE FUTURE TRACK EVENT.
[17] A
[18] A----- MAIN PROGRAM -----+
[19] A
[20] I=ISITE[1] * RD=ISITE[2] * TR1=STEP[T;RD;2] * A 'TR=' , $TR1 * 'TGT=' , $T
[21] -(MCAP2[RD]>0)/L2
[22] -L3
[23] A----- ECM MODEL -----+
[24] L2:=(ECM[T;S]=0)/L11 A ECM DOES NOT EXIST
[25] RN=RANDOM
[26] -(RN>ECM[T;S])/L12 A ECM DOES NOT WORK
[27] PK=ECM PKILL T,STD[RD;I;T]
[28] RN=RANDOM
[29] +(RN<PK)/L33 ABREAK LOCK ON
[30] TSTEP[T;RD; 2 3]+TSTEP[T;RD; 2 3]+(TSTEP[T;RD; 2 3])*(PK)
[31] TR1=STEP[T;RD;2]
[32] -L1 A 'NO LOCK BREAK NEW TSTEP=' * 'PK=' , $PK * TSTEP * -L1
[33] L12:-L1 * A 'ECM DOES NOT WORK' * 'ECM=' , $ECM[T;S] * 'RN=' , $RN * -L1
[34] L11:-L1 A 'ECM DOES NOT EXIST' * -L1
[35] L1:=(TR1*((P(DS2[RD;T+1]))-I))/L5
[36] TT=0 * DS2[RD;T+1]+((P(DS2[RD;T+1]))-I)+I;T+1=0 * -END
[37] L5:CHECK=*(DS2[RD;T+1])[I+TR1]
[38] A 'TEST = ' , $TEST * 'CHECK FOR TRACK=' , $CHECK
[39] -(CHECK#0)/L4
[40] DS2[RD;(I-1)+I+TR1+1;T+1]=0 * -L3
[41] A 'TGT = ' , ($T) , ' AGAIN FOR DETECTION'
[42] L33:'BREAK LOCK ON' * 'PK=' , $PK * 'RN=' , $RN * DS2[RD;I;(T+1)]=0 * -L3
[43] L3:TT=0 * STGT[RD;T]+T * ALLTGT[T]+T A 'TARGET = ' , ($TARGET)
[44] CAP2[RD]+CAP2[RD]+1 * -END
[45] L4:II=(AS2[RD;I+TR1;1])=0 HIT FINDS WHICH ELEMENT OF AS2 MATRIX IS ZERO
[46] AS2[RD;(I+TR1);II]=2($RD) , '2' , ($T) * GENERATE EVENTS (2=TRACK)
[47] TT=AS2[RD;I+TR1;]
[48] A 'THE EVENTS ROW FOR TRACK IS = ' , $TT-AS2[RD;I+TR1;]
[49] END:
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7 FR=ISITE FIRE F;CHECKRD;RD;FT
[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED BY THE SITE PROGRAM TO PERFORM THE
[5] A FIRE EVENT.
[6] A
[7] A----- INPUT -----+
[8] A
[9] A 1. THE LEFT ARGUMENT IS A VECTOR WHOSE FIRST ELEMENT IS THE
[10] A RADAR SITE NUMBER AND THE SECOND ONE IS THE TIME STEP.
[11] A 2. THE RIGHT ARGUMENT IS THE NUMBER OF TARGET.
[12] A 3. THIS FUNCTION USES SOME OTHER GLOBAL VARIABLES
[13] A

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[14] A----- OUTPUT -----+
[15] A
[16] A THE OUTPUT IS THE FUTURE FIRE EVENT.
[17] A
[18] A----- MAIN PROGRAM -----+
[19] A
[20] I←ISITE[1] ♦ RD←ISITE[2] ♦ FT←TSTEP[F;RD;3]
[21] →(MCAP2[RD]♦0)/L3
[22] →L4
[23] L3:→(FT<((ρ(DS2[RD;;F+1]))-I))/L5
[24] FR←0 ♦ DS2[RD;(ρ(DS2[RD;;(F+1)]))-I)+I;F+1]←0 ♦ →END
[25] L5:CHECK←×/(,DS2[RD;;F+1])[I+ρFT] A♦ 'TEST FOR FIRE=',§CHECK
[26] →(CHECK♦0)/L1
[27] DS2[RD;(I-1)+ρ(F+1);F+1]←0
[28] L4:FR←0 ♦ STGT[RD;F]←F ♦ ALLTGT[F]←F ♦ TSTEP[F;RD;]←TSTEP1[F;RD;]
[29] A 'TARGET ',(§F), ' ENTER AGAIN TO DETECTION LIST'
[30] CAP2[RD]←CAP2[RD]+1 ♦ →END
[31] L1:II←(AS2[RD;I+FT;])ρ0 A FINDS WHICH ELEMENT OF AS2 MATRIX IS ZERO
[32] AS2[RD;(I+FT);II]←2(§RD), '3', (§F) A GENERATE EVENTS (3=FIRE)
[33] FR←AS2[RD;I+FT;]
[34] L2: A 'THE EVENTS ROW FOR FIRE IS = ',§FR←AS2[RD;I+FT;]
[35] END:

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▽ INT←ISITE INTER IN;CH1;CH;NNN;II;RD

```

[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED BY THE SITE PROGRAM TO PERFORM THE
[5] A INTERCEPT OF THE TARGET.
[6] A
[7] A----- INPUT -----+
[8] A
[9] A 1. THE LEFT ARGUMENT IS A VECTOR WHOSE FIRST ELEMENT IS THE
[10] A RADAR SITE NUMBER AND THE SECOND ONE IS THE TIME STEP.
[11] A 2. THE RIGHT ARGUMENT IS THE NUMBER OF TARGET.
[12] A 3. THIS FUNCTION USES SOME OTHER GLOBAL VARIABLES.
[13] A
[14] A----- OUTPUT -----+
[15] A
[16] A 1. THE TIME THAT THE INTERCEPTION TAKES TO BE DONE.
[17] A 2. THE DISTANCE THAT THE TARGET FLY UNTIL GETS INTERCEPTED.
[18] A 3. THE DISTANCE THAT THE INTERCEPTOR FLY UNTIL THE INTERCE
[19] A PTION IS DONE.
[20] A
[21] A----- MAIN PROGRAM -----+
[22] I←ISITE[1] ♦ RD←ISITE[2]
[23] →(MCAP2[RD]♦0)/L6
[24] →L1
[25] L6: A NNN←IS2[RD;; 3 6 9]
[26] NNN←STS[RD;I;IN] A♦ 'NUMB. OF TIME STEPS=',§NNN
[27] →(NNN<((ρSEF[SS;;1])-I))/L4
[28] INT←0 ♦ DS2[SS;(I+(ρSEF[SS;;1])-I));IN+1]←0
[29] →END
[30] L4:CH←SEF[SS;I;IN] A♦ 'CHECK FOR INTERCEPTION=',§CH
[31] CH1←×/(,SEF[SS;;IN])[I+ρNNN] A♦ 'CH1=',§CH1
[32] →((CH=0),(CH1=0))/L1,L2
[33] →L3
[34] L1:INT←0 A♦ 'NO TRACK ...NO INTERCPTN'
[35] STGT[RD;IN]←IN ♦ ALLTGT[IN]←IN ♦ TSTEP[IN;RD;]←TSTEP1[IN;RD;]
[36] A♦ 'TGT = ',(§IN), ' ENTER AGAIN THE DETECTION'
[37] CAP2[RD]←CAP2[RD]+1 ♦ →END
[38] L2: 'LAUNCHING WAS SUCCESSFUL BUT ...NO INTERCEPTION DUE TO MASKING'
[39] TESTINT[SS;IN]←0 ♦ MCAP2[RD]←MCAP2[RD]-1 ♦ →L5
[40] L3:TESTINT[SS;IN]←1

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[41] L5:II+(AS2[RD;I+NNN;])\0 AFINDS WHICH ELEMENT OF AS2 MATRIX IS ZERO
[42] AS2[RD:(I+NNN);II]=2($RD),'4',($IN)
[43] INT=AS2[RD;I+NNN;]
[44] A 'THE EVENTS ROW FOR INTERCPT IS = ', $INT
[45] END:

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▽

▽ AM=ISITE ASSES AS;CHECK;II;RD;ASES

```

[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS CALLED BY THE SITE PROGRAM TO PERFORM
[5] A THE TARGET DAMAGE ASSESSMENT EVENT.
[6] A
[7] A----- INPUT -----+
[8] A
[9] A 1. THE LEFT ARGUMENT IS A VECTOR WHOSE FIRST ELEMENT IS THE
[10] A RADAR SITE NUMBER AND THE SECOND ONE IS THE TIME STEP.
[11] A 2. THE RIGHT ARGUMENT IS THE NUMBER OF TARGET.
[12] A 3. THIS FUNCTION USES SOME OTHER GLOBAL VARIABLES.
[13] A
[14] A----- OUTPUT -----+
[15] A
[16] A THE OUTPUT IS THE FUTURE TARGET DAMAGE ASSESSMENT.
[17] A
[18] A----- MAIN PROGRAM -----+
[19] I=ISITE[1] * RD=ISITE[2] * ASES=TSTEP[AS;RD;4]
[20] A IF THE RADAR DOES NOT HAVE TIME TO ASSES THE TGT (THE TGT
[21] A ENTER TO EACH OWN TERRAIN)
[22] A (ASES<((P(DS2[RD;AS+1]))-I))/L3
[23] AM=0 * DS2[RD:(L((P(DS2[RD;(AS+1))))-I))+I;AS+1]=0
[24] ASS=ASS+1 * -END
[25] A TEST IF THERE IS DETECTION DURING THE ASSES PROCCSS
[26] L3:CHECK= */TEST+(,DS2[RD;AS+1])[I+ASES]
[27] A * TEST = ', $TEST * 'CHECK FOR ASSES= ', $CHECK
[28] A -(CHECK#0)/L1
[29] AM=0 * ASS=ASS+1 * STGT[RD;AS]+AS * ALLTGT[AS]+AS
[30] * CAP2[RD]=CAP2[RD]+1 * -END
[31] A CREATE ESSES EVENTS
[32] L1:II=(AS2[RD;I+ASES;])\0 FINDS WHICH ELEMENT OF AS2 MATRIX IS ZERO
[33] AS2[RD:(I+ASES);II]=2($RD),'5',($AS)
[34] AGENERATE EVENTS (5=TGT ASSES)
[35] AM=AS2[RD;I+ASES;]
[36] A 'THE EVENTS ROW FOR ASSESSEMENT IS = ', $AM
[37] END:

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▽

▽ PK=PKM PKILL R:A:B:C:X1:X2:Y1:Y2:P

```

[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED TO CALCULATE:
[5] A 1.THE PROBABILITY THAT A MISSILE SITE KILLS A TARGET BY USING
[6] A THE APPROPRIATE FUNCTION (DATA IN PKM MATRIX)
[7] A 2.THE EFFECTIVENESS OF ECM BY USING THE APPROPRIATE FUNCTION
[8] A (DATA IN ECM MATRIX)
[9] A
[10] A----- INPUTS -----+
[11] A 1. THE FIRST ARGUMENT IS THE PK MATRIX OR THE ECM MATRIX
[12] A 2. THE SECOND ARGUMENT IS A TWO ELEMENTS VECTOR (SITE AND
[13] A DISTANCE
[14] A

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```

[15] A----- OUTPUT -----
[16] A
[17] A 1.THE PROBABILITY THAT A MISSILE SITE KILLS A TARGET
[18] A 2.THE EFFECTIVENESS OF ECM
[19] A
[20] A----- MAIN PROGRAM -----
[21] A+PKM(R[1];1)
[22] B+PKM(R[1];2)
[23] C+PKM(R[1];3)
[24] P+PKM(R[1];4)
[25] →(R[2]>A)/L1
[26] X1+Y1+0 ◊ X2+A ◊ Y2+P ◊ →L3
[27] L1:→(R[2]>B)/L2
[28] X1+A ◊ Y1+P ◊ X2+B ◊ Y2+P ◊ →L3
[29] L2:→(R[2]>C)/L4
[30] X1+B ◊ Y1+P ◊ X2+C ◊ Y2+0
[31] A----- THE USED FUNCTION -----
[32] L3:PK+(((R[2]-X1)×(Y2-Y1))÷(X2-X1))+Y1 ◊ →L5
[33] L4:PK+0
[34] L5:
▽

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▽ RN←RANDOM
[1] A
[2] A----- PURPOSE -----+
[3] A
[4] A THIS FUNCTION IS USED BY OTHER PROGRAMS TO GENERATE A RUNDOM
[5] A NUMBER
[6] A
[7] A----- INPUT -----+
[8] A
[9] A NONE
[10] A
[11] A----- OUTPUT -----+
[12] A
[13] A THE OUTPUT IS A RUNDOM NUMBER.
[14] A
[15] A----- MAIN PROGRAM -----+
[16] RN←(↑100)÷100
▽

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APPENDIX G

This Appendix contains all data of the pre-calculating phase of the air model. It also lists the data of the attrition rate of the three aircraft formations by running the dynamic phase of the air model.

ATTRITION RATE OF THE THREE AIRCRAFT FORMATIONS

1. NORMAL CASE

TARGET1

0 1 0 0 0 2 0 2 0 2 0 0 0 0 0 1 0 0 1 0 3 0 0 0 1 0 1 1 2 1 0 3 0 0 1 0 0 2 1
1 1 0 1 0 1 0 2 1 0 0

TARGET2

1 0 0 1 1 1 0 0 0 0 0 1 1 1 1 0 1 0 0 0 1 0 1 0 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0
1 1 1 0 1 0 1 0 1 1 0

TARGET3

1 2 3 2 2 3 2 1 3 4 1 3 4 2 2 2 2 3 3 2 2 2 1 2 4 1 0 0 5 3 2 1 2 1 1 1 1 1 3
3 2 3 3 3 4 1 2 2 3 4

2. CASE WITH DIFFERENT IFF PROBABILITIES

TARGET1

2 0 0 1 1 0 1 0 1 2 1 1 2 2 1 4 3 3 2 3 0 0 1 1 0 0 0 1 2 2 0 2 1 1 1 1 1 0 0
0 2 1 1 1 2 1 1 0 1 0

TARGET2

1 1 0 1 1 0 2 2 3 2 3 2 0 2 3 0 2 3 2 4 1 0 0 0 3 1 1 1 0 0 0 0 0 2 0 0 1 1 0
4 0 0 1 1 0 1 0 1 0 1

TARGET3

2 0 0 0 0 0 1 1 1 3 0 2 1 3 1 3 2 4 4 4 1 1 4 3 1 2 1 3 4 4 4 3 4 3 2 4 0 6 6
3 3 2 4 5 1 2 3 1 2 4

ATTRITION RATE OF THE THREE AIRCRAFT FORMATIONS ---

1. NORMAL CASE

TARGET1

0 1 0 0 0 2 0 2 0 2 0 0 0 0 0 1 0 0 1 0 3 0 0 0 1 0 1 1 2 1 0 3 0 0 1 0 0 2 1
1 1 0 1 0 1 0 2 1 0 0

TARGET2

1 0 0 1 1 1 0 0 0 0 0 1 1 1 1 0 1 0 0 0 1 0 1 0 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0
1 1 1 0 1 0 1 0 1 1 0

TARGET3

1 2 3 2 2 3 2 1 3 4 1 3 4 2 2 2 3 3 2 2 2 1 2 4 1 0 0 5 3 2 1 2 1 1 1 1 1 3
3 2 3 3 3 4 1 2 2 3 4

2. CASE WITH DIFFERENT IFF PROBABILITIES

TARGET1

2 0 0 1 1 0 1 0 1 2 1 1 2 2 1 4 3 3 2 3 0 0 1 1 0 0 0 1 2 2 0 2 1 1 1 1 1 0 0
0 2 1 1 1 2 1 1 0 1 0

TARGET2

1 1 0 1 1 0 2 2 3 2 3 2 0 2 3 0 2 3 2 4 1 0 0 0 3 1 1 1 0 0 0 0 0 2 0 0 1 1 0
4 0 0 1 1 0 1 0 1 0 1

TARGET3

2 0 0 0 0 0 1 1 1 3 0 2 1 3 1 3 2 4 4 4 1 1 4 3 1 2 1 3 4 4 4 3 4 3 2 4 0 6 6
3 3 2 4 5 1 2 3 1 2 4

3. CASE WHEN COMMAND AND CONTROL MODEL IS NOT APPLIED

TARGET1

1 0 0 0 1 0 0 0 1 0 0 0 0 1 0 1 1 2 0 1 0 1 1 0 0 0 1 0 0 0 1 0 0 0 0 1 0 1 1
2 0 1 1 0 1 0 0 0 1 0

TARGET2

1 2 0 2 1 2 1 1 0 1 3 0 3 1 4 1 0 1 2 2 1 2 1 2 0 2 1 2 1 1 0 1 3 0 3 1 4 1 0
1 2 2 2 2 1 2 0 2 1 2

TARGET3

2 5 1 2 1 2 5 4 2 3 3 4 0 1 1 5 1 2 5 5 1 2 2 5 1 2 1 2 5 4 2 3 3 4 0 1 1 5 1
2 5 5 0 4 2 5 1 2 1 2

4. CASE WHEN RADAR OPERATION IS DEGRADED

TARGET1

1 1 0 0 0 1 0 1 1 1 0 0 1 2 0 0 0 1 1 0 2 1 0 1 0

TARGET2

0 1 0 2 2 0 0 0 1 0 0 0 1 0 0 0 0 1 0 0 0 1 1 2 1

TARGET3

0 0 0 1 1 3 2 3 1 2 2 1 0 1 1 1 3 2 3 0 0 2 2 1 2

5. CASE WHEN ECM MODEL IS NOT APPLIED

TARGET1

0 1 1 1 0 0 0 1 1 0 1 2 1 0 0 0 1 1 1 1 1 1 0 0 2 1 1 1 2

TARGET2

1 3 0 1 1 0 1 2 1 0 1 1 0 0 2 1 1 1 1 1 0 3 2 0 2 0 1 0 1 0

TARGET3

5 5 3 3 5 7 1 5 5 4 4 4 4 5 1 6 1 3 4 1 3 3 3 6 5 5 7 5 5 4

 ATRITION RATE OF THE THREE AIRCRAFT FORMATIONS

1. FLIGHT LEVEL = 500 FEET

TARGET1

1 0 1 2 0 0 1 1 1 1 1 1 0 3 1 1 2 0 1 1 1 2 0 2 1 0 0 0 1 0 1 1 1 1 1 0 1 1 0
 2 1 1 0 0 2 0 0 2 0 1 1 1 2 0 2 1 0 0 0

TARGET2

0 0 0 2 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0 0 1 0 0 0 0 0 0 0
 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0

TARGET3

1 2 1 1 1 1 1 1 1 1 0 1 0 1 0 1 0 0 0 2 2 1 2 0 0 0 1 1 1 1 1 0 1 0 1 0 0 1 2
 0 0 1 0 1 1 0 1 0 0 0 2 2 1 2 0 0 0 1 1

2. FLIGHT LEVEL = 1000 FEET

TARGET1

0 1 0 0 0 2 0 2 0 2 0 0 0 0 0 1 0 0 1 0 3 0 0 0 1 0 1 1 2 1 0 3 0 0 1 0 0 2 1
 1 1 0 1 0 1 0 2 1 0 0

TARGET2

1 0 0 1 1 1 0 0 0 0 0 1 1 1 1 0 1 0 0 0 1 0 1 0 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0
 1 1 1 0 1 0 1 0 1 1 0

TARGET3

1 2 3 2 2 3 2 1 3 4 1 3 4 2 2 2 3 3 2 2 2 1 2 4 1 0 0 5 3 2 1 2 1 1 1 1 1 3
 3 2 3 3 3 4 1 2 2 3 4

3. FLIGHT LEVEL = 2000 FEET

TARGET1

1 1 1 0 1 1 0 0 0 0 0 1 1 0 1 1 1 1 0 0 1 1 0 1 0 1 1 0 1 2 0 4 1 0 0 1 1 1 1
1 1 0 2 0 0 0 1 0 1 1

TARGET2

0 1 1 1 1 1 0 0 0 0 0 1 0 0 1 0 1 1 0 0 3 0 1 0 0 0 0 0 0 0 0 0 0 1 0 1 1 0 1 1
0 2 1 0 1 0 0 0 0 1 0

TARGET3

1 1 2 2 2 2 1 2 2 2 2 2 1 2 2 1 4 4 5 1 1 0 3 2 4 3 1 3 0 3 3 2 2 1 2 1 2 2 3
5 4 2 2 0 2 2 1 1 2 2

4. FLIGHT LEVEL = 5000 FEET

TARGET1

0 0 0 3 0 1 2 1 0 1 0 0 1 0 1 0 0 1 3 0 1 1 2 1 2 1 0 1 1 1 2 2 1 0 1 0 1 1 0
1 1 1 1 1 0 0 3 2 1 3

TARGET2

0 0 1 0 0 1 0 1 0 0 0 1 0 0 1 1 0 1 1 1 0 1 0 0 2 2 0 1 0 0 0 0 2 0 1 0 1 0 2
0 1 1 0 0 0 3 1 1 0 2

TARGET3

1 2 1 0 1 5 2 4 1 1 2 2 2 1 2 2 2 2 0 0 2 1 0 4 2 2 3 2 1 1 2 1 2 4 3 1 1 2 2
2 1 3 4 1 4 0 2 2 1 4

5. FLIGHT LEVEL = 10000 FEET

TARGET1

1 0 0 3 0 2 0 0 0 0 1 0 1 0 1 0 0 1 1 1 2 1 1 0 0 0 0 0 1 2 2 1 1 0 1 1 2 2 1 0
1 1 0 2 1 0 0 0 0 0 0 0 2

TARGET2

2 0 1 0 1 1 0 0 1 0 0 0 0 0 1 0 1 0 0 0 1 0 0 0 1 1 1 1 1 0 0 1 2 1 1 0 0 1 0
0 1 0 0 1 1 1 0 1 0 0 0 1

TARGET3

0 4 2 1 2 1 1 3 2 0 3 2 2 0 3 1 5 2 2 1 1 1 2 1 1 3 1 2 2 2 3 1 3 1 0 1 1 2 0
3 1 3 1 0 1 1 2 4 3 3 1 1

ORIGINAL DATA OF THE SPECIFIC SENARIO

GRID SQUARE ALTITUDES

0	0	0	0	0	0	0	0	0	0	0	0	0	200
	500	600	800	50	0	0	0	0					
0	0	0	0	0	0	0	0	0	0	0	0	1500	1550
	1500	500	200	0	0	200	500	700					
0	0	0	0	0	0	0	0	0	0	500	2000	2000	
	1700	200	10	10	230	1000	510	750					
0	0	0	0	0	0	0	0	0	0	1000	1400	650	
	200	250	200	470	590	1100	520	600					

0	0	0	0	500	1500	250	0	0	0	2000	1500	500
	210	260	2300	500	510	900	1000	700				
0	0	0	3000	2000	1000	500	650	60	500	1000	1000	750
	520	2000	1500	1100	520	1000	350	310				
0	0	2500	4000	1500	2000	500	550	850	550	1100	250	2500
	3000	3100	2000	2980	510	250	100	40				
0	3500	2500	2500	2000	1000	200	1000	750	1000	250	2500	2000
	2100	3000	1100	1000	410	190	50	45				
350	2000	2100	1500	500	250	1500	3000	500	250	750	2200	2400
	2500	2600	2500	500	300	60	100	50				
2000	2750	1000	200	150	2000	2800	1000	750	2500	1800	2000	700
	1500	1000	750	100	60	190	120	150				
1500	1000	200	250	750	1750	2500	2600	2000	2000	1300	250	130
	290	150	20	60	80	200	130	200				
1600	210	900	1100	1700	2000	3500	3000	3100	800	650	150	120
	260	90	100	150	100	210	210	350				
300	1000	1500	2000	3000	2500	2000	1500	1500	1100	250	130	100
	100	80	100	190	180	230	210	1000				
1500	1600	2500	4000	3000	2000	1250	1500	500	250	150	140	110
	100	90	150	210	250	250	500	2100				
2500	2500	1750	3000	2750	2000	1000	250	200	150	150	140	110
	130	200	300	300	260	500	1050	1800				
3000	2700	2000	3100	1500	600	500	400	200	120	140	145	140
	180	250	350	500	410	1000	1500	1900				
2000	1100	650	3000	800	480	225	200	150	130	130	180	150
	210	480	500	300	580	2100	2000	1990				
1900	800	600	500	280	270	180	150	120	120	120	280	200
	400	510	1300	1000	1000	2600	2500	2000				
600	550	400	300	250	190	180	160	200	225	250	300	310
	700	1500	1600	2100	2900	3800	5000	4500				
1360	300	270	260	200	120	250	280	300	340	280	390	700
	1100	1000	2500	3000	3100	3200	3800	4900				
200	230	210	220	190	210	240	260	310	350	300	500	1480
	1150	1500	3400	3500	3200	5000	4900	4100				
190	180	170	180	150	220	250	265	320	360	540	1500	1500
	2100	3000	5000	4000	3700	6500	6900	7000				
180	170	200	240	160	230	270	280	330	500	800	2000	1600
	3000	3200	5200	7100	7000	8900	9050	8100				
220	240	250	260	260	260	280	500	700	2000	2800	2100	1800
	3100	7000	8100	9000	10100	9100	9200	9700				
270	270	260	270	275	280	700	750	1500	1000	3400	3100	4200
	4500	5500	8500	9500	11200	10000	11000	9900				
290	295	295	320	530	1400	1560	2000	2500	2500	3800	6000	6500
	8100	6500	7000	7500	10000	11000	13000	12000				
400	490	750	1500	1000	1700	2900	3000	3100	5000	6500	8000	8500
	9000	8500	10000	8000	7100	7500	7000	6000				
750	900	2000	1800	2000	3500	3600	5100	7000	7000	9000	9900	9500

OUTPUT OF TERRAIN MODEL

TERRAIN GRID SQUARE AVERAGE ALTITUDES

0	0	0	0	0	0	0	0	0	0	375	813	938
	775	525	263	13	50	175	300					
0	0	0	0	0	0	0	0	0	125	1000	1763	1688
	975	228	55	60	358	553	615					
0	0	0	0	0	0	0	0	0	375	1225	1513	1138
	588	165	173	325	730	783	595					
0	0	0	125	500	438	63	0	0	750	1475	1013	390
	230	753	868	518	775	880	705					
0	0	750	1375	1250	813	350	178	140	875	1375	938	495
	748	1515	1350	658	733	813	590					
0	625	2375	2625	1625	1000	550	528	490	788	838	1125	1693
	2155	2150	1895	1278	570	425	200					
875	2125	2875	2500	1625	925	563	788	788	725	1025	1813	2400
	2800	2300	1770	1225	340	148	59					
1463	2525	2150	1625	938	738	1425	1313	625	563	1425	2275	2250

	2550	2300	1275	553	240	100	62						
1775	1963	1200	588	725	1638	2075	1313	1000	1325	1688	1825	1775	
	1900	1713	963	240	153	118	105						
1813	1238	413	338	1163	2263	2225	1588	1813	1900	1338	770	655	
	735	480	233	75	133	160	150						
1078	578	613	950	1550	2438	2900	2675	1975	1188	588	163	200	
	198	90	83	98	148	188	223						
778	903	1375	1950	2300	2500	2500	2275	1625	700	295	125	145	
	133	93	135	155	180	215	443						
1100	1650	2500	3000	2625	1938	1563	1250	838	438	168	120	103	
	93	105	163	208	228	298	953						
2025	2088	2813	3188	2438	1563	1000	613	275	175	145	125	113	
	130	185	240	255	315	575	1363						
2675	2238	2463	2588	1713	1025	538	263	168	140	144	134	140	
	190	275	363	368	543	1013	1563						
2200	1613	2188	2100	845	452	332	238	150	130	149	154	170	
	280	395	413	448	1023	1650	1848						
1450	788	1188	1145	458	289	189	155	130	125	178	203	240	
	400	698	775	720	1570	2300	2123						
963	588	450	333	248	205	168	158	167	179	238	273	403	
	778	1228	1500	1750	2575	3475	3500						
703	380	308	253	190	185	218	235	267	274	305	425	703	
	1075	1650	2300	2775	3250	3950	4550						
523	253	240	218	180	205	258	288	325	318	368	768	1108	
	1188	2100	3100	3200	3625	4225	4425						
200	198	195	185	193	230	254	289	335	388	710	1245	1558	
	1938	3225	3975	3600	4600	5825	5725						
180	180	198	183	190	243	267	299	378	550	1210	1650	2050	
	2825	4100	5325	5450	6525	7838	7763						
203	215	238	230	228	260	333	453	883	1525	1925	1875	2375	
	4075	5875	7350	8300	8775	9063	9013						
250	255	260	267	269	380	558	863	1300	2300	2850	2800	3400	
	5025	7275	8775	9950	10100	9825	9950						
282	280	287	349	622	985	1253	1688	1875	2675	4075	4950	5825	
	6150	6875	8125	9550	10550	11250	11475						
369	458	717	838	1158	1890	2365	2650	3275	4450	6075	7250	8025	
	8025	8000	8125	8150	8900	9625	9500						
635	1035	1513	1575	2050	2925	3650	4550	5525	6875	8350	8975	9275	
	9650	10375	9275	7300	7225	7225	6775						

DATA OF RADAR SITE MINIMUM ALTITUDE MODEL

1. SITE 1

-1	-1	0	1	1	0	-1	-1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1	-1							
-1	1	0	0	1	0	1	1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1	-1							
-1	1957	1	1	1	66	0	229	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
2161	1841	1587	126	501	439	510	292	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
2145	1824	1567	1375	110	814	529	302	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
3495	2890	3283	2625	1626	1001	954	529	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
-1	4704	3977	3488	1977	2083	943	964	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
-1	-1	4846	3088	2392	2480	2691	-1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
	-1	-1	-1	-1	-1								

2. SITE 2

172

3. SITE 3

173

[illegible]

20787	20455	20246	20182	20204	20372	20663	21076	21609	22257	-1	-1	-1
	-1	-1	-1	-1	-1	-1	-1					
19123	18779	18562	18475	18518	18692	18994	19423	19973	20642	21425	22317	-1
	-1	-1	-1	-1	-1	-1	-1					
17527	17168	16942	16851	16896	17077	17393	17838	18409	19102	19910	20829	21853
	-1	-1	-1	-1	-1	-1	-1					
15998	15623	15386	15290	15338	15528	15858	16324	16919	17638	18475	19423	8119
	8684	-1	-1	-1	-1	-1	-1					
14540	14144	13894	13793	13844	14045	14392	14881	15504	16254	17123	18103	7505
	6594	7142	-1	-1	-1	-1	-1					
13153	12734	12467	12360	12413	12627	12997	13514	14169	14954	15858	6452	5630
	6114	6656	7257	-1	-1	-1	-1					
11841	11392	11106	10990	11048	11278	11674	12224	12918	13743	5527	4792	5212
	5690	5855	6428	7061	-1	-1	-1					
10607	10122	9810	9683	9747	9998	10427	11019	11757	4727	4081	4437	4851
	4990	5498	6065	6693	-1	-1	-1					
9458	8927	8581	8440	8511	8790	9262	9904	4054	3496	3788	4137	4250
	4692	5193	5755	6378	7061	-1	-1					
8404	7814	7422	7260	7342	7659	8187	8893	3038	3266	3318	3635	4011
	4446	4941	5498	6116	6726	-1	-1					
7462	6794	6338	6144	6242	6616	7219	2706	2869	2894	3144	3453	3821
	4250	1553	1199	1496	1853	-1	-1					
3650	5891	5338	5092	5217	5679	2501	2598	2594	2776	3017	3318	631
	737	431	616	672	965	-1	-1					
3442	3167	4454	4105	4287	2352	2359	2415	2528	695	608	242	103
	142	242	418	643	931	1282	-1					
2464	3035	2814	3188	2439	2370	1148	784	275	176	145	126	114
	146	241	399	620	905	1252	-1					
2675	2431	2463	-10	1714	1026	539	264	169	140	145	134	140
	190	289	452	677	965	1317	-1					
2478	2435	2189	2101	846	478	333	239	150	131	149	154	170
	280	395	570	807	1107	1650	-1					
2524	2013	2069	1813	1778	289	189	155	130	126	179	203	241
	400	699	905	1173	1570	-1	-1					
1963	1969	1552	1588	1569	1505	169	158	167	180	239	273	403
	779	1228	1501	1820	2575	-1	-1					
1989	1967	1407	1426	1416	1382	1339	336	267	275	305	426	703
	1075	1650	2301	2775	3250	-1	-1					
2059	2016	1319	1327	1323	1309	1295	1292	325	319	368	768	1108
	1291	2100	3100	3540	3677	-1	-1					
2181	1294	1291	1291	1291	1292	1300	1323	336	389	711	1245	1559
	1938	3225	3975	4470	-1	-1	-1					
2358	1340	1324	1318	1321	1333	1358	1402	1470	551	1210	1650	2050
	2825	4100	5325	5896	-1	-1	-1					
2593	1445	1419	1409	1414	1434	1473	1533	1621	1740	1926	1875	2375
	4075	5876	7350	-1	-1	-1	-1					
1668	1610	1576	1562	1569	1596	1646	1720	1824	2301	2850	2801	3400
	5025	7275	-1	-1	-1	-1	-1					
1904	1836	1795	1779	1787	1820	1878	1965	2082	2675	4075	4950	5826
	6150	6876	-1	-1	-1	-1	-1					
2200	2124	2078	2059	2069	2106	2365	2650	3275	4450	6075	7250	8025
	-1	-1	-1	-1	-1	-1	-1					
2557	2474	2423	2403	2413	2925	3650	4550	5525	6875	8350	8975	-1
	-1	-1	-1	-1	-1	-1	-1					

DATA OF MOVEMENT MODEL

1. TARGET1

TIME STEPS

1	2	3	4	5	6	7	8	9	10	11	12	13
	14	15	16	17	18	19	20	21	22	23	24	25
	26	27	28	29	30	31	32	33	34	35	36	37
	38	39	40	41	42	43	44	45	46	47	48	49
	50	51	52	53	54	55	56	57	58	59	60	61
	62	63	64	65	66	67	68	69	70	71	72	73
	74	75	76	77	78	79	80	81	82	83	84	85
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	254	255	256	257	258	259	260	261	262	263	264	265
	266											

X CORDINATE

2	3	4	5	6	7	9	10	11	12	13	14	16
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	2											

Y CORDINATE

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	108	108	108	107	107	107	106	105	105	104	104	103
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	78	77	76	75	74	73	72	71	70	68	67	66
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[illegible]

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	57	58	59	60	61	63	64	65	66	67	68	70
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	83	84	85	86	87	88	89	90	91	92	93	94
	96	97	98	99	100	101	102	103	104	105	106	107
	108	109	110	111	112	113	113	114	115	116	117	118
	119	120	121	121	122	123	124	125	126	127	128	128
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	140	141	142	143	143	144	145	146	147	148	149	150
	150	151	152	153	154	155	156	157	157			

Y CORDINATE

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	0	0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0	0	81
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72	71	71	70	70	70	70	69	69	69	69	69	69
69	69	69	69	68	68	68	68	68	68	68	68	68
67	67	67	67	67	67	67	67	66	66	66	66	66
66	66	65	65	64	64	63	63	62	61	61	61	60
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47	46	46	45	44	43	42	42	41	40	39	39	39
38	37	36	36	35	34	33	33	32	31	30	29	29
29	28	27	26	26	25	24	23	23	22	21	20	20
20	19	18	17	16	16	15	14	13	13	12	11	11
10	10	9	9	7	7	6	5	4				

ALTITUDES

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	0	0	0	0	0	0	0	0	0	0	0	20775
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21138	21138	21138	20390	20390	20390	20390	20390	20495	20495	20938	20938	20938
20938	20938	21125	21125	21125	21125	21813	21813	21813	21813	21813	21813	21813
22275	22275	22275	22275	22275	21825	21825	21825	21825	21825	21825	21825	20770
20770	20770	20770	20770	20163	20163	20163	20163	20588	20295	20295	20295	20295
20295	20295	20168	20168	20168	20168	20168	20168	20145	20145	20145	20175	20175
20175	20175	20140	20140	20140	20140	20140	20140	20130	20130	20130	20150	20150
20150	20130	20130	20130	20130	20130	20130	20167	20167	20158	20158	20158	20158
20158	20235	20235	10235	10235	10235	10218	10218	10258	10258	10258	10258	10258
10258	10258	10230	10230	10230	10230	10230	10230	10230	10243	10190	10190	10190
10190	10190	10190	10190	10228	10228	10230	10230	10230	10230	10230	10267	10267
10267	10267	10260	10260	10260	10260	10287	10287	10287	10287	10280	10280	10280
10280	10458	10458	10458	10458	10458	10369	10635	10635				

COURSE

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	0	0	0	0	0	0	0	0	0	0	0	109
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SPEED

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	0	0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0	0	420
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3. TARGET3

TIME STEPS

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72	73	74	75	76	77	78	79	80	81	82	83	84	85	
86	87	88	89	90	91	92	93	94	95	96	97	98	99	
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142	143	144	145	146	147	148	149	150	151	152	153	154	155	
156	157	158	159	160	161	162	163	164	165	166	167	168	169	
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254	255	256	257											

X COORDINATE

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73	74	75	77	78	79	80	81	82	83	84	85	86	87	
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6	5	3	2											

Y COORDINATE

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56	55	55	54	54	54	53	53	52	52	51	51	51	50	
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59	59	59	60	60	60	61	61	61	62	62	62	63	63	
63	64	64	64											

[illegible][illegible][illegible]

TARGET 3

[illegible]

DATA OF TARGET DETECTION MODEL

1. SITE 1

[illegible]

2. SITE 2

183

189

[illegible]

194

LIST OF REFERENCES

1. Cho, Chung Koo and Lee, Yong Il, A Generalized Approach to Air Defense Combat Modeling, Naval Postgraduate School, M.S. Thesis, Monterey, CA, September 1985.
2. Giordano, Frank R., and Weir, Maurice D., A First Course in Mathematical Modeling, Brooks/Cole Publishing Company, Monterey, CA.
3. Conover, W. J., Practical Nonparametric Statistics Second Edition, Wilent Sons, New York 1980

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| 13. | Major George Panagakos
Lakonias 12
Egaleo, Athens, GREECE | 3 |

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c.1

Panagakos

Modeling aircraft
attrition in the air
defense environment.

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